Modelling and Simulation of Field Oriented Control based Permanent Magnet Synchronous Motor Drive System

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Abstract

On the basis of analysis of dq model of permanent magnet synchronous motor (PMSM) and principle of field oriented control (FOC), detail modelling of PMSM drive system and simulation results presented in this paper. The PMSM model is based on electronic components rather than mathematical blocks, this enabled us to achieve simulation results more realistic. Moreover all the modules of this simulation, such as inverter and pwm generator are made from scratch instead of using premade Simulink blocks. Simulation was carried on the basis of step change in speed and torque then made performance comparison of several parameters such as abc current, dq current, speed and torque.

Keywords: FOC, PMSM simulation, dq model, synchronous motor, vector control

1. Introduction

With the advancement of permanent magnetic materials, power electronics and computing technology, AC motors, specially PM synchronous motor were adopted by many industries because of its inherent qualities such as high torque to inertia ratio, good efficiency, low cost, high power density, easy maintenance [1, 2] and advance vector control which allows decoupled control of torque and speed of AC motor similarly to DC motor made synchronous motor more popular [3]. This paper analyses the dq equivalent circuit of PMSM [4], which is appropriate for implementing FOC, then modelling of PMSM based on the equivalent circuit and implementing FOC [5]. Realistic electronic components used for modelling PMSM for accuracy.

Using powerful simulation capabilities of MATLAB/ Simulink, the entire drive system is modelled using modular approach. Whole simulation model is built around several independent functional modules such as dq model of PMSM, inverter, PWM generator, PI controller, Park and inverse Park transformation blocks. Final drive system is made through linking these separate modules in their appropriate orders [6]. By providing parameters of any specific motor, we get estimated performance characteristics graphs for that particular machine such as torque and speed.

2. Research Method

Field oriented control was introduced during 70s. It is a control mechanism to flexibly drive synchronous and induction motor. It allows decoupling control of torque and speed of AC motors similar to separately excited DC motors.

Since in DC motor, armature current which directly control the torque and field current in the rotor which produce magnetizing flux are independently accessible and armature mmf and rotor flux held orthogonally with respect to each other through mechanical commutation system such as brushes and commutators. But in case of AC motors (Synchronous and Induction motor), spatial angle between rotating stator field and rotor flux changes with the load which causes oscillatory response. FOC emulate the DC conditions in AC motor structure by monitoring the rotor field position and orient the stator field accordingly so that angle between

both of the fields can be maintain at 90o. In this way maximum torque condition can be achieved while independently controlling rotor speed [7–10].

FOC require a position sensor for constantly monitoring the rotor position, hence rotor flux position too. Stator field is oriented through varying phase and magnitude of three phase ac quantities. Hence it is also referred as 'vector control' [9-11]

