

# Optimal proportional-integral speed control for closed-loop engine timing system

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## ABSTRACT

In internal combustion engines, adjusting the air-fuel ratio is essential to control the speed and minimize the burnt fuel. The throttle opening is the actuator to control the air-fuel. A better design for the used/conventional controller can give a better response without additional cost. In this work, the proposed controller gains of the proportional-integral (PI) controller are tuned to enhance the speed in constant and variable drive cycle modes. The tuning process is conducted based on two of the most efficient performance indices used in this field. The performance indices are integral absolute error (IAE) and integral time absolute error (ITAE). The optimization problem is solved using three reliable stochastic optimization algorithms to ensure mature convergence of the solutions, to avoid local optima solutions, and to ensure effective shrinking of the search space. The optimization algorithms are teaching-learning-based optimization (TLBO), particle swarm optimization (PSO), and genetic algorithm (GA). Different simulations are conducted to validate the results. The results are compared with conventional tuning methods regarding the system's time response.

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## 1. INTRODUCTION

Improving the heavy-duty vehicle (HDV) engine's performance is essential as this reduces energy consumption and air pollution significantly. The exhaust gases from diesel engines that run most of the HDV, especially nitrogen oxides, are a major environmental problem. The sequences of this economic-environmental issue can be mitigated using different fuel injection techniques. As the ignition process is a nonlinear system, it is challenging to model the engine and tune the used controllers. Typical internal combustion (IC) engines convert chemical energy and fuel to mechanical energy and continuously repeat four strokes. Suction, compression, power, and exhaust strokes are the strokes that form the cycle of continuous power production. Therefore, the mechanical design, the IC engine, and the tuning of the used controllers are crucial in optimizing the fuel consumption and performance in HDV.

Three different stochastic optimization algorithms are adopted in this study. Genetic algorithm (GA) [1]–[4] and particle swarm optimization (PSO) [5]–[8] as the most efficient metaheuristic techniques besides the newly adopted teaching-learning-based optimization (TLBO) [9], [10] are the employed algorithms in the minimization problem. Those three algorithms show excellent results in many nonlinear control systems in different engineering fields where GA was effectively used in multilevel inverters for the photovoltaic system as a replacement for the conventional tuning method [11] and doubly-fed induction generator for maximizing

the power extracted from the wind [12]. PSO and its modified versions were used to select the optimal location of charging stations for electric vehicles (EV) [13] and permanent magnet direct current motors [14]. TLBO was recently used to solve optimal power flow problems and showed competitive results compared with different optimization techniques [15], inductor-capacitor-inductor (LCL) filter design [16], and voltage source inverter design [17]. TLBO outperformed many other rigorous optimization techniques due to the absence of any tunable gains and weighting factors. Recently, many different evolutionary algorithms have been used, which include the gravitational-search algorithm [18]–[21], grey wolf optimizer [22]–[24], and artificial bee colony algorithm [25]–[27].

This paper optimizes the HDV speed controller's proportional-integral (PI) gains ( $K_P$  and  $K_I$ ) to achieve better accurate reference tracking performance under variable drive cycles. Besides stochastic algorithms, some other tuning methods can be used, but they are mainly subjected to linear systems [28]. Two objective functions are used in this study, the integral time-weighted absolute error (ITAE) and the integral absolute error (IAE), to quantify the performance of the control system under the proposed optimization precisely [29].

## 2. MODELLING OF THE ENGINE TIMING SYSTEM

The system under study is summarized in Figure 1. The engine is loaded, and the speed of the engine is controlled. The speed controller will send the control command to the throttle and manifold. The throttle and manifold can be modeled using (1) through (5).

$$\dot{m}_i = y(\theta)q(P) \tag{1}$$

$$y(\theta) = 2.821 - 0.05231(\theta) + 0.10299(\theta^2) - 0.00063(\theta^3) \tag{2}$$

$$q(P) = \begin{cases} 1 & P \leq 0.5P_a \\ \frac{2\sqrt{PP_a - P^2}}{P_a} & 0.5P_a \leq P \leq P_a \\ \frac{-2\sqrt{PP_a - P^2}}{P} & P_a \leq P \leq 2P_a \\ -1 & P \geq 2P_a \end{cases} \tag{3}$$

