

Robust operation of microgrid energy system under uncertainties and demand response program

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Article Info

Article history:

Received Jun 1, 2019

Revised Sep 2, 2019

Accepted Sep 16, 2019

Keywords:

Demand response

Microgrid energy system

Robust framework

Uncertainty

ABSTRACT

Microgrid energy systems are one of suitable solutions to the available problems in power systems such as energy losses, and resiliency issues. Local generation by these energy systems can reduce the role of the upstream network, which is a challenge in risky conditions. Also, uncertain behavior of electricity consumers and generating units can make the optimization problems sophisticated. So, uncertainty modeling seems to be necessary. In this paper, in order to model the uncertainty of generation of photovoltaic systems, a scenario-based model is used, while the robust optimization method is used to study the uncertainty of load. Moreover, the stochastic scheduling is performed to model the uncertain nature of renewable generation units. Time-of-use rates of demand response program (DRP) is also utilized to improve the system economic performance in different operating conditions. Studied problem is modeled using a mixed-integer linear programming (MILP). The general algebraic modeling system (GAMS) package is used to solve the proposed problem. A sample microgrid is studied and the results with DRP and without DRP are compared. It is shown that same robustness is achieved with a lower increase in the operation cost using DRP.

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1. INTRODUCTION

Microgrid is a scaled-down power system that can benefit from local generation units to supply the energy demands. Optimal operation of microgrid is challenged by various factors including uncertainties, which can threaten the normal operation of microgrid energy systems [1-5]. Therefore, the robust operation of microgrid should be investigated.

A brief summary of studied papers about microgrid operations is presented in the following: Implementing a two-stage adaptive robust optimization-based collaborative operation, the economic and collaborative operation of multi-microgrids has been evaluated as a unit commitment problem [6]. The total operation cost of multi-microgrids was reduced subject to uncertainty of solar power systems. In [7], optimal design of a hybrid electric power generation system for isolated zones has been investigated and the total cost of power generation was minimized using particle swarm optimization. With the aim of calculating the sharing power of distributed energy resources with uncertainty and nonlinear load, the robust multi-objective control method has been employed in [8]. Optimal design and scheduling of power dispatch in a microgrid has been achieved using a sliding time window optimization modeling considering the unbalance of

biomass-integrated renewable energy and energy storage [9]. In order to optimize the performance of energy management in the presence of renewable energy resources, a multi-objective generation scheduling model was developed under demand response program [10]. By implementing demand response program (DRP), the optimum components sizes in a microgrid was evaluated to decrease the cost of energy in [11]. With the aim of solving microgrids operation problem in the presence of electric vehicles, the robust optimization has been implemented to reduce the operation cost of microgrid in [12]. In order to improve the characteristics of electric power distribution systems, conventional power generators and various types of renewable energy resources and electric vehicles have been used to improve the voltage profile and decrease the cost of power losses and energy [13]. Robust technique has been employed to control an isolated microgrid in the presence of high penetration of renewable energy sources [14]. Risk-based optimal operation of microgrid system is evaluated using robust optimization method in the presence of electric vehicles in [15]. Distribution system with multi-microgrid is optimally scheduled under uncertainty with robust optimization method in [16]. Similarly, robust optimization approach is used in [17] to solve uncertainty-based optimal energy transactions problem in multi-microgrid systems. In [18], a brief summary of studied papers about operation of photovoltaic based microgrids has been presented to investigate various combination methods of energy storage and electric vehicles with other energy resources. It is noteworthy that optimal scheduling of microgrid systems have been studied under different types of demand response programs in several research papers [19-21] which represents essential role of these programs in improvement of optimization results.

In this paper, the robust operation of microgrid energy system subject to uncertainties of load and renewable generation unit is studied considering the time-of-use rates of demand response program. In order to model the uncertainty of generation of photovoltaic systems, a scenario-based model is used, while the robust optimization method is used to study the uncertainty of load. Combination of robust optimization method, which is a powerful strategy providing uncertain modeling method, with stochastic programming to model uncertainty ensures optimal reaction of operator against possible negative consequences of uncertainty. Furthermore, demand response can enhance effectiveness of these methods in uncertain handling.

