# Modelling and design of grid voltage oriented vector control scheme for DC railway recuperating system

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# **ABSTRACT**

The braking energy harvested by a railway vehicle can be restored to the utility grid with a power recuperating system. A grid connected voltage source inverter (VSI) is commonly used as a grid-feeding converter in the recuperating system. This paper proposes to integrate grid voltage oriented vector control (GVOVC) and third harmonic voltage injection pulse width modulation (THVI-PWM) technique for the VSI to ensure grid voltage and frequency synchronization. A simulation study is carried out to evaluate the feasibility of the proposed control and modulation schemes using MATLAB/Simulink. The results show that the proposed controller may reach steady-state operating mode within 7 ms by producing good quality AC voltages and currents waveforms. With the independent control of voltage quantities in dq reference frame, the regulation of active and reactive power could be realized.

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# 1. INTRODUCTION

A traditional DC railway power substation used to employ twelve-pulse rectifier transformer system as shown in Figure 1 [1]–[3]. This configuration aims to minimize the DC voltage ripples and eliminate the low order AC current harmonics [4]. However, as the traction rectifier is uncontrolled, power resistors must be activated to comsume braking energies harvested by a stopping train Figure 1(a). Literatures [5], [6], had proposed to introduce a DC power recuperating system to transmit the braking energy back to the utility grid. Some simulation studies have concluded that about 10% to 40% of energy saving could be achieved with a recuperating system [7], [8]. The recuperating system is connected in parallel with the existing twelve-pulse rectifier transformer system as shown in Figure 1(b). Three typical components namely voltage source inverter (VSI), passive filters, and recovery transformer must be employed. The regenerative DC power will first be inverted using a pulse-width-modulated VSI [9], [10]. The generated AC voltages may contain high frequency switching harmonics, thus, passive filters are demanded to purify the waveshapes [11], [12]. The recovery transformer is used to step up the AC voltage level to meet with the utility grid power ratings [13].

The VSI used in this application can be classified as a grid-feeding power converter [14], which mainly used to deliver regenerative power to an energized grid. Some established linear control schemes had been proposed for grid-feeding converters, which include proportional-integral (PI) [15], and adaptive controllers [16]. These controllers had been studied, compared and evaluated for distributed power generation [17], [18], AC microgrid [19] and traction power supply [20]. Since, the synchronization of the AC voltages at the point of coupling is the key to enabling power exchanged accurately, this paper proposes to integrate grid

voltage oriented vector control (GVOVC) for the VSI in a traction power substation. As the grid voltages are sampled and feedforward in the controller, a small variation in grid voltage will be corrected immediately using a simple PI-controller. In addition, to enhance the utilization of the DC-link voltage of the VSI, the third harmonic voltage injection pulse width modulation (THVI-PWM) technique will be applied [21]–[23]. In short, this paper will present the mathematical modelling of the GVOVC in section 2. Section 3 presents the PI-controller gain tunning and analysis. A system level simulation study of a DC power recuperating system with the proposed controller is presented in section 4. Lastly, section 5 concludes the research findings of this simulation study.

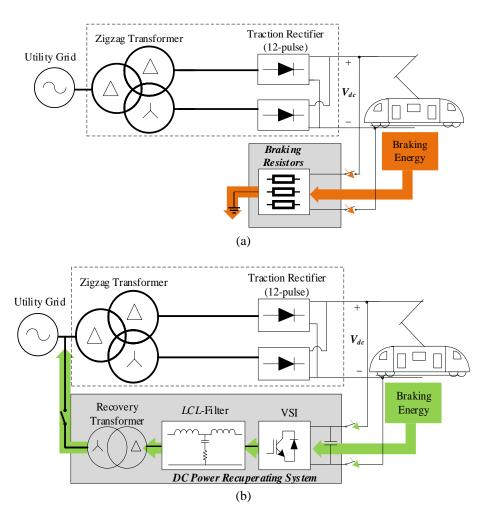


Figure 1. Braking energy management at DC power substation (a) DC power dissipation via braking resistor banks and (b) DC power regeneration inverter system

