Diagnosis of induction motor failures using discrete wavelet transform of an auxiliary winding voltage

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ABSTRACT

Over last years, great attention has been developed to avoid the machines breakdown especially in the squirrel cage induction motor which suffer from different failures. The aim of this paper is to present a new method for the diagnosis of rotor bar breakage and end ring in induction machine fed by an inverter based on discrete wavelet transform applied on the voltage of an auxiliary winding as a new monitoring signature. The expression of the auxiliary winding voltage related to a small coil inserted between two stator phases is presented. The study is focused on the high-level signals of approximation and details coefficients. Thus, the evolution of any frequency of interest in the waveform is given in this paper. The method is validated by simulations of four broken bars and end ring cases under unloaded and loaded machine.

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1. INTRODUCTION

The squirrel cage induction machine is widely used in industrial applications, it represents more than 70% of the electrical machines due to its reliability and its low maintenance costs. However, this kind of machine is often subject to several constrains during its operation and it may suffer serious damage leading to its deterioration and fail. The production shutdowns are costly in terms of time lost, maintenance costs and can cause damage to other devises. Improving the electromechanical systems operation have attracted several researchers in order to avoid downtime of the machines and guarantee its overall performance. For that reason, the preventive maintenance is important. It is based on online monitoring and diagnosis of real-time signals. Multiple methods are used to investigate diagnosis process according to various faults occurring in the machine such as bearing faults, eccentricity, broken rotor bars and stator winding inter turn faults [1]. Condition monitoring and faults diagnostics using signal analysis are the most powerful methods to detect the machine failures at the initial stage without affecting the signal contain [2], [3]. The most classical one is the fast fourier transform (FFT) that is widely used for the detection of broken rotor bars in induction machine by transforming the signal from time domain to frequency domain. This approach gives satisfactory results if the signal monitored is stationary and the machine operates under steady state mode. However, the frequencies related to the presence of broken rotor bar fault can be detected by other causes such as bearing faults and voltage fluctuations [4]. Furthermore, the stationarity of the signal changes according to the stresses and the
environment that the machine is exposed to. In this case, the FFT cannot extract the inherent information of the non-stationary signals, the fundamental frequency can mask the small characteristic frequencies produced by broken bar faults making them undistinguishable. The time frequency analysis is required to overcome the FFT disadvantages such as the short-time fourier transform (STFT) [5] which performs temporal location of different frequency components of the signal. The resolution of this method uses a constant window size for all frequencies. To adjust the time widths to the frequency the wavelet transform (WT) is used [6]-[8]. A comparative study conducted by Kim et al. proves its effectiveness [9]. Thus, the transient component will be localized to extract the components associated to the failure evolution. The wavelet which is a small wave, has time-widths that automatically change with their frequencies. It provides simultaneously time and frequency information. The WT is a powerful diagnostic technique in power applications. Many research papers have been published in this field [10]-[16]. It uses multi-resolution technique depending on the different frequencies given by the signal that means for high frequencies, the wavelet uses a low time resolution whereas a high time resolution is reached for low frequencies. In general, the wavelet transform can be categorized in two forms: continuous wavelet transform (CWT) and discrete wavelet transform (DWT) used to extract the fast transition characterizing the failures of the signal after decomposition.

In fact, in a wide range of industrial application, induction motors are used with variable speed. For this reason, the present article establishes the detection of broken rotor bars and end rings of a squirrel cage induction motor fed by an inverter [17]. Due to the inaccessibility of direct measurements of rotor parameters in asynchronous motors, a new methodology for online fault detection is presented. It is based on monitoring a novel signal related to an auxiliary winding inserted inside the machine. It’s a small coil between two stator phases. The novelty of this article is to diagnose and monitor the auxiliary winding voltage through the analysis of discrete wavelet transform coefficients with a high-order mother wavelet.

