Employing opposite ratings users in a new approach to collaborative filtering

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| **Article Info** |  | **ABSTRACT** |
| ***Article history:***Received Oct 1, 2018Revised Dec 10, 2018Accepted Jan 25, 2019 |  | Over the past few decades, various recommendation system paradigms have been developed for both research and industrial purposes to satisfy the needs and preferences of users when they deal with enormous data. The collaborative filtering (CF) is one of the most popular recommendation techniques, although it is still immature and suffers from some difficulties such asparsity, gray sheep and scalability impeding recommendation quality. Therefore, we propose a new CF approach to deal with the gray sheep problem in order to improve the predictions accuracy. To realize this goal, our solution aims to infer new users from real ones existing in datasets. This transformation allows for creating users with opposite preferences to the real ones’. On the one hand, our approach permits to amplify the number of neighbors, especially in the case of users who have unusual behavior (gray sheep). On the other hand, it facilitates building a dense similar neighborhood. The basic assumption behind this is that if user X is not similar to user Y, then the imaginary user ¬X is similar to the user Y. The performance of our approach was evaluated using two datasets, MovieLens and FilmTrust. Experimental results have shown that our approach surpasses many traditional recommendation approaches. |
| ***Keywords:***Recommendation System;Gray sheep Problem;Collaborative Filtering;Opposite Neighbors;Imaginary User;Similarity Measure. |
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1. **INTRODUCTION**

Recommendation systems are smart tools that can recommend things to users based on their preferences [1], especially personalize recommendation system. The primary purpose of recommendation systems is to facilitate the task of users by providing them with items responding to their needs. The key of personalized recommendation systems is the user preferences. In fact, preferences allow recommendation systems to understand users’ needs and behavior. They are mainly based on users' history (ratings, clicks, etc.); these interactions are divided into two categories: implicit feedback data (e.g., clicks, purchases) and explicit feedback data (e.g., ratings, votes). Explicit feedback data are more widely used in the research fields of recommendation system[2][3].

With the intensifying problem of information overload, recommendation systems have become indispensable for users to find accurate information, products, or services they are seeking. These systems have the role of filtering incoming information by transmitting relevant flows to the user and blocking those that are irrelevant [4].

 In the last decades, in the last decades, online industries have intensively used the recommondations systems to claim their place in the market and improve their customer relationship management. For instance, e-commerce systems such as Amazon [5], travelling systems such as TravelJoy [6], movie-streaming platforms such as Netflix [7], and Music applications[8] [9][10] have achieved great success by making entertainment and shopping easily accessible and providing an amazing experience to users especially during the Covid-19 pandemic.

Many recommendation system approaches have been proposed and developed in order to meet the growing needs of users and to overcome the encountered problems in the recommendation process. According to [2], three main types of recommendation systems have been proposed in the literature :Collaborative Filtering (CF) [11], recommendation systems based on the content [12], and hybrid recommendation systems [13][14].

CF recognizes commonalities between users or between items on the basis of relevance indications [15]. A content-based recommendation system suggests those items that have similar features to items that the user has liked before [3]. A typical content-based recommendation first creates user profile using user feedback and ratings about items. A hybrid recommendation system combines multiple approaches together to achieve some synergy between them [16].

CF approach is the most used approach in recommendation systems due to their efficiency and simplicity [17]. In this section, we briefly review the main CF algorithms reported in the literature. These algorithms are based on a simple intuition. They assume that good recommendations can be derived from users sharing the same interests and preferences. These preferences can be expressed in several ways, either by using ratings based on users’ interests [18], or by deducing from users’ behavior, tracking their purchase history and time spent on web content, which is known as implicit return [19]. They can be expressed in the form of a matrix called rating matrix[20]. This is the basis for creating effective prediction models and user profiles [21]. There are two main approaches to CF: Memory-based and Model-based.

* Memory-based CF recommendation approaches directly exploit users’ preferences [22] ( drawing similar relationships between the users or the items based on the user-item rating matrix). The techniques revealed in the memory-based approach are considered the first algorithm of CF [23]. The recommendations are easily applied to the ratings matrix. The techniques used in the memory-based CF make it possible to obtain the similarity to calculate the distance between two users (user-based approach), or between two items (item-based approach), according to the evaluations, in the rating matrix [24].
* Model-based approaches (also called collaborative neighborhood-based filtering) construct or learn models from collected notes based on machine learning techniques such as clustering techniques [25], dimensionality reduction approaches [26], support vector machines, and neural networks [27].

