# Analysis of DFIG Wind Turbine During Steady-State and Transient Operation

**Omer Elfaki Elbashir\*[1], Wang Zezhong[2], Liu Qihui[3]**
School of Electrical and Electronics Engineering,
Telphone: +8613693044769, North China Electric Power University, Beijing, China
\*Corresponding auther e-mail: omer.elbashir@yahoo.com\*[1], wzzh@ncepu.edu.cn[2], liuqihuifei@sohu.com[3]

***Abstract***

*In recent years, there has been a worldwide growth in the exploitation of wind energy. In the wind power industry, the majority of grid-connected wind turbines are equipped with doubly fed induction generators (DFIGs) because of their advantages over other wind turbine generator (WTG) systems. Therefore, much research effort has gone into the issues of modeling, analysis, control and grid integration of DFIG wind turbines. This paper deals with the modeling, analysis, and simulation of a DFIG driven by a wind turbine. The grid connected wind energy conversion system (WECS) is composed of DFIG and two back to back PWM voltage source converters (VSCs) in the rotor circuit. A machine model is derived in an appropriate $dq$ reference frame. The grid voltage oriented vector control is used for the grid side converter (GSC) in order to maintain a constant DC bus voltage, while the stator voltage oriented vector control is adopted in the rotor side converter (RSC) to control the active and reactive powers.*

*Keywords: DFIG, $dq$ vector control, PWM, Wind Turbine, WECS*

## 1. Introduction

Since a few years ago, the wind power generation has been commercialized because of high fuel efficiency and low air pollution. The generator technology used for variable-speed constant-frequency (VSCF) has gone a long way. Nowadays, the most popular motors used for wind power system are permanent magnets synchronous generators (PMSG) and DFIG [1].

Wind energy is one of the most important and promising sources of renewable energy all over the world, mainly because it is considered to be nonpolluting and economically viable. At the same time, there has been a rapid development of related wind turbine technology [2]. The majority of grid-connected wind turbines are equipped with DFIGs. DFIG is based on a wound rotor induction machine (WRIM), where the 3-phase rotor windings are supplied with a voltage of controllable amplitude and frequency using an ac to ac converter. Consequently, the speed can be varied while the operating frequency of the stator side remains constant.

Depending on the required speed range, the rotor converter rating is usually low compared with the machine rating. Therefore, a DFIG is preferable for variable speed wind turbine applications [3]. The choice of control strategy incorporated can vary depending on the wind turbine generators, but the most popular control scheme for the DFIG of wind turbine generators is a field oriented control (FOC).

This control strategy is well established in the field of variable speed drives and when applied to the DFIG control, allows independent control of the electromagnetic torque and stator reactive power [4]. The DFIG using back to back PWM converters for the rotor side control has been well established in the wind power system. When used with a wind turbine it offers several advantages over the fixed speed generator systems.

These advantages, including speed control and reduced flickers, are primarily achieved by controlling the VSC, with its inherent bi-directional active and reactive powers flow [5]. Among the various technologies available for WECSs, the DFIG is one of the preferred solutions because it reduced mechanical stress and optimized power capture due to the variable speed operation.

For the power system with wind turbines integrated, once a severe fault occurs, the electromagnetic power of DFIG reduced rapidly, which increase the rotor speed and the

operation point of DFIG will move from the optimum point of speed-torque characteristic curve to the speed increase direction, and the mechanical torque will decrease during severe fault, accordingly. At the same time, the rotor current will have a sharp rise, to ensure the generator with a stable operation [6].
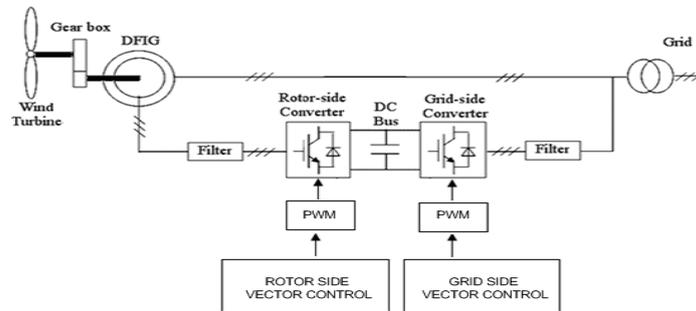