Where  $\dot{m}_i$  is the manifold input mass flow rate,  $\theta$  is the throttle angle,  $y$  is the throttle empirical formula, and  $P$  and  $P_a$  are manifold and the ambient pressure, respectively.

$$\dot{P}_m = \frac{RT(\dot{m}_i - \dot{m}_o)}{V_m} \tag{4}$$

$$\dot{m}_o = -366x10^{-3} + 8979x10^5(\omega)(P) - 337x10^4(\omega)(P^2) + 1x10^4(\omega^2)(P) \tag{5}$$

Where  $\dot{P}_m$  is the manifold pressure rate of change,  $\dot{m}_o$  is the manifold output mass flow rate,  $R$  is the specific gas constant,  $T$  is the temperature,  $\omega$  is the angular crank speed, and  $V_m$  is the manifold volume.

After finishing the compression, the fuel mass will start the combustion stage. In the combustion stage, the developed torque is related to the air ( $A$ ) to fuel ( $F$ ) ratio ( $\delta$ ), speed, spark advance  $\sigma$ , and air mass ( $m_a$ ) according to (6).

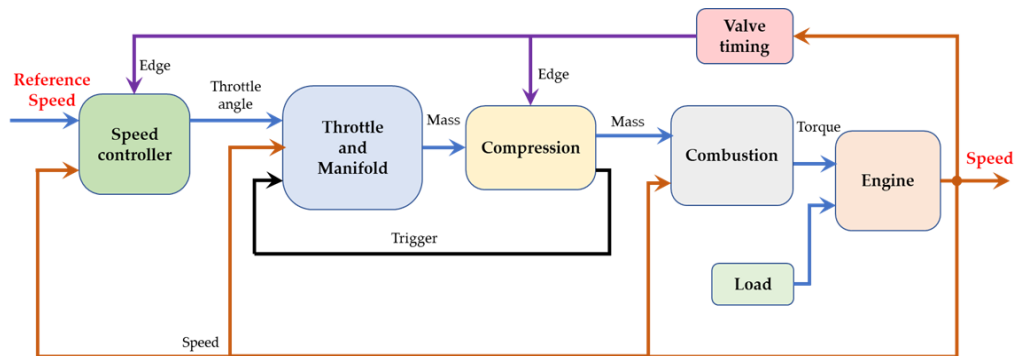


Figure 1. Speed-controlled engine timing system

$$\tau = -181.3 + 379.36(m_a) + 21.91(\delta) - 0.85(\delta^2) + 0.26(\sigma) - 0.0028(\sigma^2) + 0.027(\omega) - 1.07 \times 10^{-4}(\omega^2) + 4.8 \times 10^{-4}(\omega)(\sigma) + 2.55(\sigma)(m_a) - 0.05(m_a)(\sigma^2) \quad (6)$$

The engine's acceleration is related to the dynamic of the rotating parts. The accelerating torque, the difference between the developed and load torque, is the main factor determining if the engine is in accelerating or decelerating mode. According to Newton's second law, the acceleration of the engine ( $\dot{\omega}$ ) can be expressed as in (7).

$$\dot{\omega} = \frac{\tau - \tau_L}{J} \quad (7)$$

Where  $J$  is the inertia and  $\tau_L$  is the load torque.

### 3. FORMULATION OF THE OPTIMIZATION PROBLEM

In this work, as the controller is a PI-controller and the objective function is ITAE or IAE, the optimization problem can be formulated as (8).

$$\begin{aligned} & \min \quad \{ITAE \text{ or } IAE \\ & \text{Subject to} \quad \begin{cases} K_I^{min} \leq K_I \leq K_I^{max} \\ K_P^{min} \leq K_P \leq K_P^{max} \\ |e_{ss}| \leq \varepsilon \end{cases} \end{aligned} \quad (8)$$

The equations describe the objective functions or error indices as (9) and (10).

