

## Economic power dispatch for an interconnected power system based on reliability indices

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### ABSTRACT

Reliability indices are always one of the most important factors in the power systems. In this paper, the problem of the economic load dispatch(ELD) and the problem of combined economic emission load dispatch(CEELD) have been improved taking into account reliability indices. That is, the problem of reliability and ELD are proposed as combined economic load dispatch reliability(CELDR) and the problem of CEELD and reliability are suggested as (CEELDR). In solving CELDR and CEELDR problems, tried to use power generators in a very reliable way to save system load, as well as minimum fuel and emission costs. In this effort, the ELD of power plants is successfully implemented in a single system containing 6 generating units, taking into account the reliability and emissions of the system with and without system power loss, equality & inequality constraints, and valve point effects, by using the exchange market algorithm (EMA). The results suggest that the reliability indicators in ELD can be used to create greater reliability in providing consumers with uninterrupted power.

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## 1. INTRODUCTION

In this paper, the main objective is to schedule the output power of committed generating units so as to meet the required load with high reliability at minimum operating cost while satisfying system equality and inequality constraints [1, 2]. The practical ELD problem should be a non-convex problem with practical constraints, which cannot be solved directly through the mathematical optimization approaches. For example, the dynamic programming method can solve such types of problems, but it suffers from so-called the curse of dimensionality [3]. So, from the last decades, some advanced heuristic techniques such as genetic algorithm (GA) [4-6], stochastic fractal search (SFS) [7-9], particle swarm optimization (PSO) [10-12], biogeography-based optimization (BBO) [13-15], crow search algorithm (CSA) [16], symbiotic organisms search (SOS) [17], backtracking search algorithm (BSA) [18, 19], and exchange market algorithm [20, 21], are developed to solve these problems. In order to optimize the multi-object function of CELDR and CEELDR problems the EMA is applied to a system with 6 generation units.

EMA was first proposed by N. Ghorbani and E. Babaei in 2014. It's inspired by human intelligence and the process of trading shares in the stock markets. In the EMA, the market mode is available per each iteration of the program as balanced market, where the algorithm absorbs individuals toward the elite members, and oscillated market, where the algorithm is responsible for the searching process and finding unknown points. In EMA, the fitness of individuals is evaluated after each market mode, then they are ranked based on their conditions and fitness and placed in different groups by considering high capability of EMA in finding a global optimum point [21], in this paper the EMA algorithm is applied to solve CELDR and CEELDR problems.

## 2. PROBLEM FORMULATION

### 2.1. Objective function in problem

In solving CELDR&CEELDR problems, it is aimed to decrease the fuel cost of power plants along and greenhouse gases (GHGs) emission costs, and at the same time to increase the system reliability by applying system reliability in the solution process. The variables of the problem are the generated power of plants defined as follows [21]:

$$\text{Minimizing: } F = [F_{FC}, F_{GHG}, EENS] \quad (1)$$

where  $F_{FC}$  is the fuel cost of the units,  $F_{GHG}$  the greenhouse gases emission costs and EENS the expected energy not supplied. The objective function of the CELDR is consisting of two independent functions. Therefore, the objective function (1) should be replaced by the following objective function:

$$\text{Minimizing: } F = [F_{FC}, EENS] \quad (2)$$

### 2.2. ELD problem formulation

The aim of the ELD is minimizing the cost function of the system considering the system constraints. Generally, the simplified fuel cost function of each generation unit is as follows:

$$F_{FC} = \sum_{i=1}^n F_i(P_i) \quad (3)$$

$$F_i(P_i) = a_i + b_i P_i + c_i P_i^2 \quad (4)$$

where,  $F_i$  is the cost function of the  $i^{th}$  generation unit,  $F_{FC}$  is the total generation fuel cost,  $a_i$ ,  $b_i$  and  $c_i$  are the cost coefficients of the  $i^{th}$  generation unit,  $n$  is the last generation unit number and  $P_i$  is the output power of the  $i^{th}$  generating unit. A total generated power should equal to total system demand power plus total transmission line power losses. In other words:

$$\sum_{i=1}^n P_i = P_{load} + P_{loss} \quad (5)$$

where  $P_{load}$  is the total system load.  $P_{loss}$  is the power loss of a transmission line, which is defined as follows using  $B$  factor:

$$P_{loss} = \sum_{i=1}^n \sum_{j=1}^n P_i B_{ij} P_j + \sum_{i=1}^n B_{0i} P_i + B_{00} \quad (6)$$