It should be noted that the level of robustness depends on the policies taken by the operator of microgrids. According to each desired level of robustness, operation cost of microgrid is increased. Therefore, robust optimization method can be used as a powerful uncertainty modelling tool to provide operation strategies for energy systems against different uncertainties. The studied problem is schematically illustrated in Figure 1.

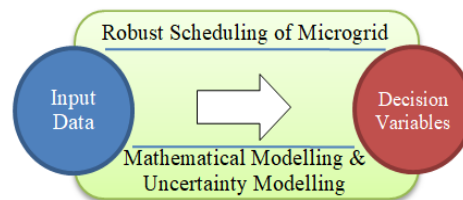


Figure 1. Studied problem

1.1. Paper Structure

The remaining parts of the paper are organized as: Robust operation of microgrid energy system is formulated in Section 2. The case studies and results of the proposed robust optimization scheme are presented in Section 3. Finally, the paper is concluded in Section 4.

2. PROBLEM FORMULATION

In this section, robust operation of microgrid energy system with load uncertainty is modelled, considering the demand response program.

2.1. Objective Function

As the objective function, the cost of the purchased power from the upstream power grid (1) should be minimized.

$$\text{Min Cost} = \sum_{t=1}^T \lambda_t \times P_t^{\text{net}} \quad (1)$$

In (1), $Cost$ is the total operation cost of the microgrid; λ_t and P_t^{net} are the price and the amount of the power purchased from the upstream network.

2.2. Constrains

The power balance is formulated as

$$P_t^{Load,DRP} + P_t^{Ess,ch} = P_t^{PV} + P_t^{net} + P_t^{Ess,dis} \tag{2}$$

where $P_t^{Load,DRP}$ is the load with DRP; $P_t^{Ess,ch}$ is the charging power of the battery energy storage systems (ESS); P_t^{PV} is the power generated by the solar system; P_t^{net} is the power from the upstream network; and $P_t^{Ess,dis}$ is the discharging power of battery ESS.

The active power generated by the photovoltaic system is expressed as

$$P_t^{PV} = A \times R_t \times \eta_{PV} \tag{3}$$

where A is the installation area; R_t is the solar radiation; and η_{PV} is the PV output efficiency.

The power imported from the upstream network is limited as

$$P_{min}^{net} \leq P_t^{net} \leq P_{max}^{net} \tag{4}$$

where P_{max}^{net} and P_{min}^{net} are the maximum and minimum allowable powers.

The stored energy in battery ESS depends on the state of charge of the battery at previous time step and the charging/discharging power at current time interval. The available energy is

$$W_t^{Ess} = W_{t-1}^{Ess} + P_t^{Ess,ch} \times \eta^{ch} - P_t^{Ess,dis} / \eta^{dis} \tag{5}$$

where W_t^{Ess} is the stored energy level; $P_t^{Ess,ch}$ and $P_t^{Ess,dis}$ are the charging and discharging powers; and η^{ch} and η^{dis} are the charging and discharging efficiencies of the battery ESS, respectively.

The stored energy of the battery ESS is limited as

$$W_{Min}^{Ess} \leq W_t^{Ess} \leq W_{Max}^{Ess} \tag{6}$$

where W_{Max}^{Ess} and W_{Min}^{Ess} are maximum and minimum energy of battery ESS, respectively.