$$ITAE = \int t \cdot e(t) dt \quad (9)$$

$$IAE = \int |e(t)| dt \quad (10)$$

The values;  $K_I^{min}$ ,  $K_I^{max}$ ,  $K_P^{min}$ ,  $K_P^{max}$  are the minimum and the maximum limits of the PI gains ( $K_P$  and  $K_I$ ), respectively,  $e_{ss}$  is the steady-state error,  $e(t)$  is the error signal, and  $t$  is the time. Both the integral and the proportional controllers are needed to achieve the required performance of the speed controller. Adding an integral controller is essential as the operating speed changes with time. On the other hand, the phase lag associated with the integral controller needs to be reduced by the proportional controller. The maximum limits for the two gains are selected first by solving the optimization problem at many different loading and speed conditions while considering the realistic drive cycle of the HDV. Then, the maximum obtained gain is multiplied by at least 10. The minimum limit for both gains is set to be exceedingly small ( $K_{I,P}^{min}=10^{-12}$ ) to avoid any simulation errors. It is essential to highlight that the optimization problem failed to have a feasible solution when the objective function is *ISE* as defined in (8).

### 4. SIMULATION RESULTS

Initially, to verify the power of the three used algorithms and the proposed work, the results will be compared with the well-tuned speed controller in [30] where ( $K_P=0.05$  and  $K_I=0.1$ ). Then, three performance indices are selected to assess the transient response performance. The rise time ( $t_r$ ) and the settling time ( $t_s$ ) are strong indicators of the speed of the controlled system. At the same time, the percentage overshoot ( $O.S$ ) indicates the maximum deviation before reaching the new steady state value.

The results from the three algorithms (GA, PSO, and TLBO) are close, and the best result for each objective function is selected as in Table 1. The number of fractions in Table 1 has no meaning and is listed to show the difference between the results from the two objectives. In practice, this accuracy is complex to be implemented in some microcontrollers.

From Table 1, the optimal gains considering the two objectives are close, and the number of digits is high to clarify this point. For the system described in Figure 1, the speed reference is suddenly changed from 2,000 rpm to 3,000 rpm at  $t=5$  s, and the step responses are shown in Figure 2 for the three cases. The transient response analysis and the three performance indices are summarized in Table 2.

From Table 2, the system exhibits faster dynamic performance when the objective function is not time-dependent, and the O.S is minimal when ITAE is the objective function. For all performance indices,

the results from the proposed work are better than those from the reference case. Compared with the reference [30] gains, the proposed work has better results;  $t_r$  is less than by 31.49%,  $t_s$  is less by 9.76%, and the O.S is less by 9.76%. In HDV applications, the objective function includes minimizing the overshoot.

- **Case-2:** this case represents the controller with  $K_p=0.033$  and  $K_I=0.064$ . The objective of ‘Case 2’ is to minimize the vehicle speed overshoot.
- **Case 3:** this case represents the controller with  $K_p=0.061$  and  $K_I=0.072$ . These values are required to eliminate speed overshoot.

Figure 3 shows the relation between the controller's speed and the overshoot. The proposed work has the highest O.S and the fastest response. The same logic applies to ‘Case 2’ and ‘Case 3’. The O.S is eliminated in ‘Case 3’, but the response is the slowest. As listed in Table 3 and assuming the IAE case as a reference,  $t_r$  of ‘Case 2’ is slower by 102.2%, and  $t_s$  is slower by 7.17%. The controller of ‘Case 3’ is slower. The  $t_r$  is slower by 55.34%, and  $t_s$  is slower by 8.93%. Considering the overshoot, ‘Case 2’ has a better response of 76.87% and 100% for ‘Case 3’ as it is eliminated.

Table 1. Optimal results for  $K_p$  and  $K_I$  based on two objective functions (ITAE and IAE)

| Objective function | $K_p$       | $K_I$       |
|--------------------|-------------|-------------|
| ITAE               | 0.253537678 | 0.118603873 |
| IAE                | 0.27397976  | 0.119128857 |
| ITAE-IAE           | 0.020442082 | 0.000524984 |

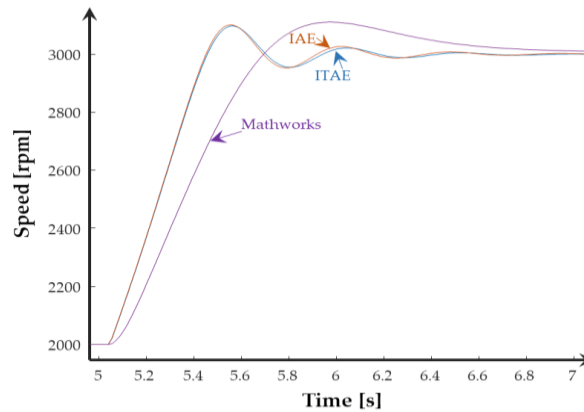


Figure 2. Step responses of three different controllers

Table 2. Comparative results for the transient response

|       | IAE      | MathWorks | Improvement (%) |
|-------|----------|-----------|-----------------|
| $t_r$ | 0.315889 | 0.461088  | 31              |
| $t_s$ | 6.07092  | 6.72723   | 9.6             |
| O.S   | 10.04829 | 11.124158 | 9.6             |