## 2. MODELLING OF RECUPERATING SYSTEM

An equivalent circuit of recuperating system is shown in Figure 2. When a train starts to break, it will act as an electrical generator. This may increase the DC-link voltage,  $V_{dc}$ , to it maximum level. Assume that the DC-link voltage is under controlled, the braking current,  $i_{br}$ , will flow into the DC terminal of the VSI. The VSI is used to process and deliver the braking energy back to the utility grid. As the VSI operates in high switching frequency, a three-phase LCL filter will be employed to mitigate the switching noises. The recovery transformer and utility grid shown in Figure 1(b) are modelled as wye-connected AC supplies,  $v_{xg}$ , with internal resistance,  $R_g$ , and reactance,  $L_g$ .

The following sub-section will present the mathematical modelling of LCL filter and GVOVC. It is highlighted that the mathematical modelling of DC link and VSI [15], the LCL filter design methodology [11], [12] and the THVI-PWM techniques [22], [23] will not be presented in this paper. All technical details can be referred from the above-mentioned literatures.

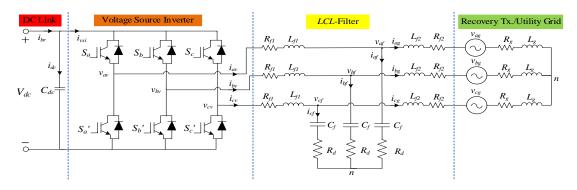


Figure 2. Equivalent circuit of recuperating system

### 2.1. Recuperating system modeling with LCL filter

As shown in Figure 2, the LCL filter is connected in wye configuration. Each phase of the LCL-filter consists of converter-side inductance,  $L_{fl}$ , with its internal resistance,  $R_{fl}$ , grid-side inductance,  $L_{f2}$ , with its internal resistance,  $R_{f2}$ , filter capacitance,  $C_f$ , and a damping resistor,  $R_d$ . Since the LCL-filter is designed with identical parameters for all the phases, the voltage drop across the filtering capacitors and damping resistor,  $v_{xf}$ , can be simplified as:

$$v_{xf} = R_d i_{xf} + \frac{1}{C_f} \int i_{xf} dt \tag{1}$$

the subscription x represents phases of a, b, and c. In addition, the currents being drain out by the filter capacitor can be derived using the classic Kichoff Current Law.

$$i_{xf} = i_{xv} - i_{xg} \tag{2}$$

Theoretically,  $i_{xf}$  should contains all the switching harmonics produced by the VSI, so that sinusoidal grid currents,  $i_{xg}$ , and voltages,  $v_{xg}$ , will be produced at the point of coupling. Consequently, a set of converter's voltage equations can be further elaborated by taking into account all the filters parameters.

$$v_{xv} = R_{f1}i_{xv} + L_{f1}\frac{di_{xv}}{dt} + R_{f2}i_{xg} + L_{f2}\frac{di_{xg}}{dt} + v_{xg} + R_gi_{xg} + L_g\frac{di_{xg}}{dt}$$
(3)

# 2.2. GVOVC

The control scheme proposes in this paper used to align the AC voltages with the orientation of grid voltage space-vector [24]. This control strategy can be easily being developed using the dq-components of a system model. Thus, a set of dynamic model equations must first be outlined. Referring to (3), the recovery transformer and utility grid are assumed ideal (by neglecting  $R_g$ , and  $L_g$ ), the three-phase voltage equations can then be transformed to  $\alpha\beta$  reference frame using two mathematical expressions as:

$$v_{\alpha v} = R_{f1}i_{\alpha v} + L_{f1}\frac{di_{\alpha v}}{dt} + R_{f2}i_{\alpha g} + L_{f2}\frac{di_{\alpha g}}{dt} + v_{\alpha g}$$

$$\tag{4}$$

$$v_{\beta \nu} = R_{f1} i_{\beta \nu} + L_{f1} \frac{di_{\beta \nu}}{dt} + R_{f2} i_{\beta g} + L_{f2} \frac{di_{\beta g}}{dt} + v_{\beta g}$$
(5)