The charging and discharging powers of battery ESS are limited by (7)-(8).

$$\alpha_t^{dis} \times P_{min}^{Ess,dis} \leq P_t^{Ess,dis} \leq \alpha_t^{dis} \times P_{max}^{Ess,dis} \tag{7}$$

$$\alpha_t^{ch} \times P_{min}^{Ess,ch} \leq P_t^{Ess,ch} \leq \alpha_t^{ch} \times P_{max}^{Ess,ch} \tag{8}$$

where $P_{min}^{Ess,dis}$, $P_{max}^{Ess,dis}$, $P_{min}^{Ess,ch}$ and $P_{max}^{Ess,ch}$ are the minimum and maximum discharge and charging power limits of the battery ESS, respectively.

In (7) and (8), α_t^{dis} and α_t^{ch} are binary variables of discharging and charging of the battery ESS, which are limited as (9) since the battery ESS is either in charging or discharging.

$$\alpha_t^{ch} + \alpha_t^{dis} \leq 1 \tag{9}$$

The demand response program with the time-of-use method is modeled based on (10)-(13).

$$P_t^{Load,DRP} = P_t^{Load} + p_t^{shup} - p_t^{shdo} \tag{10}$$

where P_t^{Load} is the base demand, P_t^{shup} and P_t^{shdo} are the increased and decreased values of the base load in DRP, which are limited as (11) and (12), respectively.

$$0 \leq P_t^{shup} \leq LPF^{shup} \times P_t^{Load} \times I_t^{shup} \quad (11)$$

$$0 \leq P_t^{shdo} \leq LPF^{shdo} \times P_t^{Load} \times I_t^{shdo} \quad (12)$$

where LPF^{shup} and LPF^{shdo} are the limitation of the increase and decrease in load, and I_t^{shup} and I_t^{shdo} are binary variables to represent the increase of load in DRP.

The increased and decreased powers for DRP are balanced as:

$$\sum_t^T P_t^{shup} = \sum_t^T P_t^{shdo} \quad (13)$$

where T is the scheduling horizon.

The robust optimization method and the different uncertainties are modelled as (14)-(20) to formulate the robust operation of microgrid energy system [22-23]. As shown, after implementing robust optimization, deviation of uncertain parameter are added to the objective function (14). (15) refers to the constants of base problem. As shown in (16)-(20) are used to model deviation of uncertain parameter. Then, by applying formulations presented in [22-23], the studied problem under uncertainty can be expressed as:

$$Min \left(\sum_{t=1}^T \lambda_t \times P_t^{net} + z_0 \Gamma_0 + \sum_{t=1}^T q_{ot} \right) \quad (14)$$

s.t.

$$(2)-(13) \quad (15)$$

$$z_0 + q_{ot} \geq d_t y_t, \quad t = 1, \dots, T \quad (16)$$

$$q_{ot} \geq 0, \quad t = 1, \dots, T \quad (17)$$

$$y_t \geq 0, \quad t = 1, \dots, T \quad (18)$$

$$z_0 \geq 0 \quad (19)$$

$$y_t \geq P_t^{net} \quad (20)$$

It should be noted that z_0 and q_{ot} are dual variables of optimization problem. Dual variables are formed when dual form of an optimization problem is written using duality theorem. Also, Γ_0 is an integer defined to determine either uncertainty is considered or not. When uncertainty is considered, $\Gamma_0 = 1$ and otherwise $\Gamma_0 = 0$.

3. NUMERICAL STUDIES

Robust operation of microgrid energy system is evaluated considering the uncertainties and the DRP in this section. The input data used for simulations is presented in Subsection 3.1. The proposed robust optimization problem is solved and the results without and with DRP are given in Subsections 3.2 and 3.3 in the following, respectively. The studied test system is captured in Figure 2.

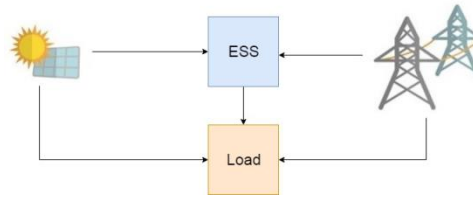


Figure 2. Test systems

3.1. Input Data

The hourly solar radiation is illustrated in Figure 3 [24]. The price of the power imported from the upstream network is illustrated in Figure 4 [25]. The energy demand of microgrid in different levels is illustrated in Figure 5 [25]. As illustrated, load is assumed to fluctuate between 0.7 and 1.3 of its base value. The technical data of battery ESS is provided in Table 1. It should be noted large number of scenarios are generated and then reduced for renewable units and the expected values are calculated to be used in the optimization process.