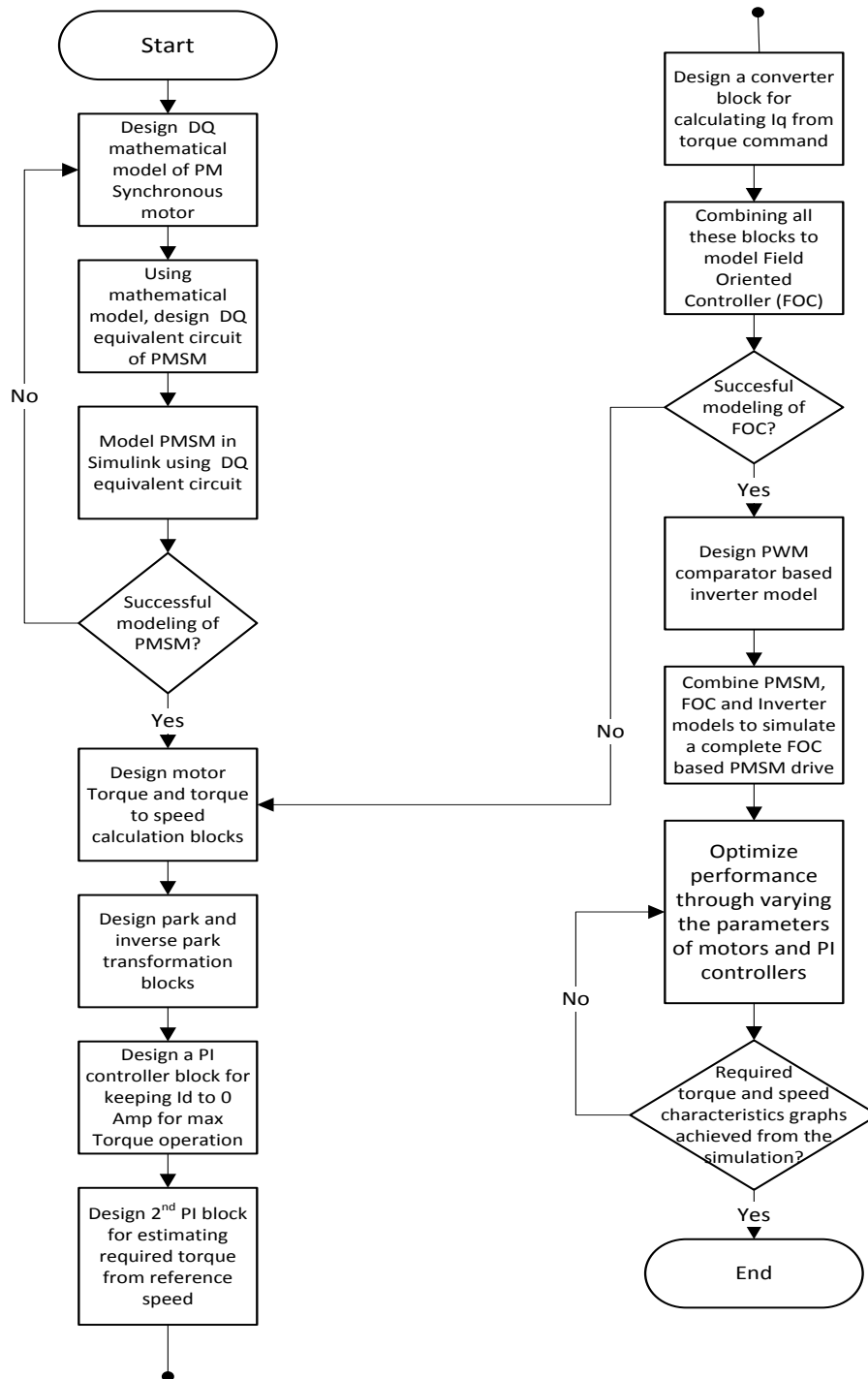The flow chart describing the methodology of implementing FOC for PMSM is shown in Figure 1.

Figure 1. Flow chart of implementing FOC for PMSM

2.1. Mathematical Model of PMSM

Mathematical model of PMSM describe in this paper is based on following assumptions
1. Core saturation and winding leakage inductance are ignored
2. Sine distribution of magnetic potential in the air gap
3. Higher harmonic waves in the magnetic field are negligible

Within these assumptions and using dq coordinate transformation, the mathematical model of PMSM in dq rotating coordinate system is represented in terms of following equations [12, 13].

DQ transformed voltages are given by:

$$V_q = R_s i_q + \omega r \lambda d + \rho \lambda_q \tag{1}$$

$$V_d = R_s i_d - \omega_r \lambda_q + \rho \lambda_d \tag{2}$$

Flux Linkages are given by:

$$\lambda_{q =} L_q I_q \tag{3}$$

$$\lambda_{d =} L_d I_{d +} \lambda_f \tag{4}$$

Substituting Equations 3 and 4 into 1 and 2.

$$V_q = R_s i_q + \omega_r (L_d i_d + \lambda_f) + \rho L_q i_q \tag{5}$$

$$V_d = R_s i_d - \omega_r L_q i_q + \rho (L_d i_d + \lambda_f) \tag{6}$$

Arranging Equations 5 and 6 in matrix form:

$$\begin{bmatrix} V_q \\ V_d \end{bmatrix} = \begin{bmatrix} R_s + \rho L_q & \omega_r L_d \\ -\omega_r L_q & R_s + \rho L_d \end{bmatrix} \begin{bmatrix} I_q \\ I_d \end{bmatrix} + \begin{bmatrix} \omega_r \lambda_f \\ \rho \lambda_f \end{bmatrix} \tag{7}$$