Figure 1. General Structure of Wind Power Generation System with DFIG

In Figure 1, the stator of the DFIG is directly connected to the grid, while two back to back PWM voltage source converters (VSCs) are inserted between the rotor and the grid to control the rotor and stator output power which is fed to the grid for the variable speed operation [7]. It is possible to control rotor current injection using VSCs to ensure effective operation in both sub and super synchronous modes. Decoupled control of active and reactive powers using the vector control is presented in [8] and current control methods for wind turbines using DFIG are presented in [9]. Both stator and rotor are able to supply the power, but the direction of active power flow through the rotor circuit is dependent on the wind speed and accordingly, the generator speed. Below the synchronous speed, the active power flows from the grid to the rotor side, and the RSC acts as a voltage source inverter while the GSC acts as a rectifier but above the synchronous speed, RSC acts as a rectifier and GSC acts as an inverter. The rotor VSC is controlled to limit the torque pulsation, and the grid VSC is controlled to limit the DC voltage ripple [10]. Two back to back voltage fed current regulated converters are connected to the rotor circuit. The firing pulses are given to the insulated gate bipolar transistors (IGBTs) devices using PWM techniques. The converters are linked to each other by means of DC-link capacitor. The main purpose of the GSC is to control the DC-link voltage and ensures the operation at unity power factor by making the reactive power drawn by the system from the utility grid equal to zero, while the RSC controls the active and reactive powers by controlling the $d-q$ components of the rotor currents.

## 2. d-q Model of Induction Generator (Park Model)

The $d-q$ axis representation of an induction generator is used for simulation, taking flux linkage as a basic variable. It is based on two axis representations commonly known as the "Park model" [11]. Here an equivalent 2-phase machine represents 3-phase machine, where $d^s - q^s$ correspond to the stator direct and quadrature axes, and $d^r - q^r$ correspond to the rotor direct and quadrature axes. A synchronously rotating $d-q$ reference frame is used with the direct $d-axis$ oriented along the stator flux position. In this way, decoupled control between the electrical torque and the rotor excitation current is obtained. The reference frame is rotating with the same speed as the stator voltage. While modeling the DFIG, the generator convention is used, indicating that, the currents are outputs and that power has a negative sign when fed into the grid.

### 2.1. Axes Transformation

The $d-q$ model requires that all the 3-phase variables have to be transformed to the 2-phase synchronously rotating frame [12]. A symmetrical 3-phase induction machine with

stationary axes $as, bs, cs$ separated by an angle $\dfrac{2\pi}{3}$ is considered. Here the 3-phase stationary reference frame's $d^s - q^s$ variables are transformed into the synchronously rotating reference frame $d^e - q^e$. Assume that the $d^s - q^s$ axes are oriented at $\theta$ angle. The voltages $v_{ds}^s$ and $v_{qs}^s$ can be resolved into $as, bs, cs$ components in a matrix form as:

$$\begin{bmatrix} v_{as} \\ v_{bs} \\ v_{cs} \end{bmatrix} = \begin{bmatrix} \cos\theta & \sin\theta & 1 \\ \cos(\theta-120°) & \sin(\theta-120°) & 1 \\ \cos(\theta+120°) & \sin(\theta+120°) & 1 \end{bmatrix} \begin{bmatrix} v_{qs}^s \\ v_{ds}^s \\ v_{0s}^s \end{bmatrix} \tag{1}$$

The corresponding inverse relation is:

$$\begin{bmatrix} v_{qs}^s \\ v_{ds}^s \\ v_{0s}^s \end{bmatrix} = \frac{2}{3}\begin{bmatrix} \cos\theta & \cos(\theta-120°) & \cos(\theta+120°) \\ \sin\theta & \sin(\theta-120°) & \sin(\theta+120°) \\ 0.5 & 0.5 & 0.5 \end{bmatrix} \begin{bmatrix} v_{as} \\ v_{bs} \\ v_{cs} \end{bmatrix} \tag{2}$$

