

## Downscaling Modeling Using Support Vector Regression for Rainfall Prediction

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### Abstract

Statistical downscaling is an effort to link global scale to local scale variable. It uses GCM model which usually used as a prime instrument in learning system of various climate. The purpose of this study is as a SD model by using SVR in order to predict the rainfall in dry season; a case study at Indramayu. Through the model of SD, SVR is created with linear kernel and RBF kernel. The results showed that the GCM models can be used to predict rainfall in the dry season. The best SVR model is obtained at Cikedung rain station in a linear kernel function with correlation 0.744 and RMSE 23.937, while the minimum prediction result is gained at Cidempet rain station with correlation 0.401 and RMSE 36.964. This accuracy is still not high, the selection of parameter values for each kernel function need to be done with other optimization techniques.

**Keywords:** statistical downscaling, general sirkulasi models, support vector regression, rainfall in dry season

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### 1. Introduction

In some recent years ago, many efforts have already done to explore the effect of climate variety whether in a big scale or climate change toward the variability of rainfall in the worldwide [1]. The climate variety especially rainfall in Indonesia mostly influenced by global phenomenon such as El-Nino and Southern Oscillation (ENSO), ENSO is conventionally identified as ocean temperature warming in eastern Pacific [2]. Indian Ocean Dipole (IOD), IOD as a modus of tropical physic in Indian Ocean is strongly believed as a main effect which causes dryness in Indonesia [3]. Madden Julian Oscillation (MJO), MJO as a global phenomenon influences the climate in western of Indonesia [4]. This phenomenon also happens in Indramayu. It is one of Indonesia district which has monsoon rain and as a central production of agriculture particularly rice [5]. The main factors cause crop failures in Indramayu are dryness (79.8%), pest attack (15.6%) and float (5.6%) [6].

One of instruments which can be used to observe the indication of climate variability is General Circulation Mode [7]. It can be known that GCM has an intense relationship between big scale climate and whether on local scale for rainfall prediction [8], [9]. Simulated rainfall pattern from the various models of GCM is able to give basic information that needed to the future development [10]. However, GCM data is considered to the low of resolution and global scale which difficult to be used in doing prediction because local climate needs high resolution, but GCM is still can be used if it mixed to the downscaling technique.

Many models that already used to predict climate in GCM and SD such as Buono *et al* (2010) [11] statistical downscaling modeling using Artificial Neural Networks (ANN) for prediction monthly rainfall in Indramayu. In addition, Wigena (2006) [12] statistical downscaling model with Regression Projection Pursuit (PPR) to forecast the rainfall (monthly rainfall case in Indramayu). This study uses Support Vector Regression on downscaling model to predict the rainfall in dry season.

Statistical downscaling is defined as transfer function that describes functional relationship of global atmospheric circulation with local climate elements [13]. Figure 1 is process illustration of downscaling statistical.

$$Y_{t,p} = f(X_{t,q,s,g}) \quad (1)$$

Where,

Y = local climate variable	q = many of X variable
X = GCM output variable	s = many of atmosphere layer
t = time period	g = GCM domain
p = many of Y variable	