CF relies on the users’ community in the system. Its main characteristic is the use of ratings obtained from users’ recommended items. The principle is to filter the flow of items as rated by the other users’ community. If an item has been deemed interesting by a user, it will be automatically recommended to users with similar views in the past.Hence, the objective of CF is to predict, for an unrated element, the evaluation that the target user might assign, based on the correlation between their own ratings and the ratings of other users who have similar interests and preferences.

Currently, CF has become the most widely-used approach[18], which motivates a significant number of researchers working on this issue. Neighborhood selection is one of the concepts used in CF. Among the research carried out on this topic, [28] proposed grouping user profiles into clusters of similar articles and composing the list of recommendations that fit in well with each cluster. [29] posited that clustering improves the performance of the recommendation. However, [30] suggests a new neighborhood-based probabilistic approach as an improvement to the nearest k nearest standard algorithm.

In the next section, we review the memory-based techniques using user-based approach (UBCF).

The top-K users who have similar preferences to a given user are called K nearest neighbors (KNN). We use similarity measures to draw similarities or correlations among users to identify the KNN. In KNN, the value of K is the number of similar neighbors we need to predict ratings [22].

 Despite its advantages, CF has a number of drawbacks affecting the accuracy of recommendations. Among these drawbacks is the gray sheep users, designating users who have unusual preferences and who do not share the same preferences with other users[15]. This problem makes the task of finding neighbors difficult.

This work aims to mitigate the gray sheep problem and to enhance the accuracy of recommendations based on the opposite preferences of users. The basic idea governing this lies in generating imaginary users based on dissimilar ones in order to enhance the user neighborhood. The underlying assumption of our approach is that if user X has an opposite preference to user Y, then the imaginary user ¬X has a similar preference to the user Y. Our approach increases the number of comparable neighbors, amplifies the density of the neighborhood, and then allows for building good recommendations.

The remainder of this paper is organized as follows: in Section 2, we provide an overview of the basic approaches to CF. In Section 3, we tackle the related work with a focus on the gray sheep users problem. In Section 4, we discuss our proposed approach and the novelty of this work. The experiments and results are presented in Section 5, followed by the conclusion and future work in Section 6.

1. **BACKGROUND**

## Collaborative Filtering Recommendation Process

The memory-based approach is based on three steps presented in Figure 1 below [31]:

Figure : Collaborative filtering recommendation process

The first step before entering the Collaborative Filtering Recommendation Process consists in collecting users’ data in need for recommendations. These data (rated films in this case) serve as a request for the algorithm.



Figure : An example of data collection

* + 1. Data representation:

The second step of CF consists in constructing the evaluation matrix and filling in the empty values. In fact, in most cases, the scoring matrix is usually filled in because users do not score items regularly [26]. The most used technique in the CF is replacing the empty squares of the matrix with the average user ratings.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| User-Item Rating

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  | I1 | I2 | I3 | I4 |
| U1 | 5 |  | 3 |  |
| U2 |  | 4 | 2 | 5 |
| U3 |  | 5 | 2 |  |

 |

Figure 3: A small-scale example of data representation

* + 1. Neighborhood formation:

In this step, we look for the neighborhood of the most similar users using a similarity metric. There are different measures for obtaining the similarity. However, the most extended ones are the Pearson correlation coefficient and cosine similarity [23].

This work employs two formulas: the Pearson correlation coefficient and the cosine. For the Pearson correlation coefficient, its values are between -1 and +1. It is considered a standard way to measure correlation [29]. However, the values obtained for the cosine similarity vary from 0 to 1 (0 means there is no correlation between the two users and 1 means that they are identical).

 Thus, we use two formulas to calculate the similarity between two users, a and b:

Pearson correlation formula:

$$sim\_{a,b}=\frac{\sum\_{j=1}^{n}\left(r\_{aj}-\overbar{r\_{a}}\right)\left(r\_{bj}-\overbar{r\_{b}}\right)}{\sqrt{\sum\_{j=1}^{n}\left(r\_{aj}-\overbar{r\_{a}}\right)^{2}\sum\_{j=1}^{n}\left(r\_{bj}-\overbar{r\_{b}}\right)^{2}}} (1)$$

Cosine similarity formula:

$$sim\_{a,b}=\cos(\left(a,b\right))=\frac{a b}{\left‖a\right‖\left‖b\right‖}=\frac{\sum\_{j=1}^{n}r\_{aj}\*r\_{bj}}{\sqrt{\sum\_{j=1}^{n}r\_{aj}^{2}}\*\sqrt{\sum\_{j=1}^{n}r\_{bj}^{2}}} (2)$$