The developed torque motor is being given by:

$$T_e = \frac{3}{2} \left(\frac{P}{2} \right) \left(\lambda_d i_q - \lambda_q i_d \right) \tag{8}$$

The mechanical Torque equation is:

$$T_e = T_L + B\omega_m + J \frac{d\omega_m}{dt} \tag{9}$$

Solving for the rotor mechanical speed form Equation 3.9

$$\omega_m = \int \left(\frac{T_e - T_l - B\omega_m}{J} \right) dt \tag{10}$$

and

$$\omega_m = \omega_r \left(\frac{2}{P} \right) \tag{11}$$

Where ωr is the rotor electrical speed where asωm is the rotor mechanical speed.

2.2. Equivalent Circuit of PMSM

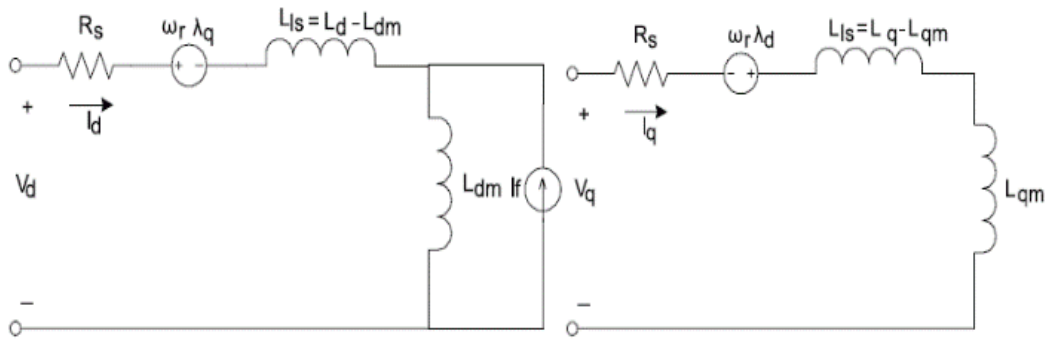Following equivalent circuit of PMSM is based on Equation 5 and 6.

Figure 2. DQ equivalent circuit of PMSM

2.3. Simulation of FOC Drive System of PMSM

Simulation of FOC drive system of PMSM is based on the mathematical model and the motor equations. It is built on several blocks such as DQ model of PMSM, Park and Inverse Park transformation block, torque and speed block, PI control, PWM generator and inverter [14, 15].

PMSM block consist of d and q axis circuits as shown in Figure 3 and 4. These blocks are made using equivalent circuit of Figure 2.
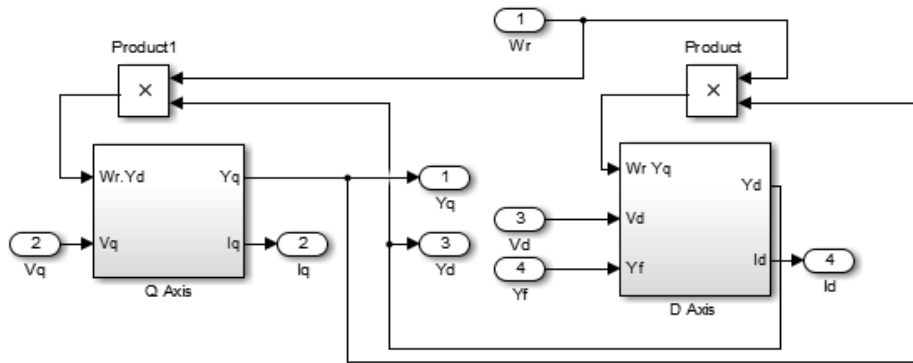