2. DISCRETE WAVELET TRANSFORM

The discrete wavelet transform is one of the most powerful diagnosis techniques for analyzing time frequency representation of a signal by decomposing it in a set of sub-signals [18]-[20]. It is suitable for highlight the change occurs in the signal in early stage. This technique uses a multi-resolution in order to analyze the signal through different frequency band. According to Mallat algorithm [18], [21], each signal is associated with certain frequency band. The DWT leads to a signal decomposition into multiple small wave signals. The number of this decomposition is called levels (n). The decomposition is implemented using two filters: a low pass filter, denoted as h(k), containing low frequency component of the signal that determine approximation coefficient $a_{nj}$; and a high pass filter denoted as g(k) containing high frequency component that identifies the detail coefficient $d_j$. The sum of approximation coefficients and detail can reconstruct and approximate the signal as shown in (1).

$$s(t) = \sum_i a^n_i \phi^n_i(t) + \sum_{j=1}^{n} \sum_i \beta^j_i \psi^j_i(t) = a_n + d_n + \cdots + d_1$$ \hspace{1cm} (1)

Where $n$ is the decomposition level, $a^n_i$ is the scaling coefficients and $\beta^j_i$ is the wavelet coefficients, $\phi^n_i(t), \psi^j_i(t)$ are the scaling function at level $n$ and wavelet function at level $j$ respectively [22]. The frequency bands related to the detail coefficient $d_j$ and approximation coefficient $a_j$ are expressed as (2) and (3).

$$f_{dj} \in \left[ \left( \frac{fs}{2^{j+1}}, \frac{fs}{2^j} \right) \right]$$ \hspace{1cm} (2)

$$f_{aj} \in \left[ 0, \left( \frac{fs}{2^{j+1}} \right) \right]$$ \hspace{1cm} (3)

For the application of the discrete wavelet transform the selection of the mother wavelet and the determination of the number of decomposition levels are important [23]. Recently, several mother wavelets families exist with different properties categorized in two kinds of wavelet. The first one is the wavelet with infinite support such as Morlet, Gaussian, Meyer, Haar, and Mexican Hat. The second one is the compact supported wavelet which is divided into biorthogonal wavelet and orthogonal wavelet such as Daubechies or Coiflet. For this kind, a high-order mother wavelet is recommended for the extraction of the small frequencies and the reconstruction of the signal without losing information. The mother wavelet function generated by a translation (a) and a scale parameter (b) is defined as (4).

\[
\psi_{(a,b)}(t) = \frac{1}{\sqrt{b}} \psi \left( \frac{t-a}{b} \right) 
\]  
(4)

For the feature extraction, the used dyadic scales is discretized as \( a = 2^j \) where \( j \) denotes the level and \( b = 2 \). After that, the scalar product of this mother wavelet and a function \( f(t) \), gives the expression of the discrete wavelet function as (5).

\[
dwt(a, b) = (f, \psi_{(a,b)}) = \sum_{m=0}^{q} f(t_m) \frac{1}{\sqrt{b}} \psi \left( \frac{m-a}{b} \right) dt 
\]  
(5)

The filters used in the DWT are constructed from the selected mother wavelet \( (t) \) and the scaling function \( \phi(t) \) as (6).

\[
\begin{align*}
\psi(t) &= \sqrt{2} \sum_{k} g(k) \phi(2t - k) \\
\phi(t) &= \sqrt{2} \sum_{k} h(k) \phi(2t - k)
\end{align*}
\]  
(6)

With \( \sum_{k} g(k) = 0 \) and \( \sum_{k} h(k) = \sqrt{2} \). Therefore, the approximation and the detail coefficients corresponding to the low and high frequency components respectively are presented as (7).

\[
\begin{align*}
a_{j,k} &= \sum_{m} h(2k - m)a_{j-1,k} \\
d_{j,k} &= \sum_{m} g(2k - m)d_{j-1,k}
\end{align*}
\]  
(7)

For the best failures extraction, the number of decomposition levels depends on the sampling frequency. It can be determined by the follow (8).

\[
n = \text{integer}\left[ \frac{\log(f_s)}{\log(2)} \right] 
\]  
(8)

In this paper, Debauchies mother wavelet has been used for the DWT analysis in order to avoid overlapping between adjacent wavelet signals. The higher order Debauchies (dbN) gives an ideal failures extraction by using high number of filters, for db40, the filter length corresponding is \( L_{db40} = 2N = 80 \). The fundamental frequency is \( f_s = 50 \text{ Hz} \), the sampling frequency is \( f_s = 10,000 \text{ samples/s} \), the application of (6) leads to \( n = 7 \). According to (2) and (3) the frequency bands associated to each level is presented in Table 1. When the number of decomposition levels increase, the frequency bands of DWT correspondent decrease. The detail \( d_j \) includes the high frequency component of the signal and the low frequencies includes in \( a_j \).