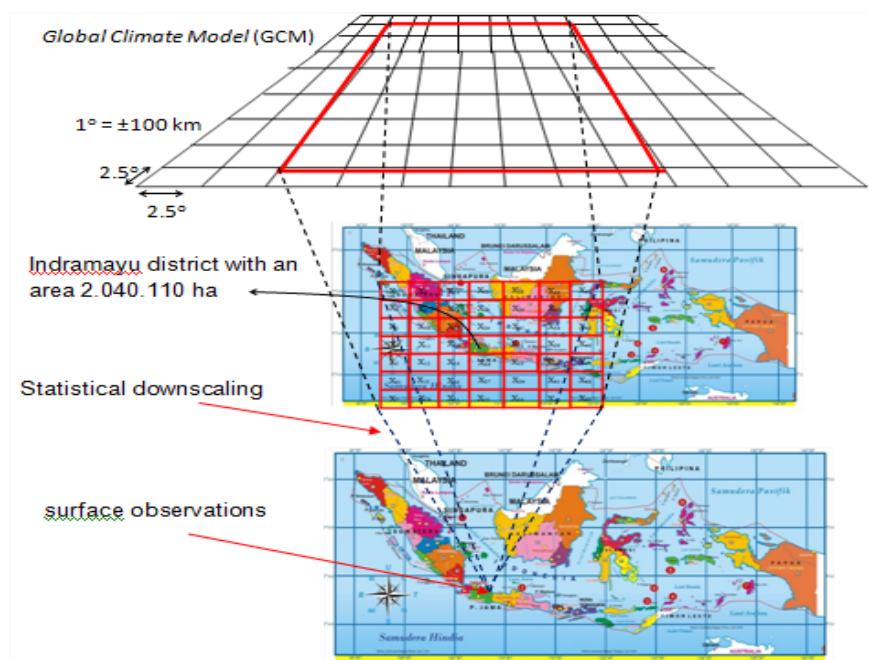


Figure 1. Statistical Downscaling Illustration

## 1.2. Support Vector Regression

Support Vector Regression (SVR) is the expansion of Support Vector Machine (SVM). SVM used to solve clarification problem, while SVR used to regression case. SVR is a method that can overcome overfitting, so that it will result better performance [14].

Suppose we have a set of data as much as  $l$  set training data in a formula:  $\{x = x_i, y_i$  with  $i=1, \dots, l$ , by  $x$  input data  $= \{x_1, x_2, x_3, \dots, x_n\} \subseteq \mathfrak{RN}$  and the corresponding output as  $\{y = [y_1, \dots, y_l] \subseteq \mathfrak{R}\}$ . When  $\epsilon$  value is equal as 0, we will get a perfect regression. Suppose we have a function as regression line below:

$$f(x) = w \cdot \phi(x) + b \quad (2)$$

By  $\phi(x)$  shows a point in feature space  $F$  the mapping result of  $x$  in input space. Coefficient of  $w$  and  $b$  are estimated by minimizing the risk function that describes in the following formulation:

$$\min \frac{1}{2} \|w\|^2 + C \frac{1}{l} \sum_{i=1}^l L_{\epsilon}(y_i, f(x_i)) \quad (3)$$

Depends on

$$y_i - w\phi(x_i) - b \leq \epsilon$$

$$w\phi(x_i) + b - y_i \leq \epsilon, i = 1, 2, 3, \dots, \ell$$

With,

$$L_\epsilon(y_i, f(x_i)) = \begin{cases} |y_i - f(x_i)| - \epsilon, & |y_i - f(x_i)| \geq \epsilon \\ 0, & \text{to the others} \end{cases}$$

By minimizing  $\|w\|^2$  will make the function as thin as possible, as a result the capacity function can be controlled.  $\epsilon$ -insensitive loss function required to minimize norm from  $w$  achieve better generalization to regression function  $f(x)$ . That is why we have to solve the following problem:

$$\min \frac{1}{2} \|w\|^2 \tag{4}$$

Depends on:

$$y_i - w\phi(x_i) - b \leq \epsilon$$

$$w\phi(x_i) + b - y_i \leq \epsilon, i = 1, 2, 3, \dots, \ell$$

Assume the function of  $f(x)$  which can approximate to all of these points  $(x_i, y_i)$ . Then, we will get a cylinder as describe in Figure 2.

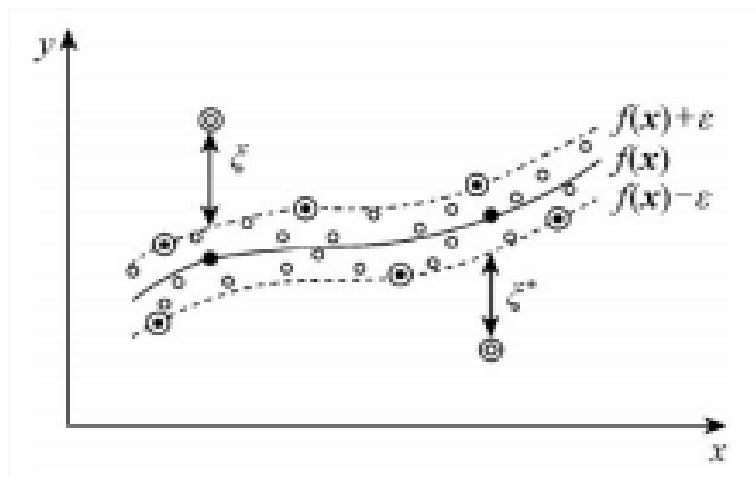


Figure 2. Regression Function at SVR [15]