* + 1. Predictions generation:

In this step, after selecting the nearest k-neighbors for the active user using the similarity degree based on the ratings matrix, the CF process generates predictions for unseen items. The prediction can be generated using the following formula:

$p\_{s,i}=\overbar{r}\_{s}+\frac{\sum\_{p=1}^{k}(r\_{p,i}-\overbar{r\_{p}})\*sim\_{s,p}}{\sum\_{p=1}^{k}\left|sim\_{s,p}\right|}$ (3)

In this formula, we calculate the predictions of rating for all the items that have not yet been seen by user s. We use the KNN technique where K represents the number of closest neighbors and $\overbar{r}\_{s}$ represents the user's average rating s.

User-Item Rating

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
|  | I1 | I2 | I3 | I4 |
|  U1 | 5 | 3 | 3 | 4 |
| U2 | 3 | 4 | 2 | 5 |
| U3 | 4 | 5 | 2 | 5 |

Figure 4: A small-scale example of predictions’ generation

## Evaluation metrics

After generating the predictions, we move to the stage of evaluating the performances of these predictions. In the literature, the performance of recommendation systems is measured with two commonly-used evaluation measures: MAE (mean absolute error) and RMSE (mean squared error). MAE calculates the mean absolute differences between the predicted values and the actual values as presented in the following formula:

$MAE=\frac{\sum\_{(s,i)}^{}\left|p\_{s,i}-r\_{s,i}\right|}{N}$ (4)

As N represents the number of the predicted rating calculated during the test phase, ***rs,i*** is the actual rating given by the user s to the item i, and ***ps,i***is the rating predicted by the user s for the item i.

RMSE (Root Mean Square Error) is a standard way to measure the error of a model in predicting quantitative data. Formally, it is defined as follows:

$RMSE= \sqrt{\frac{\sum\_{(s,i)}^{}\left(p\_{s,i}-r\_{s,i}\right)2}{N}}$ (5)

In this section, we have cited the steps of the CF user-based approach. We can see that it is fairly easy to implement and give good recommendations, but regardless of these advantages, there are many disadvantages to this approach that influence the results, such as the small quantity, the scalability, and the gray sheep problem. In the latter, it is difficult to find similar neighbors for a user’s preference, which undermines the results obtained.

1. **RELATED WORK**

In this section, we discuss the problem of gray sheep users and deal with how this problem is overlooked in research on recommendation systems.

The work in [32] confirms that the efficiency of traditional CF algorithm varies from one user to another. There are two main categories for users: White Sheep (WS) and Gray Sheep (GS). WS users have high similarity to many other users (the correlation value is high), whereas the GS users are dissimilar or partly similar to other users and have a lower correlation coefficient with almost all users [31]. Therefore, the user recommendations become less accurate due to GS users [33]; hence, they do not benefit from recommendation systems. There are some works that deal with the problem of gray sheep users[34][35] [36]. [32]highlighted the problem of GS and onlined a hybrid recommendation system for updated recommendations. They combined CF and content-based filtering approaches, using an average-weighted approach. However, they did not specifically target GS users nor did they offer a formal solution for this problem. [37] Used the MovieLens dataset to test this approach for a CF domain using. As this is a simulation, they did not describe a method for identifying these users and meeting their needs. GS users can be recognized using clustering algorithms offline, where the similarity threshold for separating these users from the rest of the clusters can be found empirically [36].

To identify GS users in the system, many approaches are suggested, including re-using outlier detection techniques based on user-user similarity distribution [38]. This is a distribution-based identification technique for GS users which borrows from the detection of outliers and the search for information, while taking into account the specifics of the preference data on which CF relies [22], i.e., clustering-based approaches [39][36] or social network approaches [40]. In all, these approaches identify GS users with accuracy and eliminate GS users while making recommendations for the rest of the users with a high degree of accuracy. Hence, they do not take into account GS users. In order to solve this problem, this work deploys all users and benefits from GS users.

1. **PROPOSED METHOD**

As stated earlier, the basic CF approach uses the K-nearest neighbors to make new predictions. It only relies on users who have similar preferences to the active user, regardless of users with low similarity or dissimilarity in the prediction phase. In GS cases, the similarity between the active user and other users is still low or nonexistent, as most of them are distant. Figure 2 shows concretely the case of GS in the CF process.