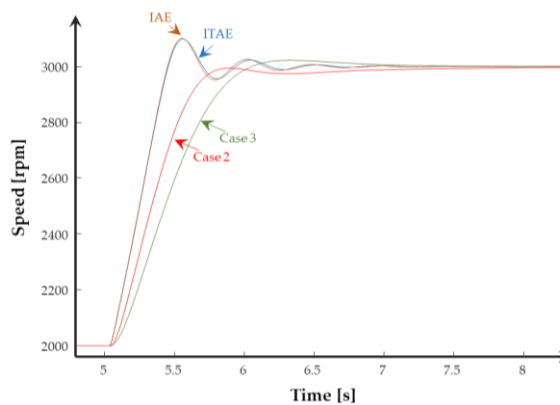


Figure 3. Step responses for the two proposed controllers and the new objectives

Table 3. Comparative results for the transient response of the proposed work and the minimum O.S controllers

|           | ITAE     | IAE      | Case 2   | Case 3  |
|-----------|----------|----------|----------|---------|
| $t_r$ (s) | 0.31836  | 0.315889 | 0.63876  | 0.49069 |
| $t_s$ (s) | 6.08049  | 6.07092  | 6.506006 | 6.61319 |
| O.S       | 9.793149 | 10.04829 | 2.32440  | 0       |

## 5. CONCLUSION

In this work, three different optimization algorithms are adopted to tune the gains of the PI controller of the speed-controlled engine timing system. GA, PSO, and TLBO are used to make sure that the results are optimal. Two objective functions are selected to enhance the transient response of the speed controller. The ITAE and IAE are measured when a sudden change in the speed reference is applied. The effectiveness of the proposed work is tested by comparing the results with highly tuned speed controllers. Three transient response indicators validate the work's superiority: the rise time, the settling time, and the overshoot. The objective function is also compared with another objective in which the maximum transient deviation has to be minimized or eliminated.