Where $v_{os}^s$ is added as the zero sequence component. Equation (2) represents the transformation of 3-phase quantities into 2-phase $d - q$ quantities. It is more convenient to set $\theta = 0$, so that $q - axis$ is aligned with the $a - axis$ in this case. The sine components of $d$ and $q$ parameters will be replaced with cosine values, and vice versa if $d - axis$ coincides with $a - axis$. If the synchronously rotating $d - q$ axes rotate at a synchronous speed $\omega_e$ with respect to $d^s - q^s$ axes, then the voltages on the $d^s - q^s$ axes can be converted into $d - q$ a synchronously rotating frame as:

$$v_{qs} = v_{qs}^s \cos\theta_e - v_{ds}^s \sin\theta_e$$
$$v_{ds} = v_{qs}^s \sin\theta_e + v_{ds}^s \cos\theta_e \tag{3}$$

Resolving the rotating frame parameters into stationary frame:

$$v_{qs}^s = v_{qs} \cos\theta_e + v_{ds} \sin\theta_e$$
$$v_{ds}^s = -v_{qs} \sin\theta_e + v_{ds} \cos\theta_e \tag{4}$$

### 2.2. DFIG Model in Synchronous Rotating Reference Frame

For the modeling of DFIG in the synchronously rotating frame, we need to represent the 2-phase stator $(d^s - q^s)$ and rotor $(d^r - q^r)$ circuit variables in a synchronously rotating $(d - q)$ frame as shown below:
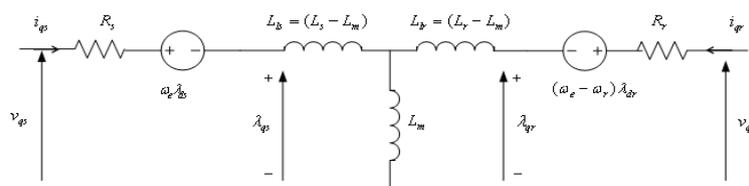


Figure 2. Dynamic d-q Equivalent Circuit of DFIG (q-axis circuit)
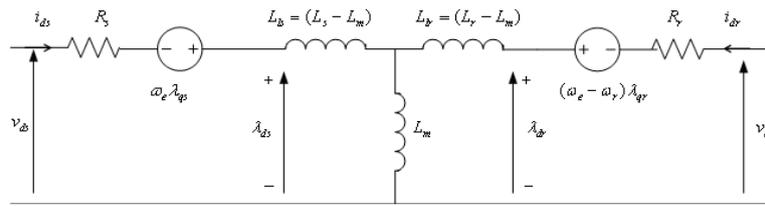
Figure 3. Dynamic d-q Equivalent Circuit of DFIG (d-axis circuit)

According to Kron's equation, the stator circuit equations are:

$$
v_{qs}^s = R_s i_{qs}^s + \frac{d}{dt}\lambda_{qs}^s
$$
$$
v_{ds}^s = R_s i_{ds}^s + \frac{d}{dt}\lambda_{ds}^s
$$

(5)

Where $\lambda_{qs}^s$ is the $q-axis$ stator flux linkage, and $\lambda_{ds}^s$ is the $d-axis$ stator flux linkage respectively. Convert equation (5) to the synchronous rotating frame:

$$
v_{qs} = R_s i_{qs} + \frac{d}{dt}\lambda_{qs} + \left(\omega_e \lambda_{ds}\right)
$$
$$
v_{ds} = R_s i_{ds} + \frac{d}{dt}\lambda_{ds} - \left(\omega_e \lambda_{qs}\right)
$$

(6)

When the angular speed $\omega_e$ is zero, the speed of $emf$ due to $d$ and $q$ axis is zero and the equation's changes to stationary form. If the rotor is blocked or not moving, i.e. $\omega_r = 0$, the machine rotor equations can be written in a similar way as the stator equations:

$$
v_{qr} = R_r i_{qr} + \frac{d}{dt}\lambda_{qr} + \left(\omega_e \lambda_{dr}\right)
$$
$$
v_{dr} = R_r i_{dr} + \frac{d}{dt}\lambda_{dr} - \left(\omega_e \lambda_{qr}\right)
$$

(7)

Let the rotor rotate at an angular speed $\omega_r$, then the $d-q$ axes fixed on the rotor fictitiously will move at a relative speed $(\omega_e - \omega_r)$ to the synchronously rotating frame. The $d-q$ frame rotor equations can be written by replacing $(\omega_e - \omega_r)$ in the place of $\omega_e$ as:

$$
v_{qr} = R_r i_{qr} + \frac{d}{dt}\lambda_{qr} + \left(\omega_e - \omega_r\right)\lambda_{dr}
$$
$$
v_{dr} = R_r i_{dr} + \frac{d}{dt}\lambda_{dr} - \left(\omega_e - \omega_r\right)\lambda_{qr}
$$