In ELD problem without considering power losses. The total power should be the same as the total load as follows:

$$\sum_{i=1}^n P_i = P_{load} \quad (7)$$

The output power of each generation unit should correspond to the following constraint:

$$P_{i,\min} \leq P_i \leq P_{i,\max} \quad (8)$$

where,  $P_{i,\min}$  and  $P_{i,\max}$  are the minimum and maximum power amounts of  $i^{th}$  unit, respectively.

Power generation units with multi-steam valve create more variations in power unit cost function. Therefore, the cost function in (4) should become:

$$F_i(P_i) = a_i + b_i P_i + c_i P_i^2 + |e_i \times \sin(f_i \times (P_{i,\min} - P_i))| \quad (9)$$

where  $e_i$  and  $f_i$  are the coefficients of unit  $i$  reflecting valve-point loading [21].

**2.3. Emission problem formulation**

It is aimed to decrease the greenhouse gases (GHGs) emission costs of power plants. The GHGs is  $CO_2$  in this paper. The greenhouse gas emission costs from each unit depends on the power generated by that unit, which is given in (10).

$$F_{GHG} = \sum_{i=1}^n h_i EM_i(p_i) \tag{10}$$

$$EM_i(p_i) = ef_i (f_i + g_i p_i + h_i p_i^2) \tag{11}$$

where,  $EM_i(p_i)$  is the GHGs emissions of thermal unit  $i$ .  $f_i$ ,  $g_i$  and  $h_i$  are the fuel consumption coefficients of thermal units,  $ef$  is the fuel emission factor of GHGs for thermal generator,  $h$  is the given GHGs emission price which is determined by markets [21].

**2.4. Reliability problem formulation**

In calculating the system's EENS, our goal is creating a relationship between each unit forced outage rate value and amount of the productive power of that unit. In this way, we can compute the EENS of each power unit that depends on the value of forced outage rate ( $FOR$ ) and production power of each unit by using the following equations:

$$EENS_i = FOR_i \times T \times P_i \quad (MWh) \tag{12}$$

$$EENS = \sum_{i=1}^n EENS_i \quad (MWh) \tag{13}$$

where,  $P_i$  is the  $i^{th}$  unit's power capacity in terms of MW.  $T$  is the time interval in terms of hours,  $n$  is the number of the last unit. As shown in (12) and (13) have been used to compute EENS in the power market and deregulated systems [22].

**2.5. Combination of ELD, emission and reliability in objective function**

Since the ELD and emission cost, and EENS in terms of (\$/h) and MWh respectively, per-unit coding approaches have been used for combination multi-objective functions to a single objective function [22]. The final objective function of the CEELDR problem is as follows:

$$\text{minimize}(F = \gamma \times F_{FC,pu} + \eta \times F_{GHG,pu} + \mu \times EENC_{pu}) \quad (pu) \tag{14}$$

where  $F_{FC,pu}$  is the fuel cost in per-unit and equals:

$$F_{FC,pu} = \frac{F_{FC}}{F_{FC,max}} \quad (pu) \tag{15}$$

$$F_{FC,max} = \sum_{i=1}^n (a_i + b_i P_{i,max} + C_i P_{i,max}^2) \quad (\$/h) \tag{16}$$