In (4) and (5) can be presented using space vector notation:

$$\vec{v}_v^S = R_{f1}\vec{t}_v^S + L_{f1}\frac{d\vec{t}_v^S}{dt} + R_{f2}\vec{t}_g^S + L_{f2}\frac{d\vec{t}_g^S}{dt} + \vec{v}_g^S \tag{6}$$

where the superscript s of (6) means for electrical quantities referring to stationary reference frame. In order to transform all the stationary quantities into synchronous rotatory reference frame, (6) is multiplied with a constant  $e^{-j\theta}$ . The  $\theta$  refers to the synchronous rotating angular speed of the rotatory reference frame,  $\omega_r$ . Thus, it result as (7).

$$\vec{v}_{v}^{r} = R_{f1}\vec{t}_{v}^{r} + L_{f1}\frac{d\vec{t}_{v}^{r}}{dt} + R_{f2}\vec{t}_{g}^{r} + L_{f2}\frac{d\vec{t}_{g}^{r}}{dt} + \vec{v}_{g}^{r} + j\omega_{r}L_{f1}\vec{t}_{v}^{r} + j\omega_{r}L_{f2}\vec{t}_{g}^{r}$$

$$\tag{7}$$

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The superscript r of (7) means for electrical quantities referring to rotatory reference frame. By decomposing (7) into dq components, the vector orientation of the VSI are formulated:

$$v_{dv} = R_{f1}i_{dv} + L_{f1}\frac{di_{dv}}{dt} + R_{f2}i_{dg} + L_{f2}\frac{di_{dg}}{dt} + v_{dg} - \omega_r L_{f1}i_{qv} - \omega_r L_{f2}i_{qg}$$
(8)

$$v_{qv} = R_{f1}i_{qv} + L_{f1}\frac{di_{qv}}{dt} + R_{f2}i_{qg} + L_{f2}\frac{di_{qg}}{dt} + v_{qg} + \omega_r L_{f1}i_{dv} + \omega_r L_{f2}i_{dg}$$

$$\tag{9}$$

the dq-voltage vectors given in (8) and (9) are properly align with grid voltage space vector as:

$$v_{dg} = |\vec{v}_g| \tag{10}$$

$$v_{aa} = 0 ag{11}$$

the synchronous rotating angular speed,  $\omega_r$ , is set equal to the angular speed of the grid voltage,  $\omega$ . Hence, (8) and (9) can be simplified as (12), (13).

$$v_{dv} = R_{f1}i_{dv} + L_{f1}\frac{di_{dv}}{dt} + R_{f2}i_{dg} + L_{f2}\frac{di_{dg}}{dt} + v_{dg} - \omega L_{f1}i_{qv} - \omega L_{f2}i_{qg}$$
 (12)

$$v_{qv} = R_{f1}i_{qv} + L_{f1}\frac{di_{qv}}{dt} + R_{f2}i_{qg} + L_{f2}\frac{di_{qg}}{dt} + \omega L_{f1}i_{dv} + \omega L_{f2}i_{dg}$$
(13)

This paper adopts the decoupled current compensation and voltage feed-forward compensation techniques to simplify (12) and (13). In addition, the fundamental component of the converter-side current,  $i_{xy}$ , and grid-side current,  $i_{xy}$ , are assumed equivalent. Hence, the dynamic models of the recuperating system can be finalized as:

$$v_{dv} = R_{f1}i_{dg} + L_{f1}\frac{di_{dg}}{dt} + R_{f2}i_{dg} + L_{f2}\frac{di_{dg}}{dt}$$
(14)

$$v_{qv} = R_{f1}i_{qg} + L_{f1}\frac{di_{qg}}{dt} + R_{f2}i_{qg} + L_{f2}\frac{di_{qg}}{dt}$$
(15)

based on the developed dynamic model, a pair of PI-controller is introduced to regulate the grid current as shown in Figure 3, where Figures 3(a) and 3(b) present the respective current regulators in *d*-axis and *q*-axis. The PI-controller is employed with two main controlled objectives. The controller must ensure zero steady state error and offer good dynamic response. The open-loop and close-loop transfer functions.