(8)

$$
\lambda_{qs} = L_{ls} i_{qs} + L_m (i_{qs} + i_{qr}) = L_s i_{qs} + L_m i_{qr}
$$

(9)

$$
\lambda_{ds} = L_{ls} i_{ds} + L_m (i_{ds} + i_{dr}) = L_s i_{ds} + L_m i_{dr}
$$

(10)

$$
\lambda_{qr} = L_{lr} i_{qr} + L_m (i_{qs} + i_{qr}) = L_r i_{qr} + L_m i_{qs}
$$

(11)

$$\lambda_{dr} = L_{lr}i_{dr} + L_m(i_{ds} + i_{dr}) = L_r i_{dr} + L_m i_{ds} \tag{12}$$

The torque expression can be written in terms of flux linkages and currents as:

$$T_e = \frac{3}{2}\frac{P}{2}(\lambda_{dr}i_{qr} - \lambda_{qr}i_{dr}) \tag{13}$$

## 3. Control Algorithm

Figure 4 and 5 below, shows the DFIG based WECS with the vector control. The rotor currents are used to control the stator active and reactive powers. The RSC controls the DFIG, while the GSC function is to maintain the DC link voltage constant. The vector control on DFIG is implemented in the two following steps.

### 3.1. GSC Control

The adopted vector control strategy must fulfill the two main objectives of the grid side converter. 1) Regulate DC bus voltage. 2) Control reactive power exchanged bidirectional between the rotor of the machine and the grid. Thus, by aligning the grid voltage vector with synchronous frame direct axis, its indirect axis component becomes null $(v_q = 0)$. The active and reactive powers are controlled independently using the vector control strategy. Since the amplitude of supply voltage is constant, the active and reactive powers are controlled by means of $i_d$ and $i_q$ respectively.

$$P_s = \frac{3}{2}(v_d i_d + v_q i_q) = \frac{3}{2}v_d i_d, (v_q = 0)$$
$$Q_s = \frac{3}{2}(v_q i_d - v_d i_q) = -\frac{3}{2}v_d i_q, (v_q = 0) \tag{14}$$

Where $i_d, i_q$ and $v_d$ are grid current and voltage respectively, as $(v_q = 0)$. Based on the sign of a non-zero slip ratio $s$, a part of DFIG's generated active power is interchanged with the grid through the rotor, which can deliver or absorb grid's power in super or sub-synchronous modes, respectively. Equation (14), states that active power and consequently, DC bus voltage can be controlled via $i_d$, whereas $i_q$ can control reactive power flow in the grid. This strategy is depicted in Figure 5. The control signals for the grid converters are:

$$v_d^* = \left(K_{p1} + \frac{K_{i1}}{s}\right)\left[i_d^* - i_d\right]$$
$$v_q^* = \left(K_{p1} + \frac{K_{i1}}{s}\right)\left[i_q^* - i_q\right] \tag{15}$$

Where $K_p$ is the proportional gain of the controller, and $K_i$ is the integral gain of the controller. The angular position of the grid voltage is detected using a phase locked loop (PLL), which has good quality in terms of stability and of transient response [13]. This locked angle will be used to transform system variables to the $d-q$ reference frame. The DC bus voltage is maintained constant via the outer voltage PI controller which processes the error between the reference and measured DC bus voltage and yields $i_d^*$, while $i_q^*$ is set to zero to compensate for reactive power at the grid side. The GSC provides needed magnetizing energy through the rotor for the DFIG. Finally, the measured grid currents $(i_d, i_q)$ and reference currents $(i_d^*, i_q^*)$ are compared then processed by inner current PI controllers, in order to generate appropriate signals for the GSC.
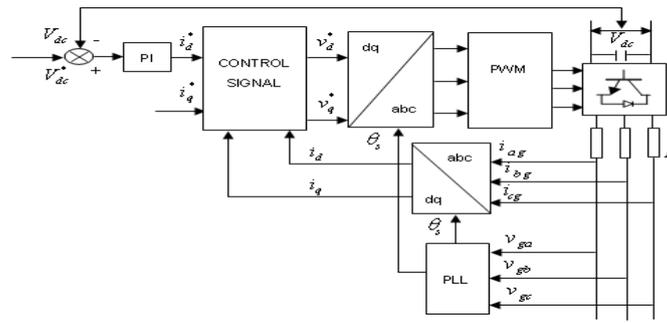
Figure 4. Vector Control Structure for GSC