Table 1. ESS Characteristics

Parameter	W_{min}^{ess}	W_{max}^{ess}	p_{min}^{ch}	p_{max}^{ch}	p_{min}^{dis}	p_{max}^{dis}	η_t^{ch}	η_t^{dis}
Value	0 kWh	7.5 kWh	0 kWh	3 kWh	0 kWh	3 kWh	95%	95%

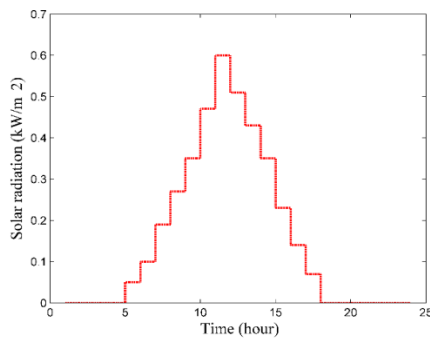


Figure 3. Solar radiation

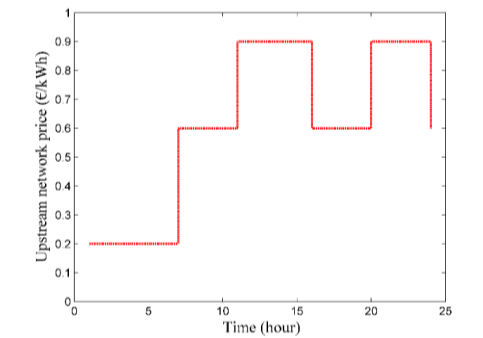


Figure 4. Upstream network price

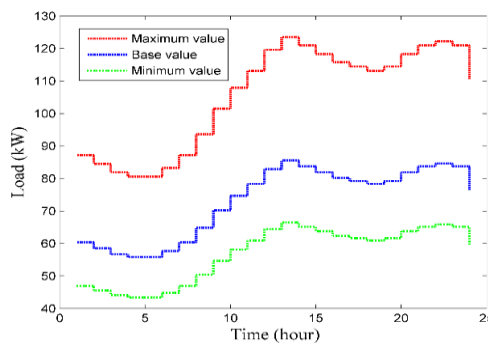


Figure 5. Upstream network price

3.2. Results of Robust Energy Management without DRP

In this section, results of the robust and stochastic scheduling of the microgrid energy system are presented. Calculating the expected values of solar radiation in each hour, the robust optimization method is applied to provide strategy for different levels of load uncertainty without DRP. The load is assumed to

fluctuate between 0.7 and 1.3 of its base value. It should be noted that these values are selected random and can change based on the expectations of operator. Therefore, the most possible value of the load which is threatening the usual operation of the microgrid is 1.3 times the base value. Accordingly, the simulations are performed for several steps and the results are obtained. The total operation costs of microgrid against different levels of load uncertainty are presented in Table 2.

Table 2. Robust Cost without DRP

Load uncertainty level (of base value)	0.7	0.8	0.9	1.0	1.1	1.2	1.3
Operation cost of microgrid (€)	829.779	956.269	1082.759	1209.249	1335.739	1462.229	1588.719

According to the results presented in Table 2, in order to become robust against 30% variation in load, the operation cost of microgrid energy system should be increased by 31.38, to guarantee its normal operation against 30% additional load. On the other hand, when the load value is reduced to 70% of its base value, the operator of microgrid energy system can gain an economic profit up to 379.47 €. In fact, due to reduction of load value up to 30 %, daily operation cost of microgrid energy system will decrease up to 31.38 %. Therefore, by employing each one of the provided strategies by robust optimization method, the energy system can be resilient against different levels of load uncertainties. As a result, the imported power from the upstream network in different load uncertainty levels without DRP is obtained which is illustrated in Figure 6.