Figure 3. PMSM model (Top level)
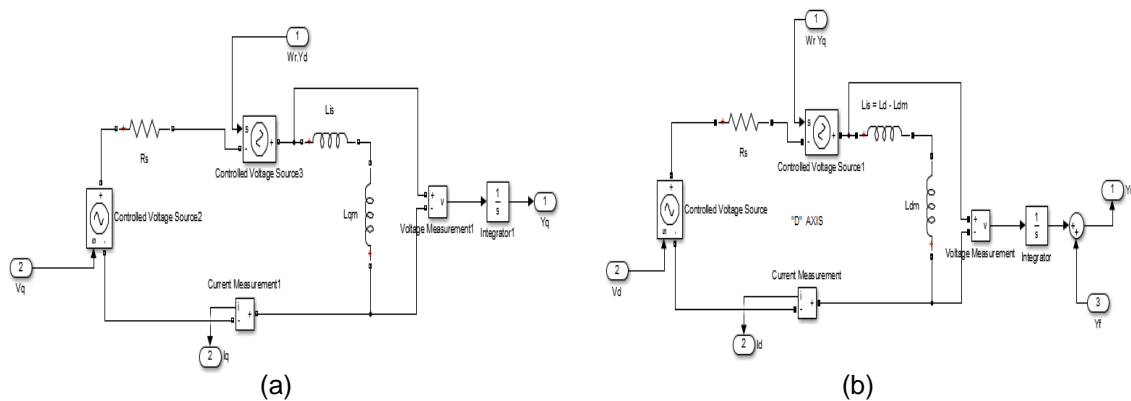

(a)   (b)

Figure 4. (a) q-axis circuit (b) d-axis circuit

Torque calculation block are based on equation 8 as shown in Figure 5(a) and speed calculation is based on Equation 10 and 11. It is shown in Figure 5(b).

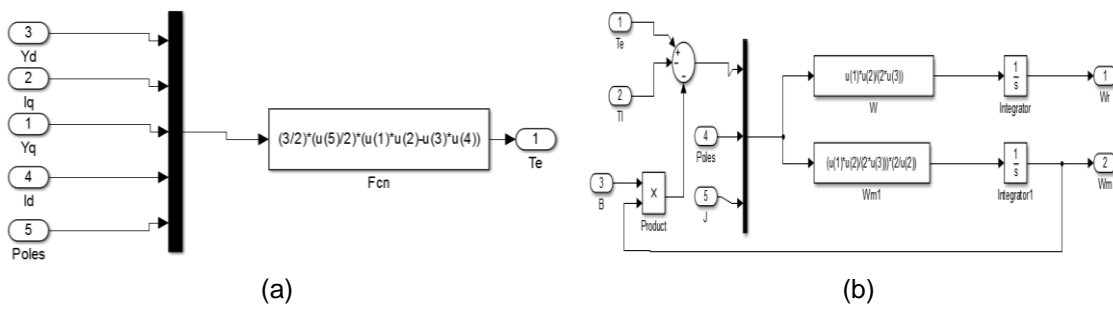(a)   (b)

Figure 5. (a) Torque calculation block (b) Speed calculation block

Park and inverse park transformation blocks are used for conversion of parameters in different phase domains. They are also referred as abc-dq and dq-abc transformation as illustrated in Figure 6(a) and 6(b).
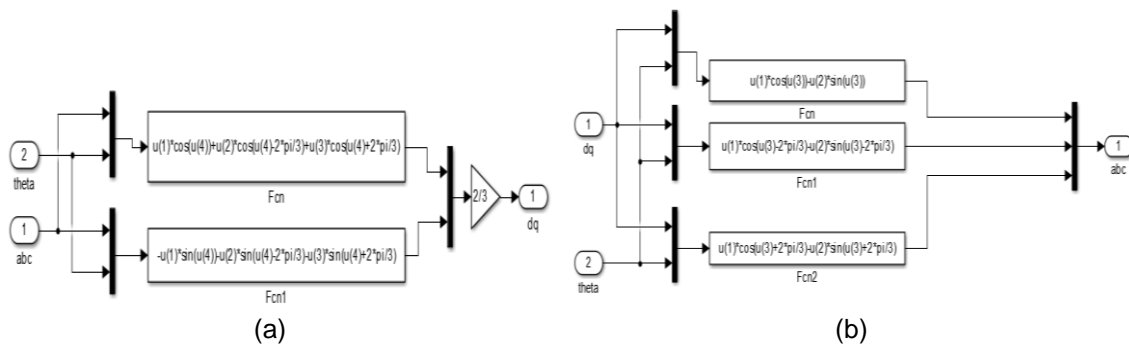

(a)   (b)