### 3.2. RSC Control

The main purpose of the RSC is to maintain the rotor speed constant irrespective of the wind speed and also the control strategy has been implemented to control the active and reactive powers flow of the machine using the rotor current components. The active power flow is controlled through $i_{dr}$ and the reactive power flow is controlled through $i_{qr}$. To ensure unit power factor operation like GSC, the reactive power demand is also set to zero here. The standard voltage oriented vector control strategy is used for the RSC to implement control action. Here the real axis of the stator voltage is chosen as the $d$-axis. Since the stator is connected to the utility grid and the influence of stator resistance is small, the stator magnetizing current $i_m$ can be considered as constant. Under voltage orientation, the relationship between the torque and the $d - q$ axis voltages, currents and fluxes can be written with neglecting of leakage inductances. To maximize the turbine output power, DFIG must be controlled through the control of $i_{dr}$ and $i_{qr}$. To simplify the control and calculate $i_{dr}^*$, the stator flux component $\lambda_{ds}$ is set to zero.

$$
\begin{aligned}
\lambda_{ds} &= 0 \\
\lambda_{qs} &= (L_{ls} + L_m)i_{qs} + L_m i_{qr} = L_m i_m
\end{aligned}
\tag{16}
$$

The equations of rotor fluxes are:

$$
\begin{aligned}
\lambda_{qr} &= \frac{L_m}{L_s}\lambda_{qs} + \sigma L_r i_{qr} = \frac{L_m^2}{L_s}i_m + \sigma L_r i_{qr} \\
\lambda_{dr} &= \frac{L_m}{L_s}\lambda_{ds} + \sigma L_r i_{dr} = \sigma L_r i_{dr}
\end{aligned}
\tag{17}
$$

Where $\sigma = 1 - \dfrac{L_m^2}{L_s L_r}$

By substituting the values of $\lambda_{dr}$ and $\lambda_{qr}$ from equation (17) in equation (8), the rotor voltages are:

$$
\begin{aligned}
v_{dr} &= R_r i_{dr} + \sigma L_r \frac{d}{dt}i_{dr} - (\omega_e - \omega_r)\sigma L_r i_{qr} \\
v_{qr} &= R_r i_{qr} + \sigma L_r \frac{d}{dt}i_{qr} + (\omega_e - \omega_r)\sigma L_r i_{dr}
\end{aligned}
\tag{18}
$$

The reference value $v_{dr}^*$ and $v_{qr}^*$ can be found from Equation (18) as:

$$v_{dr}^* = v_{dr}' - (\omega_e - \omega_r)[L_r i_{qr} + L_m i_{qs}]$$
$$v_{qr}^* = v_{qr}' + (\omega_e - \omega_r)[L_r i_{dr} + L_m i_{ds}]$$

(19)

Where $v_{dr}'$ and $v_{qr}'$ are found from the current errors processing through standard PI controllers. The electromagnetic torque can be expressed as:

$$T_e = \frac{3}{2} P \frac{L_m}{L_s} \lambda_{qs} i_{dr}$$

(20)

The reference current $i_{dr}^*$ can be found either from the reference torque or from the speed errors through standard PI controllers. Similarly $i_{qr}^*$ can be found from the reactive power errors. The value of $i_{dr}^*$ can be found using Equation (20):