Accuracy of  $\epsilon$  in this case we assume that all points in the range  $f \pm \epsilon$  (feasible). In the case of ineligibility, where there are some points that may be out of range  $f \pm \epsilon$ , we need to add variable of slack  $\xi, \xi^*$ . Furthermore, the optimization problem can use the following formula:

$$\min = \frac{1}{2} \|w\|^2 + C \sum_{i=1}^{\ell} (\xi_i + \xi_i^*) \tag{5}$$

Depends on:

$$y_i - w^T\phi(x_i) - \xi_i - b \leq \epsilon, i = 1, 2, 3, \dots, \ell$$

$$w\phi(x_i) - y_i - \xi_i^* + b \leq \epsilon, i = 1, 2, 3, \dots, \ell$$

$$\xi, \xi^* \geq 0$$

The constant of  $C > 0$  determined the bargaining between the thinness of function  $f$  and the upper limit of deviation that more than  $\epsilon$  was still tolerated.  $\epsilon$  was comparable to the accuracy of the approximation of the training data. The highest value of  $\epsilon$  was related to  $\xi_i^*$  that has small and low approximation accuracy. The highest value for variable  $\xi_i^*$  will make empirical errors which have a considerable influence on the regularization factor. In SVR support vector there was the training data which located out of  $f$  from the decision function.

By  $C$  was determined by user,  $K(x_i, x_j)$  was dot-product kernel that identified as  $K(x_i, x_j) = \phi^T(x_i) \phi^T(x_j)$ , by using Lagrange multipliers and optimalization condition, The regression function was formulated explicitly in the following formula:

$$f(x) = \sum_{i=1}^l (\alpha_i - \alpha_i^*) K(x, x_i) + b \tag{6}$$

Before doing training and test of SVR, it is better for us to decide parameter value of  $C$ ,  $\epsilon$  to the function of Linear Kernel and  $C$  parameter,  $\epsilon$ , and  $\gamma$  to RBF kernel function.

## 2. Research Method

This study was undertaken in several phases. All of those phases can be seen in the following figure Figure 3.