Figure 6. (a) abc-dq conversionblock (b) dq-abc conversion block

PWM generation block as shown in Figure 7(a), is used to compare calculated phase current Iabc (ref) with the current reading from motor Iabc and generate pwm signals, which is fed to the inverter. Inverter model is shown in Figure 7(b). For each phase, one switch is used to set negative and positive DC level. PWM signals from PWM generation block controls the inverter's phase voltage.
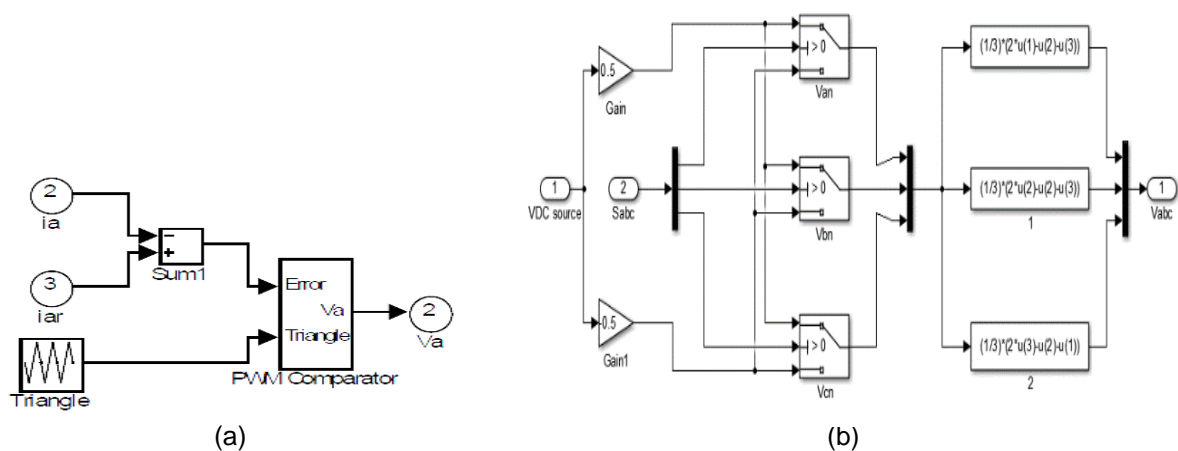

(a)   (b)

Figure 7. (a) PWM generation block (b) Inverter block

Using all the modules, the complete FOC drive system for PMSM has been developed as shown in Figure 8.

Figure 8. Complete FOC model of PMSM

3. Results and Analysis

After completion of modelling FOC drive system, it has been simulated and tested in two different control modes, variable speed and torque, through step change in the commanded parameters. These results were obtained by using the motor parameters as listed in Table 1. These parameters were taken from [11].

Table 1. Pmsm Parameters Used For Simulation

Parameters	Symbol	Value
rated voltage	V_{LL}	220 V
output power	P_{OUT}	900 W
rated stator current	I_s	16.7 A
pole pairs	P	4
rated speed	ω_m	1700 rpm
stator resistance	Rs	4.3 Ω
PM flux linkage	λ_{af}	0.272 Wb-turns
q-axis inductance	Ld	27 mH
d-axis inductance	Lq	67 Mh
Motor Inertia	J	0.000179 kg m^2

3.1. Variable Speed Mode

In variable speed mode, two different speed commands are given through a step block. Initially speed was set to 200 rpm for 30 msec, then it was increased to 500 rpm. But load torque is kept at a constant value of 3 Nm throughout the simulation.

Following are the graphs obtained from the variable speed mode.

3.1.1. Iabc Current Response

Figure 9 illustrate Iabc current response in variable speed mode, it was obtained from reverse park transformation. Initially waveforms are distorting but during steady state of initial

commanded speed of 200 rpm, the response is close to sinusoidal waveforms. After 30 msec, when commanded speed increases to 500 rpm, distortion occurs again due to the non gradual increase in the input command. But steady state achieved after 10 msec. It is also observed that waveform frequency increases during 500 rpm. Although amplitude is having same for both speed.