$$i_{dr}^* = \frac{T_e^* L_s}{\lambda_{qs} L_m}$$

(21)
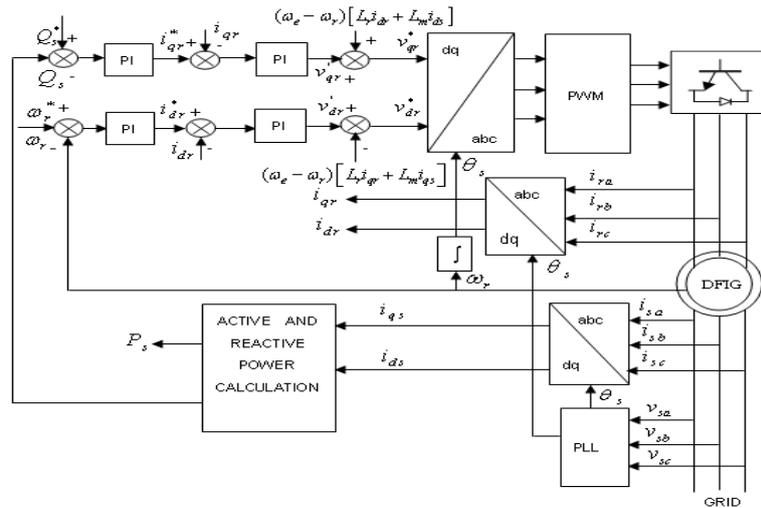


Figure 5. Vector Control Structure for RSC

## 4. Results and Discussion

The induction machine is simulated using MATLAB/SIMULINK environment. The performance of the DFIG system is analyzed under grid voltage fluctuations. The main objective of this Work is to study the performance analysis of the DFIG for a wind turbine application both during steady-state operation and transient operation (voltage fluctuations). The voltage fluctuations are made by lowering and raising the voltage values in the utility grid intentionally for simulation keeping in view of different grid disturbances.

## 4.1. Simulation under Balance Grid

DFIG characteristic's waveforms under steady-state conditions are shown in Figure 6. It is observed that the active and reactive powers supplied by the utility grid are decoupled and DC link voltage is maintained constant due to the control strategy made in the GSC.

(a) Stator voltage

(b) Stator current

(c) Rotor current

(d) Active power

(e) Reactive power

(f) DC link voltage

(g) Rotor speed
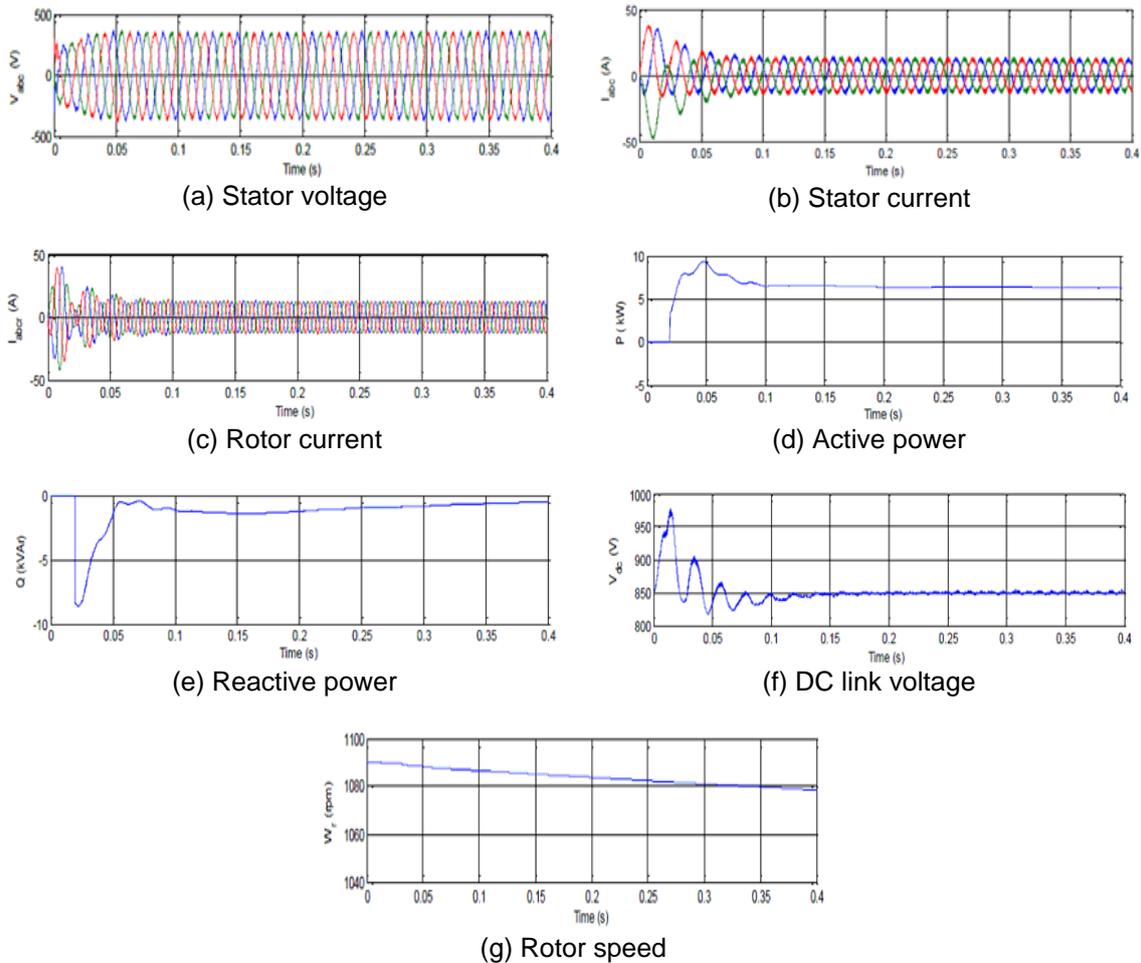
Figure 6. Simulation Results of the Grid under Balance Condition