In (14),  $F_{GHG,pu}$  is the emission cost in per-unit and equals:

$$F_{GHG,pu} = \frac{F_{GHG}}{F_{GHG,max}} \quad (pu) \tag{17}$$

$$F_{GHG,max} = \sum_{i=1}^n h_i \times ef_i (f_i + g_i P_{i,max} + h_i P_{i,max}^2) \tag{18}$$

where,  $EENS_{pu}$  is the per unit form of EENS and equals:

$$EENS_{pu} = \frac{EENS}{EENS_{\max}} \quad (pu) \quad (19)$$

and

$$EENS_{\max} = \sum_{i=1}^n FOR_i \times T \times P_{i,\max} \quad (MWh) \quad (20)$$

The parameters  $\gamma$ ,  $\eta$  and  $\mu$  are constants related to the influence percentage of each fuel cost, emission cost and EENS on the objective function and It is necessary to specify that the sum of these parameters is equal to one [22].

### 3. EXCHANGE MARKET ALGORITHM

The detailed data about the EMA that is appropriate for solving optimization problems, represented in [22]. The EMA has two searcher operators and two absorbent operators. In the EMA method there exists a specific number of shares, each member intelligently tries to buy a number of them, and intelligently performs to gain the maximum possible profit at the end of each period by calculating the validity of his own total shares. After each market mode, the members with high, middle, and lower ranks will be sorted as group 1, group 2, and group 3, respectively [22].

#### 3.1. EMA in balanced mode

In this mode, each individual is ranked based on the number of each type of share he holds and the fitness function. After sorting population, they will be sorted as group 1, group 2, and group 3, respectively and they will be changed, as follows [22].

##### 3.1.1. Frist group members with high ranks

The members of this group are the elite stockbrokers.

##### 3.1.2. Second group members with mean ranks

The members of this group use the successful experiences of elite stockbrokers, and based on the (21) to get further profit.

$$\begin{aligned} pop_j^{group(2)} &= r \times pop_{i,i}^{group(1)} + (1-r) \times pop_{2,i}^{group(1)} \\ i &= 1,2,3,\dots,n_i \quad \text{and} \quad j = 1,2,3,\dots,n_j \end{aligned} \quad (21)$$

where,  $n_i$  is the  $n^{th}$  member of the first group,  $n_j$  is the  $n^{th}$  member of the second group and  $r$  is a random number in interval [0, 1].  $pop_{i,i}^{group(1)}$  and  $pop_{2,i}^{group(1)}$  are the members of the first group and  $pop_j^{group(2)}$  is the  $j^{th}$  member of the second group.

##### 3.1.3. Third group members with low ranks

The members of this group get more profit would change the number of their shares based on the (22) and (23):

$$S_k = 2 \times r_1 \times (pop_{i,1}^{group(1)} - pop_k^{group(3)}) + 2 \times r_2 \times (pop_{i,2}^{group(1)} - pop_k^{group(3)}) \quad (22)$$

$$pop_k^{group(3),new} = pop_k^{group(3)} + 0.8 \times S_k \quad k = 1,2,3,\dots,n_k \quad (23)$$

where  $r_1$  and  $r_2$  are random numbers in the interval [0 1] and  $n_k$  is the  $n^{th}$  member of the third group.  $pop_k^{group(3)}$  is the  $k^{th}$  member and  $S_k$  is the share variations of the  $k^{th}$  member of the third group.

#### 3.2. EMA in oscillation mode

In this mode, the shareholders would start trading their shares. They will be sorted as a member of group 1, group 2, and group 3, respectively, and will be changed in their shares based on the policy of the group as follows [22].

**3.2.1. First group members with high ranks**

The members of this group lead the stock market and to preserve their rank, they do not undergo the trade risk.