3.1.2. Idq Current Response

The dq component of current is shown in Figure 10, its d component is almost remain at zero as commanded throughout the graph. But some distortion can be seen in the non stable regions due to sudden changes in speed.
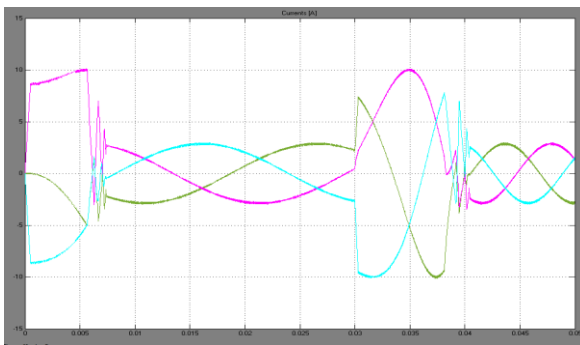
Figure 9. abc current in variable speed mode
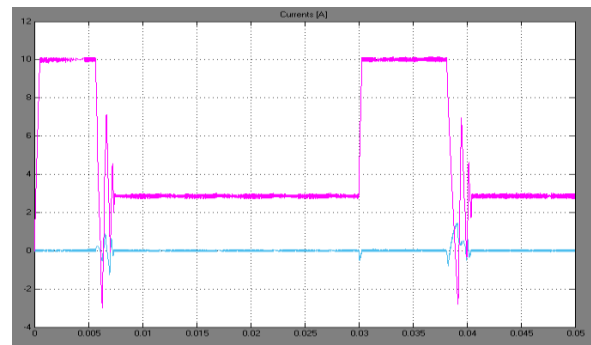
Figure 10. Idq current in variable speed mode

3.1.3. Speed Response

Figure 11 shows the electrical versus mechanical speed response graph. The difference between these two terms is due to number of poles as explained in Equation 11. It is also observe that a time is required for the motor to gradually reach at the desired speed. According to the graph, it is about 10 msec. In both of the steady states, the response is almost linear and very close to the commanded values.

3.1.4. Generated Torque Response

Figure 12 shows that in spite of constant torque operation, there can be seen large spikes of torque during non-steady state modes, during these periods speed is gradually increased and high torque needed until stability gained. Apart from these large spikes, torque is kept constant at input load value of 3 Nm in steady states.
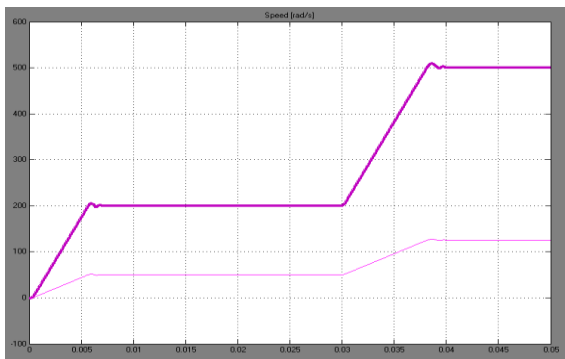

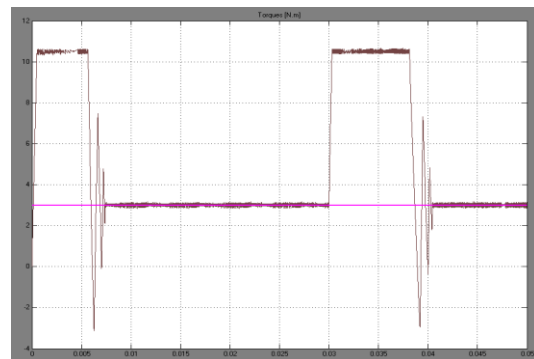Figure 11. Electrical verses mechanical speed in variable speed mode

Figure 12. Developed torque in variable speed mode

3.2. Variable Torque Mode

In variable torque mode, two different load values are input through step block. Initial load value is set to 1 Nm and final value is set to 3 Nm. While speed is kept constant throughout this simulation mode

Following are the graphs obtained from the variable torque mode.

3.2.1. Iabc Current Response

Figure 13 illustrate Iabc current response in variable torque mode. Waveform is non sinusoidal in the beginning. After gaining stability, sinusoidal waveform achieved It has also been observed that waveform amplitude is decreased during less load value. Variation of amplitude indicates that for more torque more current is needed. Frequency is constant for both of the load values. It is due to constant speed operation.