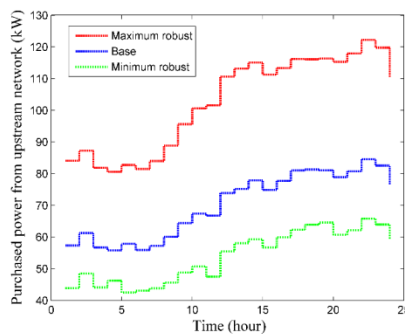


Figure 6. Upstream network power without DRP

In detail, when the uncertainty of load is not considered, the total power provided by the upstream network is 1881.753 kW. When the load is in maximum level, total imported power from the upstream network is 2466.453 kW. On the other hand, when the load is minimum, the total imported power is 1297.053 kW.

3.3. Results of Robust Energy Management with DRP

Applying the time-of-use program of the DRP, the total operation costs against different levels of load uncertainty are obtained and presented in Table 3. It can be seen that the maximum value of load uncertainty can be handled by 5.05 % less increase in operation cost under DRP which is economically beneficial for the microgrid operator. Moreover, by reduction of load value to 70% of its base value, the microgrid energy system can benefit 9.68% more reduction in cost utilizing the DRP. The power imported from the upstream network in this case is illustrated in Figure 7. As shown, the load is shifted from the peak periods to off-peak ones, and thus the power is purchased economically optimal to reduce the total operation cost as much as possible.

Table 3. Robust Cost with DRP

Load uncertainty level (of base value)	0.7	0.8	0.9	1.0	1.1	1.2	1.3
Operation cost of microgrid (€)	749.399	875.889	1002.379	1128.869	1255.359	1381.849	1508.339

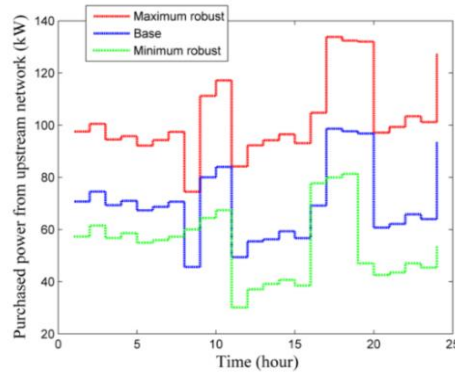


Figure 7. Upstream network power with robust scheduling and DRP

3.4. Comparisons

To approve the positive role of DRP on the uncertainty-based performance of the microgrid, simulation results are presented in Table 4, with and without taking the DRP into consideration.

Table 4. Comparison Results

Load uncertainty level (fraction of base value)	Operation cost of microgrid (€)	
	Without DRP	With DRP
0.7	829.779	749.399
0.8	956.269	875.889
0.9	1082.759	1002.379
1	1209.249	1128.869
1.1	1335.739	1255.359
1.2	1462.229	1381.849
1.3	1588.719	1508.339

4. CONCLUSION

In this paper, robust and stochastic operation of microgrid energy system is studied considering the uncertainties in load and renewable power of PV system. A large number of scenarios are generated first and then reduced using the fast-forward scenario reduction algorithm. Consequently, the expected values of uncertain parameters related to renewable power of PV system are calculated. The robust scheduling of the microgrid energy management is formulated as a mixed-integer linear programming (MILP) optimization problem. According to the results, robust scheduling of microgrid energy system in the worst condition is obtained against 30% higher load level compared to the base load, while daily operation cost of microgrid is increased by 31.38% without DRP. However, the same robustness can be achieved with a lower increase in the operation cost using the DRP, which is more economically beneficial for the microgrid operator. The proposed robust optimization method can be used as a powerful uncertainty modelling tool to provide operation strategies for energy systems against different uncertainties.

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