**3.2.2. Second group members with mean rank**

The sum of the shares held by members tends to be constant and only the number of some of each type of shares increases and some decrease in a way that the sum remains constant. The number of shares held by each member increases based on (24) [22].

$$\Delta n_{t1} = n_{t1} - \delta + (2 \times r \times \mu \times \eta_1) \tag{24}$$

$$\mu = \left( \frac{t_{pop}}{n_{pop}} \right) \tag{25}$$

$$n_{t1} = \sum_{y=1}^n |s_{ty}| \quad y = 1, 2, 3, \dots, n \tag{26}$$

$$\eta_1 = n_{t1} \times g_1 \tag{27}$$

$$g_1^k = g_{1,max} - \frac{g_{1,max} - g_{1,min}}{iter_{max}} \times k \tag{28}$$

where  $\Delta n_{t1}$  is the amount of shares should be added to some shares,  $n_{t1}$  total shares of  $t^{th}$  member before applying the share changes.  $\delta$  is the information of exchange market,  $S_{ty}$  the shares of the  $t^{th}$  member,  $\eta_1$  the risk level related to each member of the second group,  $r$  a random number.  $t_{pop}$  the number of the  $t^{th}$  member in the exchange market. As shown in (25),  $n_{pop}$  shows the number of the last member in the exchange market and  $\mu$  a constant coefficient for each member. Each member of the second group,  $r$  is a random number.  $t_{pop}$  the number of the  $t^{th}$  member in the exchange market. As shown in (27),  $g_1$  the common market risk amount which decreases as iteration number increases. As shown in (28),  $iter_{max}$  the last iteration number,  $k$  the number of program iteration,  $g_{1,max}$  and  $g_{1,min}$  indicate the maximum and minimum values of risk in the market, respectively and are adjustable parameters of the EMA. The  $\Delta n_{t2}$  of each person equals:

$$\Delta n_{t2} = n_{t2} - \delta \tag{29}$$

where  $\Delta n_{t2}$  is the amount of shares should be decreased from some shares and  $n_{t2}$  is the sum share amount of  $t^{th}$  member after applying the share variations.

**3.2.3. Third group members with low ranks**

In this group each member sells a number of shares. The shareholders of this group change some of their shares based on (30):

$$\Delta n_{t3} = (4 \times r_s \times \mu \times \eta_2) \tag{30}$$

$$r_s = (0.5 - rand) \tag{31}$$

$$\eta_2 = n_{t1} \times g_2 \tag{32}$$

$$g_2^k = g_{2,max} - \frac{g_{2,max} - g_{2,min}}{iter_{max}} \times k \tag{33}$$

where  $\Delta n_{i3}$  the shear amount should be added to the shares of each member,  $r_s$  a random number in the interval  $[-0.5 \ 0.5]$  and  $\eta_2$  the risk coefficient related to each member of the third group. In (33),  $g_2$  the variable risk of the market in the third group and  $\mu$  a constant coefficient for each member.  $g_{2,max}$  and  $g_{2,min}$  indicate the maximum and minimum values of risk, respectively [22].

#### 4. IMPLEMENTATION OF EMA IN SOLVING CELDR&CEELDR PROBLRMS

The CELDR&CEELDR problems are accomplished using the EMA by taking the following steps:

- a) Selecting initial values.
- b) Calculating members' fitness by (14), ranking them, and sorting of shareholders in three groups.
- c) Applying variations on the shares of the second group members in normal mode by (21).
- d) Applying variations on the shares of the third group members by (23).
- e) Recalculating shareholders' fitness by (14), ranking and sorting members in three separate groups.
- f) Trading the shares of the second group members using (24) in oscillated mode.
- g) Trading the shares of the third group members using (30) in oscillated mode.
- h) Jumping to step 2 until the program ending criterion is satisfied.

A flowchart of the EMA's implementation for solving the above problems is shown in Figure 1.