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## REFERENCES

- [1] M. Chattoraj and U. R. Vinayakamurthy, "A hybrid approach to enhanced genetic algorithm for route optimization problems," *Indonesian Journal of Electrical Engineering and Computer Science (IJECS)*, vol. 30, no. 2, pp. 1099–1105, 2023, doi: 10.11591/ijeecs.v30.i2.pp1099-1105.
- [2] S. Katoch, S. S. Chauhan, and V. Kumar, "A review on genetic algorithm: past, present, and future," *Multimedia Tools and Applications*, vol. 80, pp. 8091–8126, Feb. 2021.
- [3] M. S. A. Forhad, M. S. Hossain, M. O. Rahman, M. M. Rahaman, M. M. Haque, and M. K. H. Patwary, "An improved fitness function for automated cryptanalysis using genetic algorithm," *Indonesian Journal of Electrical Engineering and Computer Science (IJECS)*, vol. 13, no. 2, pp. 643–648, 2019, doi: 10.11591/ijeecs.v13.i2.pp643-648.
- [4] A. Abdelaziz, V. Santos, M. S. Dias, and A. N. Mahmoud, "A hybrid model of self-organizing map and deep learning with genetic algorithm for managing energy consumption in public buildings," *Journal of Cleaner Production*, vol. 434, p. 140040, Jan. 1, 2024.
- [5] B. M. Abed and W. M. Jasim, "Multi-objective optimization path planning with moving target," *IAES International Journal of Artificial Intelligence (IJ-AI)*, vol. 11, no. 3, pp. 1184–1196, Sep. 2022, doi: 10.11591/ijai.v11.i3.pp1184-1196.
- [6] S. A. Altamir, M. A. Kahya, and A. S. Y. Aladool, "Shooting swarm algorithm for solving two-point boundary value problems," *Indonesian Journal of Electrical Engineering and Computer Science (IJECS)*, vol. 29, no. 1, pp. 553–561, 2023, doi: 10.11591/ijeecs.v29.i1.pp553-561.
- [7] E. Karunarathne, J. Pasupuleti, J. Ekanayake, and D. Almeida, "Comprehensive learning particle swarm optimization for sizing and placement of distributed generation for network loss reduction," *Indonesian Journal of Electrical Engineering and Computer Science (IJECS)*, vol. 20, no. 1, pp. 16–23, 2020, doi: 10.11591/ijeecs.v20.i1.pp16-23.
- [8] R. S. Raheem, M. Y. Hassan, and S. K. Kadhim, "Particle swarm optimization based interval type 2 fuzzy logic control for motor rotor position control of artificial heart pump," *Indonesian Journal of Electrical Engineering and Computer Science (IJECS)*, vol. 25, no. 2, pp. 814–824, 2022, doi: 10.11591/ijeecs.v25.i2.pp814-824.
- [9] X. Yu and W. Zhang, "A teaching-learning-based optimization algorithm with reinforcement learning to address wind farm layout optimization problem," *Applied Soft Computing*, vol. 151, p. 111135, Jan. 2024, doi: 10.1016/j.asoc.2023.111135.
- [10] T. Brar, T. Kumar, and M. K. Sharma, "Optimizing multimodal transportation systems using the teaching-learning-based algorithm," *International Journal of Applied and Computational Mathematics*, vol. 10, no. 1, p. 18, Feb. 2024, doi: 10.1007/s40819-023-01655-8.
- [11] T. G. Manjunath and A. Kusagur, "Analysis of different meta heuristics method in intelligent fault detection of multilevel inverter with photovoltaic power generation source," *International Journal of Power Electronics and Drive Systems (IJPEDS)*, vol. 9, no. 3, pp. 1214–1222, Sep. 2018, doi: 10.11591/ijpeds.v9.i3.pp1214-1222.
- [12] N. Elmouhi, A. Essadki, and H. Elaimani, "Robust control of wind turbine based on doubly-fed induction generator optimized by genetic algorithm," *International Journal of Power Electronics and Drive Systems (IJPEDS)*, vol. 13, no. 2, pp. 674–688, 2022, doi: 10.11591/ijpeds.v13.i2.pp674-688.
- [13] M. A. Zaki, T. Mahmoud, M. Atia, and E. S. A. El Aziz Osman, "Optimal sizing and siting of electric vehicle charging station by using archimedes optimization algorithm technique," *International Journal of Power Electronics and Drive Systems (IJPEDS)*, vol. 12, no. 4, pp. 2557–2569, Dec. 2021, doi: 10.11591/ijpeds.v12.i4.pp2557-2569.
- [14] K. G. Abdullhussein, N. M. Yasin, and I. J. Hasan, "Comparison between butterfly optimization algorithm and particle swarm optimization for tuning cascade pid control system of pmdc motor," *International Journal of Power Electronics and Drive Systems (IJPEDS)*, vol. 12, no. 2, pp. 736–744, 2021, doi: 10.11591/ijpeds.v12.i2.pp736-744.
- [15] S. Albatran, S. Harasis, M. Ialomoush, Y. Alsmadi, and M. Awawdeh, "Realistic optimal power flow of a wind-connected power system with enhanced wind speed model," *IEEE Access*, vol. 8, pp. 176973–176985, 2020, doi: 10.1109/ACCESS.2020.3027065.
- [16] S. Albatran, A. Koran, I. A. Smadi, and H. J. Ahmad, "Optimal design of passive RC-damped LCL filter for grid-connected voltage source inverters," *Electrical Engineering*, vol. 100, no. 4, pp. 2499–2508, 2018, doi: 10.1007/s00202-018-0725-5.