$$G_{OL}(s) = \left(K_P + \frac{K_i}{s}\right) \cdot \left(\frac{1}{s(L_{f_1} + L_{f_2}) + (R_{f_1} + R_{f_2})}\right) \tag{16}$$

$$G_{CL}(s) = \frac{sK_P + K_i}{s^2(L_{f_1} + L_{f_2}) + s(R_{f_1} + R_{f_2} + K_P) + K_i}$$
(17)

The controller gain,  $K_p$  and  $K_i$  can be determined by equaling the denominators of (17) with the generalized transfer function of a second-order system. These gains can then be formulated as:

$$K_i = (L_{f1} + L_{f2})\omega_n^2 \tag{18}$$

$$K_p = 2\zeta\omega_n(L_{f1} + L_{f2}) - (R_{f1} + R_{f2})$$
(19)

where  $\zeta$  and  $\omega_n$  represent the damping ratio and natural frequency of a second order system.

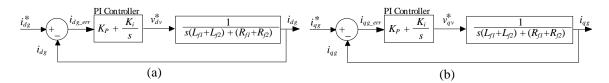


Figure 3. Current regulators with PI-controller (a)  $i_{dg}$  and (b)  $i_{qg}$ 

## 3. CONTROLLER GAIN TUNNING AND ANALYSIS

The PI controller gains are tuned based on a set of LCL-filter parameters given in Table 1 [11]. This paper proposes to design the PI controller with two equal real poles ( $\zeta$ =1). The natural frequency,  $\omega_n$ , is proposed to be set at one order of magnitude smaller than the VSI switching frequency. The  $K_i$  and  $K_p$  are calculated as 287.80 and 0.67. The PI controller is then analyzed in the frequency and time domains as shown in Figure 4. Figure 4(a) shows the Bode plots of (16) and (17) with the calculated gains. The cut-off frequency,  $f_c$ , is measured at 275 Hz. The phase margin is estimated as 77°. Since the phase margin is greater than 60°, a stable dynamic response is being expected. The close-loop bandwidth is assumed equal to the cut-off frequency of the open-loop transfer function. In summary, the close-loop bandwidth is fall under the permitted range of the LCL-filter design [11]. Figure 4(b) shows a step-response of the current regulator. When the input change is detected, the PI controller shows a fast transient response with 0.88 ms rise time is measured. An overshoot of 12.7% is detected at 2.37 ms. Finally, the controller reaches the settling time of 6.3 ms. The final value of the step-response is shown at the amplitude of one, which confirmed the objective of zero steady state error is met.

Table 1. System parameters

Voltage source inverter		LCL-filter	
DC-link voltage, $V_{dc}$	900 V	Converter side inductor, $L_{fI}$	300 μΗ
DC-link capacitor, $C_{dc}$ ,	1 mF	Converter side inductor internal resistance, $R_{fI}$	$7.50~\mathrm{m}\Omega$
PWM switching frequency, $f_{sw}$	1350 Hz	Grid side inductor, $L_{f2}$	100 μH
Amplitude modulation index, $m_a$	1.15	Grid side inductor internal resistance, $R_{f2}$	$2.50~\mathrm{m}\Omega$
Rated nominal AC voltage, $v_{ab}$	585 V	Filter capacitor, $C_f$	1.00 mF
Rated fundmental frequency, $f_g$	50 Hz	Damping resistor, $R_d$	$0.05 \Omega$

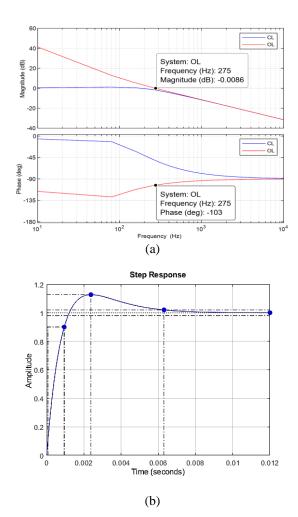


Figure 4. PI controller analysis (a) bode plots of open loop (OL) and close loop (CL) and (b) step response of the current controller