The three possible cases are delineated thus:



*Figure 5: Example of GS cases in Neighborhood-based techniques*

The figure above shows an example of hypothetical neighbors that can be generated after inverting preferences. We have represented the new imaginary neighbors by red dots, formed via the step of increasing the matrix. The new neighbors can be positively correlated with the target user.

The core of our approach is to benefit users (GS users) whose preferences are different from the target user. The underlying assumption of our approach is that users must have more or less the same interests. If user X’s interests are opposite to user Y, then the imaginary user ¬X would have the same interests as the user Y. Therefore, additional information will be provided to the recommendation engine to make good recommendations.

The new process of our approach includes an additional step that increases the neighborhood number of the active user; which is called ratings matrix augmentation (Figure 6).

*Figure 6: New Memory-Based CF Process*

The augmentation step of the ratings matrix consists of adding rows in the ratings matrix that represent opposed users to real users. The imaginary user is obtained by deducing the opposite preference from each item evaluated using the following formula:

$¬r\_{uj}=Max-r\_{uj} +Min$ (6)

***ruj***: the rating of user u for an item j.

***Max*** and ***Min***: the high and low values respectively in a given numerical scale.

Example:

By providing a sample of rating that ranges from 1 to 5 in the figure below- if a user u rates an item as ***ruj***= 5- the estimated rating of the user ¬u will be ***¬ruj***= 1.

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
| ItemsUsers | I1 | I2 | I3 | I4 | I5 | I6 | I7 |
| $$U$$ | **4** |  | **2** |  | **5** |  | **3** |

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
| ItemsUsers | I1 | I2 | I3 | I4 | I5 | I6 | I7 |
| $$U$$ | **4** |  | **2** |  | **5** |  | **3** |
| $$¬U$$ | **2** |  | **4** |  | **1** |  | **3** |

*Figure 7: Example of an opposite rating matrix on a 5-point scale*

Figure 5 illustrates a sample-case of imaginary neighbors that can be generated after inverting preferences. We represented the new imaginary neighbors by red dots, formed via the step of increasing the matrix. The new neighbors thus can be positively correlated with the target user.Figure 7 shows an example of an opposite user on a 5-point scale using the formula 6 above. ¬U represents the opposite user of the user U after the application of the formula. It relies on the inference of an opposing user's ratings by providing the opposite preference of a given user.

Finally, we list the pseudonyms of our proposed method in Algorithm Matrix Augmentation.

**Algorithm : Matrix Augmentation**

**Input : Matrix T[nbrusers][nbritems] ;**

**Output: MatrixAugmentation TA [2 x nbrusers][nbritems];**

**Initialize Max=5, Min=1 ;**

**cpt1 =1**

**cpt2 =1**

**while cpt 1 <= nbrusers do // for all users in the dataset**

 **while cpt2 <= nbritems do // for all his/her rated items**

 **if T[cpt1][ cpt2]>0**

**TA[nbrusers+cpt1] [cpt2]= Max – T[cpt1][ cpt2] +Min**

**cpt2++**

 **cpt1++**

**return TA**

Figure 8:Algorithm Matrix Augmentation

1. **RESULTS AND DISCUSSION**

In this section, many experiments are performed to demonstrate the novelty and efficiency of our approach.Therefore , we divided our dataset into 80% for the training set and 20% for the test set. We calculated the means of the results of a cross-validation of 10 times. We also implemented a system of film recommendation under R thanks to Recommenderlab[41] with the MovieLens and FilmTrust datasets. The objective is to check the performance of our proposed approach (AUBCF) with the traditional user-based CF approach (UBCF) using real-world datasets. A brief description of the datasets used will be in order, ensued by the evaluation procedure, and the specification test environment. Hence, the results were acquired from comparisons to come up the most successful approach.

## Datasets collection:

We executed our experiments with two commonly-used datasets: FilmTrust and MovieLens. Both are academic research projects of web-based movie recommendation systems.

MovieLens is a set of evaluation data on a scale of 5 points ranging from 1 (bad) to 5 (excellent). It includes 1682 films, 943 users, and 100,000 rankings.

The FilmTrust dataset includes 1856 users, 2092 movies, and 759922 reviews. It was collected from a social network based on a video recommendation system including reviews. The odds are 5-point scales ranging between 0.5 and 4 stars.

## Experiments

All the experiments and techniques were performed on Intel i5 at 2.4GHz and 8 GB RAM, using MovieLens and FilmTrust datasets.