<table>
<thead>
<tr>
<th>Levels</th>
<th>Approximation signals ( a_j ) (Hz)</th>
<th>Detail signals ( d_j ) (Hz)</th>
</tr>
</thead>
<tbody>
<tr>
<td>j=1</td>
<td>( a_1 ) 0-2500</td>
<td>( d_1 ) 2500-5000</td>
</tr>
<tr>
<td>j=2</td>
<td>( a_2 ) 0-1250</td>
<td>( d_2 ) 1250-2500</td>
</tr>
<tr>
<td>j=3</td>
<td>( a_3 ) 0-625</td>
<td>( d_3 ) 625-1250</td>
</tr>
<tr>
<td>j=4</td>
<td>( a_4 ) 0-312.5</td>
<td>( d_4 ) 312.5-625</td>
</tr>
<tr>
<td>j=5</td>
<td>( a_5 ) 0-156.25</td>
<td>( d_5 ) 156.25-312.5</td>
</tr>
<tr>
<td>j=6</td>
<td>( a_6 ) 0-78.125</td>
<td>( d_6 ) 78.125-156.25</td>
</tr>
<tr>
<td>j=7</td>
<td>( a_7 ) 0-39.0625</td>
<td>( d_7 ) 39.0625-78.125</td>
</tr>
</tbody>
</table>

3. **AUXILIARY WINDING VOLTAGE**

The aim of the proposed method consists of inserting a small coil as a “sneak” between two stator phases. The technic is built considering the auxiliary winding that forms an angle \( \theta_0 \) with the A stator phase as shown in Figure 1. Therefore, the inserted coil has no conductive contact with the other phases. It is coupled mutually with all the motor circuits in the stator and the rotor. The determination of the auxiliary winding voltage is the main key of this approach. Monitoring this signal is extremely beneficial to achieve an efficient diagnosis of the squirrel cage induction machine [24], [25]. This technic was applied previously for a wound rotor induction machine [26], [27]. The mathematical model of the squirrel cage induction machine fed by an inverter is presented in [17].

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The mathematical model of this method is presented in this section. As known, the voltage is a derivation of the flux. Therefore, the auxiliary winding voltage is expressed as (9).

\[ V_{aux} = \frac{d \phi_{aux}}{dt} \]  

(9)

From the current vector \( \mathbf{I} = [I_{sa}, I_{sb}, I_{sc}, I_{r1}, \ldots, I_{ri}, \ldots, I_{rn}] \) obtained from the squirrel cage induction machine fed by an inverter, the auxiliary winding flux is defined as (10).

\[ \phi_{aux} = a I_{sa} + b I_{sb} + c I_{sc} + \sum_{i=1}^{N_r} d_j I_{ri} \]  

(10)

The coefficients \( a, b, c \) and \( d_j \) depend on the angle \( \theta_0 \), as shown in [13],

\[ a = M_{aux} \cos(\theta_0), \quad b = M_{aux} \cos\left(\frac{2\pi}{3} - \theta_0\right), \quad c = M_{aux} \cos\left(\frac{4\pi}{3} - \theta_0\right), \quad d_j = M_{aux} \cos\left(\theta + \frac{j\pi}{3}\right), \quad j = 0, 2, 4, \ldots \]

\( M_{aux}, M_{aux} \) are the mutual inductances of the inserted coil with the stator phases and the rotor bars respectively. In order to form a three-phase system with the auxiliary winding, we consider two other fictive coils. Their shift phase angles are 120°. The expressions of the voltage in these fictive coils are (11).

\[ V_{auxa} = \frac{d \phi_{auxa}}{dt}, \quad V_{auxb} = \frac{d \phi_{auxb}}{dt}, \quad V_{auxc} = \frac{d \phi_{auxc}}{dt} \]  

(11)