3.2.2. Idq Current Response

Figure 14 illustrates dq current response during variable torque mode. Likewise in variable speed mode, its d component is almost zero. Few distortions in both d and q components can be seen before steady state. While sudden change in load does not impact dq components severely as we have seen during variable speed mode.
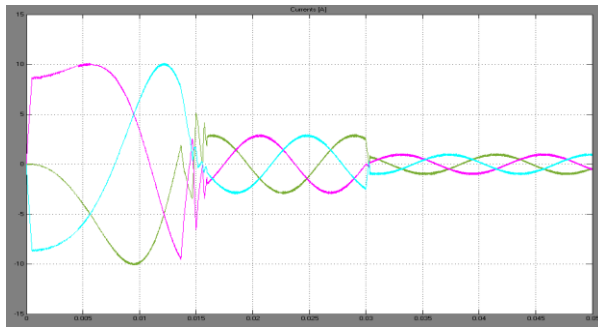

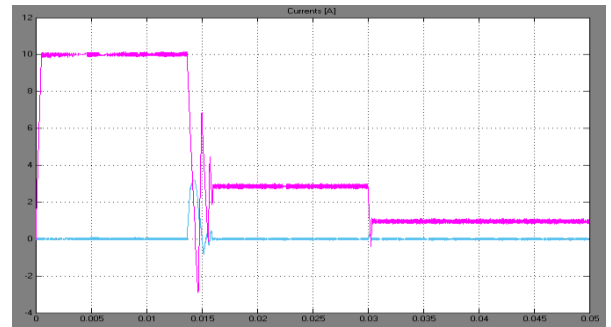Figure 13. abc current in variable torque mode

Figure 14. Idq current in variable torque mode

3.2.3. Speed Response

Figure 15 shows the electrical versus mechanical speed response graph. After gradually increases the speed upto commanded value, response is quite linear and sudden change in load does not impact the speed response.

3.2.4. Generated Torque Response

Figure 16 shows that the torque response in variable torque mode is quite good as compare to that of variable speed mode. Although few distortion can be seen before steady state.
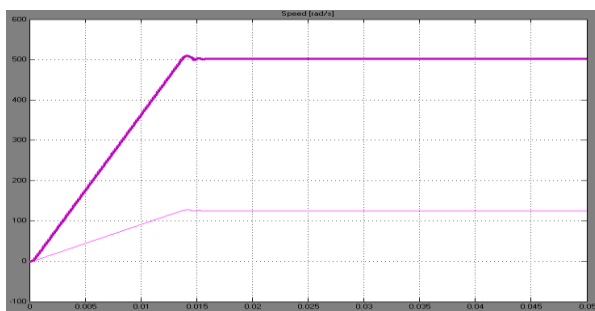

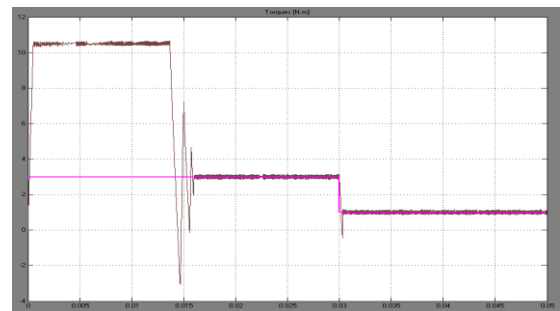Figure 15. Electrical verses mechanical speed in variable torque mode

Figure 16. Developed torque in variable torque mode

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4. Conclusion

Achieved results shows that the simulation model has good dynamic response in terms of torque and speed. Although by comparing the results from both simulation modes, it has been observed that simulation perform better in variable load mode because if we observe the graphs of torque and current in variable speed mode, large overshoots can be seen in non-steady state, whenever there is sudden change in commanded speed. Since we use step command for varying torque and speed both. But non gradual increase in torque does not affect the system stability that much. For instance, speed does not affect at all by sudden load variation as shown in Figure 15. Even current values are not overshooting, although slight oscillation in dq current graph can be seen before steady state region as shown in Figure 14.

But overall system performance is quite stable and able to meet certain requirements. In most applications, speed kept constant while load may vary with the passage of time and simulation results shows this system is quite insensitive to load torque, no overshoots has been observed while varying the load and speed remain perfectly constant as commanded.

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