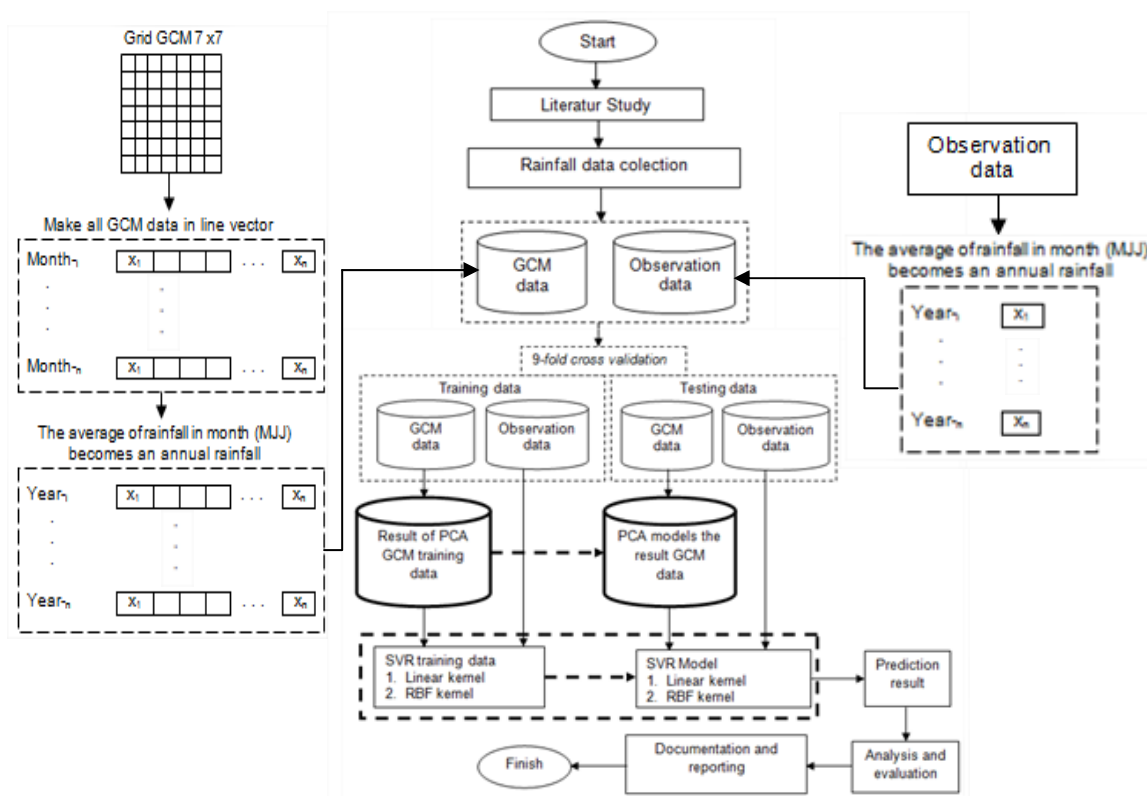


Figure 3. Research Flowchart

The beginning of this study was literature review; it used in order to understand all problems that will be researched. The data used in this research is secondary data divided to GCM hindcast data result (used as clarify variable) and data of rainfall observation (used as respond variable). Result of GCM hindcast data was acquired from the Climate Information Tool Kit (CLIK) APEC Climate Center (APCC) as the rainfall data and type of ASCII file which consists of 6 models with a resolution grid of latitude and longitude  $2.5^0 \times 2.5^0$ , data accessed

from the website CLIK APCC (<http://clik.apcc21.org>), as well as two models of GCM hindcast rainfall obtained from the website of the International Research Institute Data Library (IRIDL) (<http://iridl.ldeo.columbia.edu>), as data of Climate Prediction Center (CPC) Unified Gauge-Based Analysis of Global Daily Precipitation from The International Research Institute for Climate and Society (IRI) and TSV file type with a grid resolution of latitude and longitude  $0.5^{\circ} \times 0.5^{\circ}$ . Hindcast GCM data used to build prediction model in 3 different months: May, June, and July (MJJ) from the year of 1982-2008 (27 years) every model at every rainfall station. In this study, there are 8 GCM hindcast rainfalls to build prediction model as shown in Table 1.

The data of rainfall observation (respond variable) is the average value of seasonal rainfall at every rainfall station in Indramayu by longitudinal position of  $107^{\circ}52'-108^{\circ}36'BT$  and  $6^{\circ}15'-6^{\circ}40'LS$ , it was obtained from the measurement and test that performed by Meteorology Department in Indramayu. There were 15 observation stations used as shown in Table 2. The data of rainfall observation was used 3 months: May, June, July (MJJ) from the year of 1982-2008 (27 years) at every rainfall station.

Data of GCM was cropped in grid of  $7 \times 7$  and then make all of GCM data model to the line vector; Next, average rainfall of data GCM and observations to be the annual rainfall. Furthermore, distribute training and test data by using 9-fold cross Validation, 9 is divided due to the number of year and redone in nine times. The data PCA is necessary to be done because it can avoid the double linear data in GCM model and to save computing time during training and testing the SVR model. Reduction process is held by taking one or more major components with diversity of  $\geq 98\%$ . Finally the SVR training and testing can be done.