## Pearson correlation:

The figure below (Figure. 8) shows the results obtained by comparing our proposed approach named AUBCF (UBCF augmented) and the user-based CF approach (UBCF) as a basic approach for the FilmTrust dataset.

|  |  |
| --- | --- |
| **Experiment 1: FilmTrust**E:\doc doctorat\RESU\new conf merr\FT graph.pngFigure 8: MAE comparison using FilmTrust dataset | **Experiment 2: MovieLens**E:\doc doctorat\RESU\new conf merr\AUBCF.pngFigure 9: MAE comparison using MovieLens dataset |

Figure 8 represents a comparison of MAE where the horizontal axis is the size of the neighborhood used for the calculation of MAE. The figure shows that our approach (AUBCF) decreases regularly for the MAE, while the traditional approach (UBCF) decreases to N = 40 and then remains stable until N = 60 where the MAE begins to increase.

In Figure 9, we can see that the MAE of our approach (AUBCF), in green, and the traditional approach (UBCF), in red, are inversely proportional to the number of users in the neighborhood. The traditional approach (UBCF) has a higher MAE than our approach (AUBCF).

## Cosine:

Figures 10 and 11 demonstrate the results obtained by comparing the traditional approach (UBCF), in red, and the proposed approach (AUBCF), in green, for each dataset. The diagram represents a comparison of MAE where the horizontal axis is the size of the neighborhood in each experiment. It increases from 10 to 100 at the interval of 10.

|  |  |
| --- | --- |
| **Experiment 1 : FilmTrust**E:\doc doctorat\RESU\new conf merr\MAE comparison using FilmTrust dataset.pngFigure 10: MAE comparison using FilmTrust dataset | **Experiment 2 : MovieLens**E:\doc doctorat\RESU\new conf merr\MAE comparison using MovieLens dataset.pngFigure 11: MAE comparison using MovieLens dataset |

The proposed approach (AUBCF) in Figure 10 remains regular for the MAE while the traditional approach (UBCF) increases to N = 30; then it remains stable until N = 60 where the MAE begins to decrease. In Figure 11, the MAE of proposed approach (AUBCF) and the traditional approach (UBCF) are inversely proportional to the size of the neighborhood. They decrease steadily up to N=60, then they remain stable up to N = 100. Thus, our approach (AUBCF) has a lower MAE than the traditional approach (UBCF).

All in all, we conclude from these experiments that the proposed approach (AUBCF) offers better performance than the traditional approach (UBCF) in both datasets.

## Statistical inference

In most experiments, it is important to make sure that the observed difference between the proposed method and baseline one is statistically significant; and it is unlikely to be due to chance or noise in the data. the appropriate statistical test to use is the Wilcoxon test.The Wilcoxon test is a nonparametric statistical test that compares two data samples without assuming the data to have a specific distribution, the goal of the test is to decide whether the population distributions are identical or not. Our null hypothesis is that the results of algorithm AUBCF and the results of algorithm UBCF are identical populations, that any small gain, or loss, observed is not statistically significant.

Generally, we reject the null hypothesis if the p-value is less than a certain threshold (often 0.05). In other words, if p-value< 0.05 we can infer that the difference is statistically significant.

|  |  |  |
| --- | --- | --- |
|  | **Pearson correlation** | **Cosine** |
| FilmTrust | 6.900406e-25 | 0.01639486 |
| MovieLens | 4.473234e-05 | 0.0002432247 |

Table : Comparison of p-value between Pearson correlation and cosine by Wilcoxon test for both datasets

According to the table all p-values are below the threshold (0.05), we rejected the null hypothesis and we can say that the difference is statistically significant.

Finally, the obtained results of algorithm AUBCF are better than the results of algorithm UBCF.

1. **CONCLUSION & FUTURE WORKS**

Despite the poularity and the great usage of CF, it is not without limitations as it still has to overcome the GS problem. Therefore, this work proposed a new CF approach to solve this problem. This approach aims to increase the number of neighbors for the active user based on users with different interests and preferences. To evaluate our algorithm, we compared it to UBCF as a traditional approach. The comparison was done on two datasets, FilmTrust and MovieLens. The obtained results show that our approach outperforms UBCF and improves prediction accuracy for GS problems.

The contribution of our work can be summarized in a three main points. First, our approach makes full use of the rating data to improve the accuracy of recommendation systems. All the rating data from users are used in the model, not just the WS users rating data. Second, the problem of GS users is solved in our model which makes it possible to obtain an accurate similarity when there is no correlation between two users. Third, this paper proposes a new approach for collaborative filtering which shows superiorperformance than the traditional collaborative filtering.

In future work, we will consider the idea of hybridizing our approach with various machine learning techniques in order to improve the accuracy of the recommendations.

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