## 4.2. Simulation under Change in Supply Frequency

Figure 7, shows how the system is collapsing with change in supply frequency. When the supply frequency changes from 50Hz rated to 48Hz, the system is not responding to the control strategy. It clearly indicates that the different control strategy needs to be employed to respond to the change in frequency. Since the machine frequency is at a rated value 50Hz, it is not responding to 48Hz, at that time the behavior of the machine is disturbing in nature.



(a) Stator voltage

(b) Stator current

(c) Rotor current

(d) Active power

(e) Reactive power                                    (f) DC link voltage
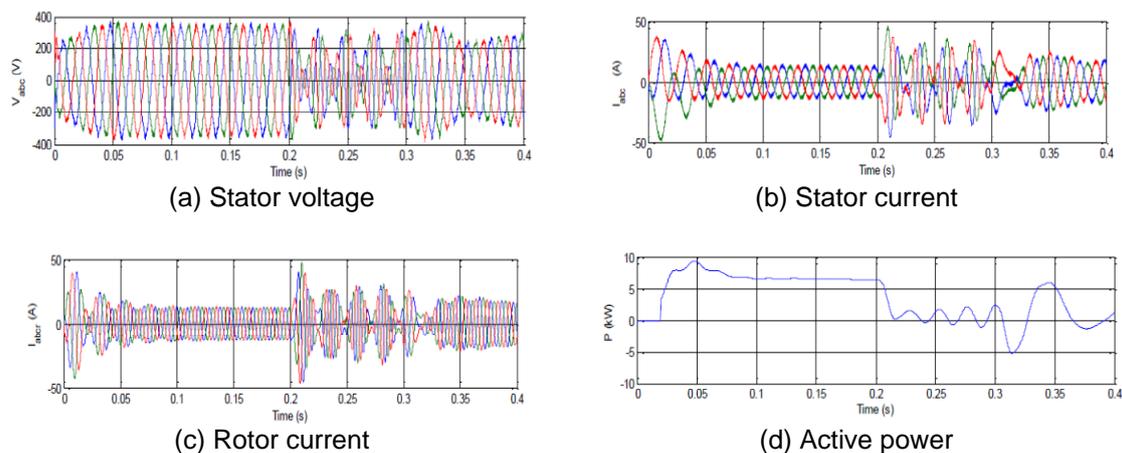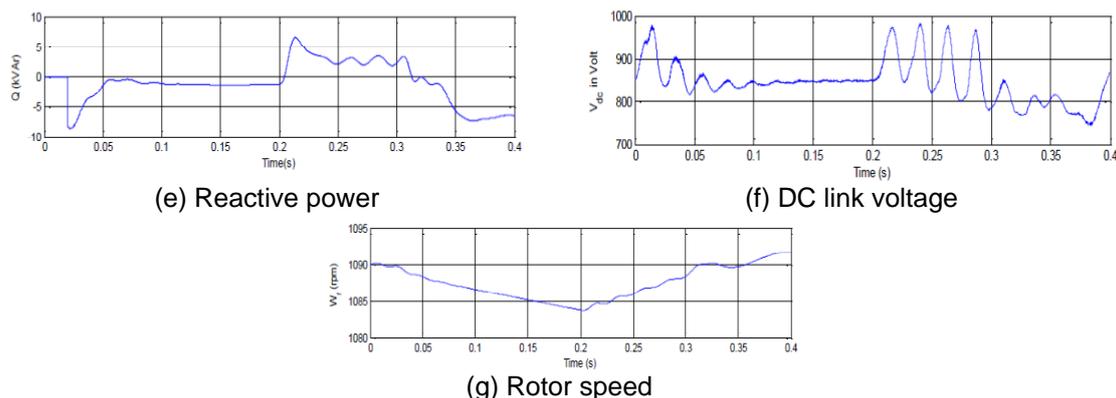