Tabel 1. The Data of GCM Hindcast Rainfall and its Founders

No	Model Name	Ensemble	Institution	Sources	References
1	GCPS T63T21	4	Korea	<a href="http://clik.apcc21.org">http://clik.apcc21.org</a>	[16]
2	GDAPS T106L21	20	Korea	<a href="http://clik.apcc21.org">http://clik.apcc21.org</a>	[16]
3	CMC1-CanCM3	120	Columbia	<a href="http://iridl.ldeo.columbia.edu">http://iridl.ldeo.columbia.edu</a>	[17], [19]
4	CanCM3-AGCM3	10	Canada	<a href="http://clik.apcc21.org">http://clik.apcc21.org</a>	[16]
5	GFDL-CM2P1	120	Columbia	<a href="http://iridl.ldeo.columbia.edu">http://iridl.ldeo.columbia.edu</a>	[17], [19]
6	NASA-GSFC L34	8	U.S.A	<a href="http://clik.apcc21.org">http://clik.apcc21.org</a>	[16]
7	METRI AGCM L17	10	Korea	<a href="http://clik.apcc21.org">http://clik.apcc21.org</a>	[16]
8	PNU	5	Korea	<a href="http://clik.apcc21.org">http://clik.apcc21.org</a>	[16]

Tabel 2. The Name and Location of the 15 Rainfall Observation Stations in Indramayu

Y	Station Name	LS	BT	Y	Station Name	LS	BT
Y <sub>1</sub>	Bangkir	-6.336	108.325	Y <sub>9</sub>	Ujungaris	-6.457	108.287
Y <sub>2</sub>	Bulak	-6.338	108.116	Y <sub>10</sub>	Loh berner	-6.406	108.282
Y <sub>3</sub>	Cidempet	-6.354	108.246	Y <sub>11</sub>	Sudimampir	-6.402	108.366
Y <sub>4</sub>	Cikedung	-6.492	108.185	Y <sub>12</sub>	Juntinyuat	-6.433	108.438
Y <sub>5</sub>	Losarang	-6.398	108.146	Y <sub>13</sub>	Krangkeng	-6.503	108.483
Y <sub>6</sub>	Sukadana	-6.535	108.300	Y <sub>14</sub>	Bondan	-6.606	108.299
Y <sub>7</sub>	Sumurwatu	-6.337	108.325	Y <sub>15</sub>	Kedokan	-6.509	108.424
Y <sub>8</sub>	Tugu	-6.433	108.333		Bunder		

### 3. Results and Analysis

Downscaling model by using SVR to predict the rainfall in dry season with clarify variable in model of GCM and observation of rainfall as respond variable, All of those data were used at every 15 rainfall stations in Indramayu. Here are the results of the prediction of the model GCM rainfall averaged as shown in Table 3.

Based on the prediction result on Table 3, it can be said that the result will be better if it has a high correlation while RMSE in low value. On the kernel linear function the high correlation value was obtained at Cikedung rainfall station. On the other hand, the low correlation value was gotten at Cidampet rainfall station. Overall, it can be concluded that result production by using kernel linear function was better than RBF kernel function. It was marked by the correlation value or RMSE value in every rainfall station.

Tabel 3. The Average Correlation of the Prediction Result by using GCM Model Data and RMSE Values between Rainfall Observation in Indramayu

No	Station	Kernel Linear		Kernel RBF	
		Correlation	RMSE	Correlation	RMSE
1	Bangkir	0.578	62.269	0.562	67.799
2	Bulak	0.684	26.052	0.345	30.298
3	Cidempet	<b>0.401</b>	<b>36.964</b>	0.241	35.353
4	Cikedung	<b>0.744</b>	<b>23.937</b>	0.538	42.483
5	Losarang	0.721	26.955	0.556	32.823
6	Sukadana	0.419	30.517	0.528	31.287
7	Sumurwatu	0.670	36.918	-0.053	42.855
8	Tugu	0.651	28.449	0.472	32.258
9	Ujungaris	0.515	29.653	0.422	32.261
10	Lohbener	0.675	32.349	0.579	35.478
11	Sudimampir	0.514	55.424	0.472	57.634
12	Juntinyuat	0.611	44.384	0.648	49.783
13	Kedokan Bunder	0.726	39.267	0.696	43.202
14	Krangkeng	0.655	43.335	0.414	49.422
15	Bondan	0.681	24.730	0.208	27.580