### 4. SYSTEM LEVEL SIMULATION AND ANALYSIS

The proposed vector control strategy is evaluated via MATLAB/Simulink simulation software. Figure 5 shows the simulation model built for the proposed system. The DC power recuperating system is modelled as shown in Figure 5(a) with the VSI power circuit is presented in Figure 5(b). All the simulation parameters are configured as listed in Table 1. The GVOVC and THVI-PWM scheme are depicted in Figure 5(c). Three-phase balance grid voltages rated at 585 V, 50 Hz are used as the reference voltages for the GVOVC.

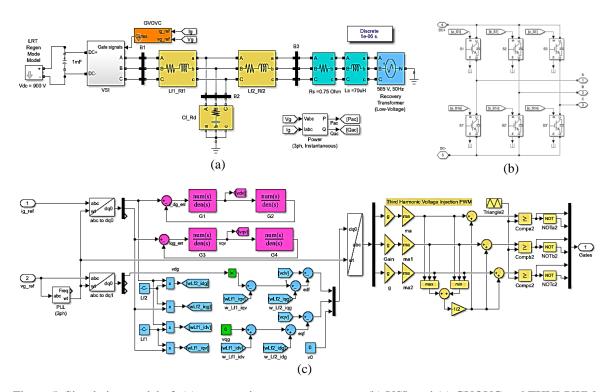


Figure 5. Simulation model of; (a) recuperating converter system, (b) VSI, and (c) GVOVC and THVI-PWM

The angular speed of the grid is extracted using the phase lock loop module. This angular speed is then used as input to abc-dq transformation blocks. The dq-currents controller blocks (magenta blocks) consist of the PI-controller (G1 and G3) and the dynamic model of the VSI (G2 and G4). The transfer function G1–G4 are identical to the block shown in Figure 3. The dq-voltages of the VSI (light-blue color blocks) can then be estimated using (15) and (16). The estimated dq-reference voltages are inversely transformed back to abc-domain before modulating. The estimated abc- reference voltages are first being normalized and then set to the desired amplitude modulation index,  $m_a$ . In this simulation, the  $m_a$  is fixed at the ratio of 1.15. The THVI-PWM model is developed based on the formulation given in [23]. The modulating waves are then compared with a 1350 Hz triangular carrier wave to generate a series of gate pulses for the VSI.

The simulation model is programmed to initially run with the conventional sinusoidal pulse width modulated inverter (SPWM) scheme [11]. The proposed GVOVC scheme is activated when the simulation time reaches 0.15s. Figure 6 shows the simulation results of three-phase voltage and current waveforms captured at buses B1, B2, and B3 (Figure 5 (a)). As shown in Figure 6(a), the VSI produces badly distorted AC voltages and currents at bus B1. The distortion is mainly due to the switching frequency set in kilo Hertz range. By using the fast fourier transform (FFT) analyzer of the simulation software, both voltages and currents total harmonic distortion (THD) are measured at 68.75% and 7.25%. The designated LCL-filter had mitigated the switching distortion. Figure 6(b) presents the voltages and currents at bus B2, it is noted that the high switching ripple currents are being drained out by the filter capacitor effectively. As a result, good quality of grid voltages and currents are captured at bus B3, as shown in Figure 6(c). The GVOVC scheme is enable upon reaching the simulation time of 0.15 s. The VSI encountered light fluctuation from 0.15 s until 0.157 s. This has proven that the controller gains are tunned correctly to ensure the system reaching its steady state witin 7 ms. The amplitude of the grid voltages is amplified to about 490 V (peak) after entering steady state. This is mainly due to effect of THVI-PWM.