After testing different value of \( \theta_0 \), this angle does not affect the simulation results. Therefore, we choose \( \theta_0=0 \). Thus, the auxiliary winding flux of the phase A is represented as (12) and (13).

\[ \phi_{auxa} = \phi_{sa} + \phi_{sb} + \phi_{sc} + \sum_{i=1}^{N_r} \phi_{ri} \]  

(12)

\[ \phi_{auxa} = M_{aux} I_{sa} - \frac{M_{aux}}{2} I_{sb} - \frac{M_{aux}}{2} I_{sc} + \sum_{i=1}^{N_r} M_{aux} \cos\left(\theta + \frac{j\pi}{3}\right) I_{ri}, \quad j = 0, 2, 4, \ldots \]  

(13)

4. SIMULATION RESULT AND DISCUSSIONS

In this section, the proposed method is applied to diagnose a 450W squirrel cage induction machine fed by an inverter under several faults and operation conditions. The simulation is carried out by MATLAB wavelet toolbox for performing DWT of the auxiliary winding voltage signal with seven levels corresponding to different frequency bands as shown in Table 1; whereas Daubechies-40 was selected as the mother wavelet. The performance of the proposed method for fault detection is tested in different rotor bar breakages cases and under load levels. The characteristic of the simulated motor is presented in Table 2.

The motor fed by an inverter has been tested under five cases with 2 load conditions: healthy state, the presence of a broken bar, two broken bars, five broken bars and two broken bars with one broken end ring. The supply frequency \( f \) is included in details \( d_7 \). The frequencies below \( f \) are included in the
approximation of the level 7 $a_7$. The higher-level signals associated to the frequency bands below the supply frequency, are discussed in this section. The results show the advantage of the time-frequency representation of the signal. The oscillations occur in different frequency bands at the same time as shown in Figure 2. Figure 2(a) and Figure 2(b) present the sampled auxiliary winding voltage signal ($s$ at the top) and the signals resulting from the DWT for the healthy state in the case of an unloaded machine and in the case of a motor with $Cr=3$Nm. The detail $d_6$ reproduces the analyzed auxiliary winding voltage. The signals $a_7$, $d_7$ and $d_6$ do not present any variation. The non-defected machine case is considered as a reference for this study to which the faulty cases will be compared.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>quantity</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$V$</td>
<td>Power supply voltage</td>
<td>220/380 V</td>
</tr>
<tr>
<td>$f$</td>
<td>Frequency</td>
<td>50 Hz</td>
</tr>
<tr>
<td>$p$</td>
<td>Number of poles pairs</td>
<td>1</td>
</tr>
<tr>
<td>$N_r$</td>
<td>Number of rotor bars</td>
<td>27</td>
</tr>
<tr>
<td>$N_s$</td>
<td>Number of stator slots</td>
<td>193</td>
</tr>
<tr>
<td>$R_s$</td>
<td>Resistance of stator winding</td>
<td>4.1 Ω</td>
</tr>
<tr>
<td>$R_b$</td>
<td>Resistance of a rotor bar</td>
<td>74 μΩ</td>
</tr>
<tr>
<td>$R_e$</td>
<td>Resistance of the rotor end ring</td>
<td>74 μΩ</td>
</tr>
<tr>
<td>$L_b$</td>
<td>Leakage inductance of rotor bars</td>
<td>0.33 μH</td>
</tr>
<tr>
<td>$L_e$</td>
<td>Leakage inductance of rotor end rings</td>
<td>0.33 μH</td>
</tr>
<tr>
<td>$J$</td>
<td>Moment of inertia</td>
<td>$4.5 \times 10^{-3}$ Nms$^2$</td>
</tr>
</tbody>
</table>

![Decomposition at level 7: $s = a_7 + d_7 + d_5 + d_4 + d_3 + d_2 + d_1$](image1)

(a)

![Decomposition at level 7: $s = a_7 + d_7 + d_5 + d_4 + d_3 + d_2 + d_1$](image2)

(b)

Figure 2. Wavelet analyses of auxiliary winding voltage for healthy state in case of (a) unloaded machine and (b) $Cr=3$ Nm

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For the breakage of one rotor bar presented in Figure 3, in the case of an unloaded machine, in Figure 3(a) a small variation appears at t=1.97s. The oscillation amplitude in the approximation signal $a_7$ is 4.46 V. In the details $d_7$, it corresponds to 25.33 V. When the load increases to Cr=3 Nm as shown in Figure 3(b), the oscillation amplitude increases to 25.27 V and to 151V for the approximation $a_7$ and the detail $d_7$ respectively.