The best GCM model was in Taylor chart that closer to the observation point. By looking at standard deviation, RMSE and correlation, observation point is the standard deviation of data point at a particular location [20]. There are 8 explanation of GCM models we can find at Taylor chart, they are: 1. CMC1-CanCM3, 2. GDAPS T106L21, 3. GFDL-CM2P1, 4. GCPS T63T21, 5. CanCM3-AGCM3, 6. METRI AGCM L17, 7. NASA-GSFC L34, 8. PNU. Here is Taylor chart for GCM model at Cikedung and Cidempet rainfall station as shown in Figure 5.

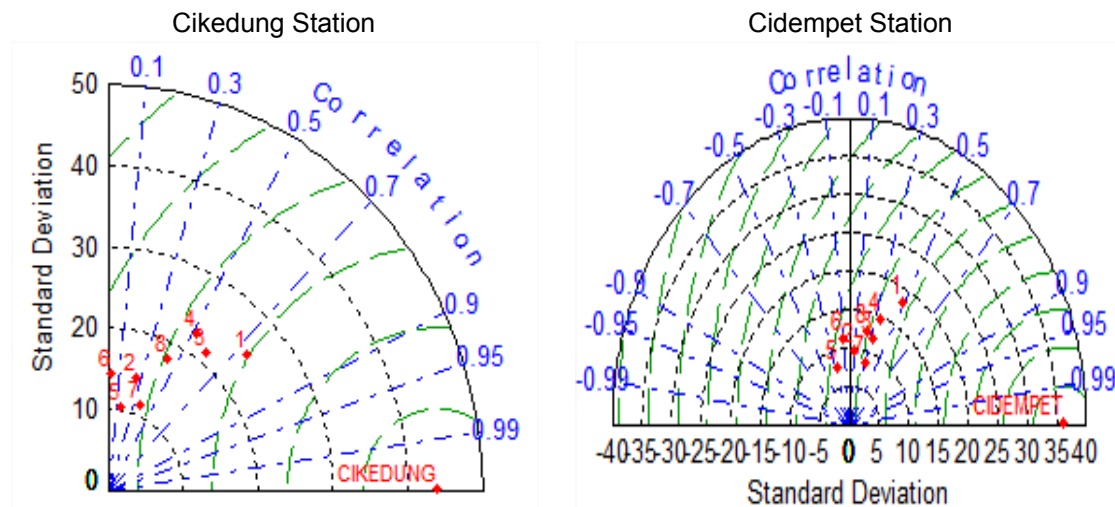


Figure 5. Taylor Chart for GCM Model

Based on the chart in Figure 5, it was known that Cikedung rainfall station was at standard deviation about  $\pm 44$  and RMSE value  $\pm 30$ . The 1 model was potentiality to be the best model in this location if it compared to another model while Cidempet rainfall station was at  $\pm 36$  standard deviation. The 1 model became the best model in this location if it compared to another model. But, the 1 model at Cidempet station was not as better as 1 model at Cikedung station, it was caused by the 1 model at Cidempet station has  $\pm 32$  RMSE value. The overall of linear kernel function was better than RBF kernel function.

#### 4. Conclusion

To sum it up, the models which were resulted to predict the rainfall in dry season will be better if it looked from the average of prediction result or the error average. The best correlation value was obtained at Cikedung rainfall station in 0.744 correlation value and 23.937 RMSE while the lowest linear kernel function was gained at Cidempet rainfall station in 0.401 correlation value and 36.964 RMSE. The kernel function of RBF was not included to the best function because the result prediction was lower than linear kernel function. It can be seen from the correlation value or RMSE on RBF kernel function.

Suggestion to the next research, downscaling model of GCM model data can be applied in order to predict the rainfall in dry season by using Support Vector Regression. The utilization of GCM grid can be used besides grid of 7x7. The accuracy was not high yet, and then the selection of parameter values for each kernel function needs to be performed with other optimization techniques.

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