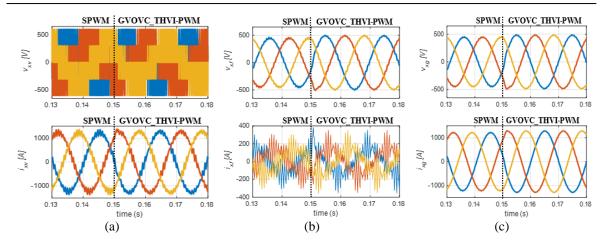


Figure 6. Simulation results of voltage and current waveforms measured at; (a) B1 (converter-side), (b) B2 (filter capacitor in series with damping resistance), and (c) B3 (grid-side)

Figure 7 shows the harmanic spectrums for grid voltages and current at bus B3, before and after the activation of GVOVC with THVI-PWM. The voltage and current harmonic indexes are recorded less than 2%. With SPWM control scheme, the most significant harmonics components are captured around the frequency modulation index and its multiples as shown in Figure 7(a). Whereas, with the proposed control scheme, some lower order harmonics (3 < h < 19) are captured in Figure 7(b). This is mainly due to the effect of injecting the third harmonic voltage into the modulating wave. Fortunately, all individual harmonics components percentage are kept lower than the IEEE standard [25].

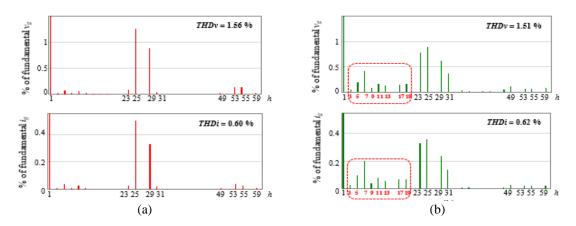


Figure 7. Harmonic spectrum of grid voltages captured at bus *B3* (Figure 8 (c)) (a) SPWM and (b) GVOVC\_THVI-PWM

Figure 8 shows the dq-axes of grid voltages and currents results which are used to further analyse the instantaneous active and reactive power variations at bus B3. Prior to 0.15 s, the recuperating converter is being controlled using SPWM method. As shown in Figure 8(a), the dq-components of the grid voltages yields an average of 420 V and 150 V. When GVOVC and THVI-PWM scheme are enable,  $v_{dg}$  is increased to an average of 482 V. This is mainly due to the effect of amplitude modulation index had been set to 1.15, which resulting of 14.76% of grid voltage (d-component) amplification. On the other hand, with the reference  $v_{qg}$  is fixed to 0 V, the q-component of grid voltage is captured closed to 0 V once the system operates in steady state mode. The dq-grid currents show similar changes as if the grid voltages, the respective waveforms are presented in Figure 8(b). Lastly, Figure 8(c) presents the instantaneous power delivered to the utility grid. The proposed control and modulation scheme manage to increase approximately 16% of the active power,  $P_{ac}$ , to the utility grid. Besides, the lagging power factor had been corrected after enabling the proposed control scheme. When the system is stable, the simulation result as shown in Figure 8(c) shows a leading power factor, which extends future works in the area of reactive power exchange with the utility grid [8].

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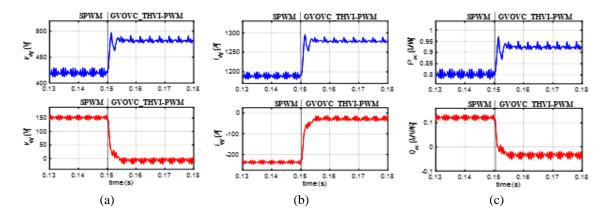


Figure 8. Instantaneous waveforms of; (a) dq-voltages, (b) dq-currents, and (c) active and reactive power

### 5. CONCLUSION

This paper presents a simulation study of a recuperating converter control scheme used in a DC traction power substation. With the objective to feed-in the regerative power harvested by a train to an energized grid, the GVOVC with THVI-PWM scheme had been proposed. The mathematical modeling and design of the controller had been presented. The feasibility of the proposed controller had been validated via simulation analysis. The simulation study shows that good quality of three-phase AC voltages and currents are produced at the point of common coupling. The voltage and current harmonics distortion indexes are recorded at 1.51% and 0.62%. The proposed THVI-PWM technique offers further adjustment of the AC voltage amplitude to not more than 15%. Since the proposed controller permits independent control of the voltage quantities in dq reference frame, the regulation of active and reactive powers could be realized.

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