- [17] H. Jamal, S. Albatran, and I. A. Smadi, "Optimal design of output LC filter and cooling for three-phase voltage-source inverters using teaching-learning-based optimization," in *2016 IEEE Energy Conversion Congress and Exposition (ECCE)*, IEEE, Sep. 2016, pp. 1–6, doi: 10.1109/ECCE.2016.7855316.
- [18] S. Albatran, M. I. Alomoush, and A. M. Koran, "Gravitational-search algorithm for optimal controllers design of doubly-fed induction generator," *International Journal of Electrical and Computer Engineering (IJECE)*, vol. 8, no. 2, pp. 780–792, 2018, doi: 10.11591/ijece.v8i2.pp780-792.
- [19] F. W. Ipeyeda, M. O. Oyediran, S. A. Ajagbe, J. O. Jooda, and M. O. Adigun, "Optimized gravitational search algorithm for feature fusion in a multimodal biometric system," *Results in Engineering*, vol. 20, p. 101572, Dec. 1, 2023.
- [20] Z. Ahmad, T. Mahmood, A. Rehman, T. Saba, and F. S. Alamri, "Enhancing time series forecasting with an optimized binary gravitational search algorithm for echo state networks," *IEEE Access*, Jul. 5, 2023. DOI: 10.1109/ACCESS.2023.3111502.
- [21] S. A. Halim, A. Mohamed, N. A. M. Kamari, A. Ayob, A. H. A. Bakar, and H. A. Illias, "Optimisation of zinc oxide surge arrester design using gravitational search algorithm and imperialist competitive algorithm," *Indonesian Journal of Electrical Engineering and Computer Science (IJECS)*, vol. 13, no. 3, pp. 853–860, 2019, doi: 10.11591/ijeecs.v13.i3.pp853-860.
- [22] F. A. Izzaqi, N. A. Windarko, and O. A. Qudsi, "Minimization of total harmonic distortion in neutral point clamped multilevel inverter using grey wolf optimizer," *International Journal of Power Electronics and Drive Systems (IJPEDS)*, vol. 13, no. 3, pp. 1486–1497, 2022, doi: 10.11591/ijpeds.v13.i3.pp1486-1497.
- [23] X. Yu, Q. Zhao, Q. Lin, and T. Wang, "A grey wolf optimizer-based chaotic gravitational search algorithm for global optimization," *The Journal of Supercomputing*, vol. 79, no. 3, pp. 2691–2739, Feb. 2023.
- [24] M. Z. M. Tumari, M. H. Suid, and M. A. Ahmad, "A modified grey wolf optimizer for improving wind plant energy production," *Indonesian Journal of Electrical Engineering and Computer Science (IJECS)*, vol. 18, no. 3, pp. 1123–1129, Jun. 2020, doi: 10.11591/ijeecs.v18.i3.pp1123-1129.
- [25] V. H. Ahgajan, Y. G. Rashid, and F. M. Tuaimah, "Artificial bee colony algorithm applied to optimal power flow solution incorporating stochastic wind power," *International Journal of Power Electronics and Drive Systems (IJPEDS)*, vol. 12, no. 3, pp. 1890–1899, 2021, doi: 10.11591/ijpeds.v12.i3.pp1890-1899.
- [26] S. E. Comert and H. R. Yazgan, "A new approach based on hybrid ant colony optimization-artificial bee colony algorithm for multi-objective electric vehicle routing problems," *Engineering Applications of Artificial Intelligence*, vol. 123, p. 106375, Aug. 1, 2023.
- [27] T. Ye, H. Wang, T. Zeng, M. G. Omran, F. Wang, Z. Cui, and J. Zhao, "An improved two-archive artificial bee colony algorithm for many-objective optimization," *Expert Systems with Applications*, vol. 236, p. 121281, Feb. 1, 2024.
- [28] S. Albatran, I. A. Smadi, and H. A. Bataineh, "Generalized optimal and explicit PI/PID tuning formulas for underdamped second-order systems," *International Journal of Control, Automation and Systems*, vol. 18, no. 4, pp. 1023–1032, Apr. 2020, doi: 10.1007/s12555-019-0178-2.
- [29] M. Pietrala, P. Leśniewski, and A. Bartoszewicz, "An ITAE Optimal Sliding Mode Controller for Systems with Control Signal and Velocity Limitations," *Acta Mechanica et Automatica*, vol. 17, no. 2, pp. 230–238, 2023, doi: 10.2478/ama-2023-0022.
- [30] MathWorks, "Engine timing model with closed loop control." Accessed: Oct. 15, 2023. [Online]. Available: <https://www.mathworks.com/help/simulink/slref/engine-timing-model-with-closed-loop-control.html>

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