(g) Rotor speed
Figure 7. Simulation Results of the Grid under Change in Supply Frequency


## 5. Conclusion

The main objective of this Work is to study the performance analysis of the DFIG for a wind turbine application both during steady-state and transient operation. The modeling, control and simulation of DFIG coupled with a wind turbine has been carried out. The grid voltage oriented vector control is used for the GSC in order to maintain a constant DC bus voltage, while the stator voltage orientated vector control is adopted in the RSC to control the active and reactive powers. The DFIG system is simulated using MATLAB/SIMULINK environment. It is concluded that, the traditional voltage control technique which is used on both GSC as well as the RSC to analyze the performance of the DFIG system under grid voltage fluctuations is suitable under sudden change in grid voltage.

## References

[1]   Yingchao Zhang, Huijuan Liu, Haijiao Zhang, Xiang Zhao. Performance analysis of doubly excited brushless generator with outer rotor for wind power application. *TELKOMNIKA Indonesian Journal of Electrical Engineering.* 2010; 10(3): 471-476.
[2]   A Tapia, G Tapia, JX Ostolaza, JR Saenz. Modeling and control of a wind turbine driven doubly-fed induction generator. *IEEE Trans. Energy Conv.* 2003; 18(2): 149-204.
[3]   Y Liao, L Ran, G. Putrus, KS Smith. Evaluation of the effects of rotor harmonics in a doubly-fed induction generator with harmonic induced speed ripple. *IEEE Trans. Energy Conv.*, 2003; 18(4): 508-515.
[4]   A Mullane, M O'Malley. The inertial response of induction machine-based wind turbines. *IEEE Trans. Power Syst.*, 2005; 20(3): 1496-1503.
[5]   R Pena, JC Clare, GM Asher. *A doubly-fed induction generator using back-to-back PWM converters supplying an isolated load from a variable speed wind turbine.* IEE proc. On Electric Power Appl., 1996; 143(5): 331-338.
[6]   Hongwei Li, Haiying Dong, Shuaibing Li, Linxin Cao. Transient stability analysis of grid-connected wind turbines with time domain simulation. *TELKOMNIKA Indonesian Journal of Electrical Engineering.* 2014; 12(1): 29-37.
[7]   L Xu, Y Wang. Dynamic modeling and control of DFIG-based wind turbines under unbalanced network conditions. *IEEE Trans. On Power Systems.* 2007; 22(1): 314-323.
[8]   R Pena, JC Clare, GM Asher. *Doubly-fed induction generator using back-to-back PWM converters and its application to variable speed wind-energy generation.* Proc. Inst. Elect. Eng., Elect. Power Appl., 1996; 143(3): 231–241.
[9]   A Petersson, L Harnefors, T Thiringer. Evaluation of current control methods for wind turbines using doubly-fed induction machines. *IEEE Trans. Power Electron.,* 2005; 20(1): 227–235.
[10]  Z Yi, P Bauer, JA Ferreira, J Pierik. Operation of grid connected DFIG under unbalanced grid voltage condition. *IEEE Trans. on Energy Conversion.* 2009; 24(1): 240-246.
[11]  GR Slemon. Modelling induction machines for electric drives. *IEEE Transaction on Industry Application.* 1989; 25(6): 1126-1131.
[12]  S Muller, M Deicke, Rik W De Doncker. Doubly-fed induction generator systems for wind turbines. *IEEE Industry Applications Magazine.* 2002.
[13]  S Rahmani, K Al-Haddad, F Fnaiech. *A new control technique based on the instantaneous active current applied to shunt hybrid power filters.* IEEE 34th Annual Power Electronics Specialist Conference, PESC '03, 2003; 2: 808-813.