Figure 3. Wavelet analyses of auxiliary winding voltage for one broken bar in case of (a) unloaded machine and (b) Cr=3 Nm

Figure 4 presents the case of two broken bars, in Figure 4(a) more oscillations appear in the approximation signal $a_7$. The first one occurs at t=1.97 s with an amplitude of 4.445 V. The other one occurs at t=2.573 s with an amplitude of 6.581 V. The details signal $d_7$ shows two oscillations at t=1.97 s corresponding to an amplitude of 25.33 V and a large oscillation at t=2.564 s with an amplitude of 74.79 V. When the load level reaches Cr=3 Nm, as shown in Figure 4(b), for the approximation signal $a_7$, the
Oscillations amplitudes increase to 23.93 V and 27.22 V at the same time as the previous case. The details signal $d_7$ reaches 152.4 V and 172.5 V respectively at $t=1.97$ s and $t=2.564$ s.

![Wavelet analyses of auxiliary winding voltage for two broken bars in case of (a) unloaded machine and (b) $Cr=3$ Nm](image)

Figure 4. Wavelet analyses of auxiliary winding voltage for two broken bars in case of (a) unloaded machine and (b) $Cr=3$ Nm

Multiple oscillations with different width shown in Figure 5 are produced by five broken bars. In the case of an unloaded machine in Figure 5(a), the oscillations appear at $a_7$ from $t=1.54$ s with an amplitude of 4.451 V until $t=3.5$ s that corresponds to the amplitude of 47.96 V. The detail $d_7$ presents the same variation and has different amplitudes and width starting from $t=1.558$ s with 21.76 V until $t=3.55$ s corresponding to an amplitude of 121.6 V. At $t=2.96$ s, an oscillation amplitude attends 136.8 V. In the case of $Cr=3$ Nm presented in Figure 5(b), a clear perturbation appears with the evolution of $a_7$ over the time. From $t=1.572$ s to $t=3.559$ s, the oscillations present an amplitude of 29.31 V and 27.8 V respectively. The maximum amplitude reaches 61.02 V at $t=2.96$ s. Moreover, $d_7$ shows the largest variation at $t=3.1$ s with an amplitude.
of 421.5 V. Other one starts from t=1.57 s to t=3.536 s. Their amplitudes are 127.7 V and 190.8 V respectively.

![Figure 5](image)

Figure 5. Wavelet analyses of auxiliary winding voltage for five broken bars in case of (a) unloaded machine and (b) Cr=3 Nm

The breakage of two adjacent bars causes the breakage of an end ring. In this case, Figure 6 shows the variation that occurs in the auxiliary winding voltage within the approximation and the details signals. For an unloaded machine in Figure 6(a), three oscillations in $a_7$ with different width and amplitude as 4.445 V, 6.581 V and 6.142 V appear at t=1.943 s, t=2.573 s and t=2.93 s respectively. The oscillations presented in the detail $d_7$ occur at t=1.955 s with an amplitude of 23.84 V until t=2.961 s that corresponds to an amplitude of 74.56 V. For Cr=3 Nm Figure 6(b), the oscillations amplitude increase. The signal $a_7$ presents three oscillations with an amplitude around 25 V. The signal $d_7$ shows larger oscillations with an amplitude that reaches 162 V at t=2.186 s.
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5. CONCLUSION
This paper has introduced a new method to diagnose rotor broken bar and end rings fault in induction motor fed by an inverter. The method is based on the application of discrete wavelet transform to the auxiliary winding voltage of an inserted coil between two phases in the machine stator side. The method is tested on MATLAB software under different faulty conditions. The simulation results show the effectiveness of this approach to provide a time-frequency localization and prove the ability of the proposed signal for the failures extraction even in the case of an unloaded condition.

REFERENCES


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