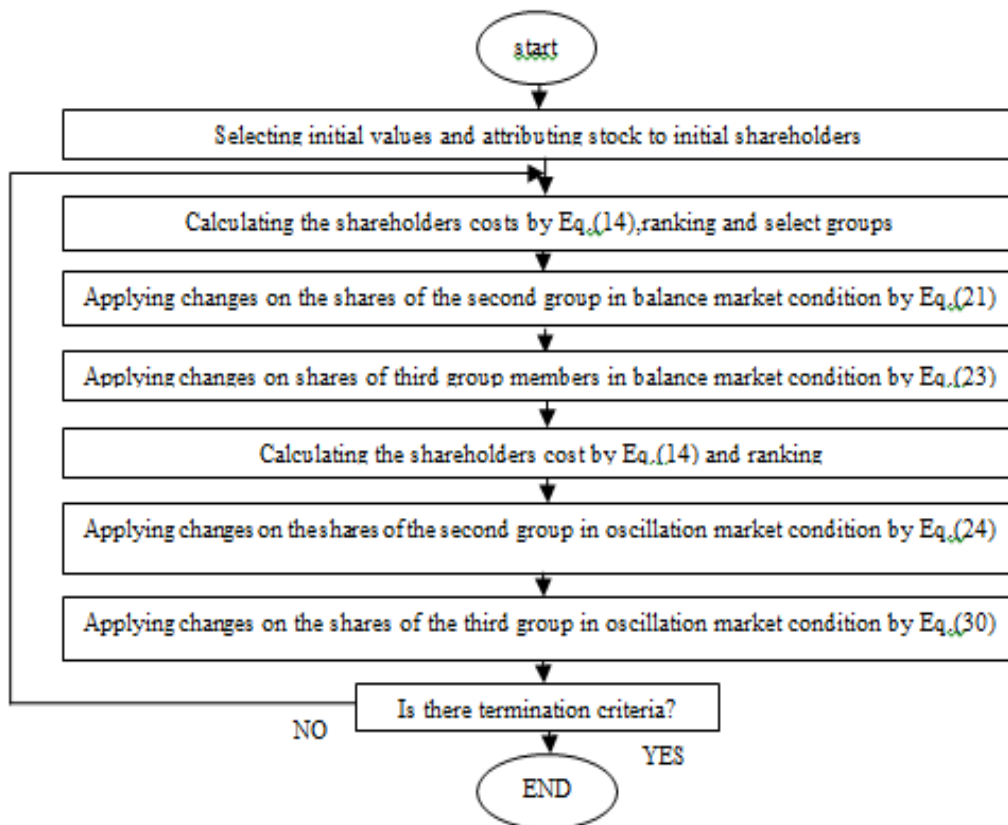


Figure 1. Flowchart of EMA for solving CELDR&CEELDR problems

#### 5. RESULTS AND DISCUSSION

In this paper, EMA is implemented successfully in 6-units system considering ELD, emission and reliability. All the programs are developed and simulated using MATLAB version 7.01. The system configuration is Pentium IV processor with 3.2GHz speed and 2 GB RAM. The CEELDR is considered for just one hour. Fifty separate experimentations were conducted to compare the solution quality and convergence characteristics. The initial population size and iteration number are set to 100 and 5000, respectively. The objective function's penalty factor in per unit form is set to 0.07 and in non-per-unit form is

set to 100. The number of individuals in 1<sup>st</sup>, 2<sup>nd</sup> and 3<sup>rd</sup> groups in non-oscillation market mode are set to 25, 25 and 50% of the initial population, and the pattern for the oscillated market mode are set to 25, 60 and 15% of initial population [22]. The necessary adjustable parameters of the proposed algorithm are risk factors of 2<sup>nd</sup> and 3<sup>rd</sup> groups in an oscillated market mode are presented in Table 1.

Table 1. Adjustable parameters of EMA for solving CEELDR problem

Risk value	$g_1$ [max, min]	$g_2$ [max, min]
6 units system	[0.1, 0.0001]	[0.005, 0.0005]

**5.1. Six units system**

The tests are applied to 6 generating units with power losses of transmission line, equality and inequality constraints, valve-point effects, and are solved by the EMA method. The fuel cost coefficients, generator limits, and emission data are reported in [23]. The total system load is 1200MW.

**5.1.1. Solving CELDR problem considering different influence percentages of reliability**

In this section, six independent experimentations are conducted considering different influence percentages of each independent function on the objective function to investigate the efficiency of CELDR problem. The FOR values of units in different cases (1 to 6) are presented in [24]. The experimentations are detailed as follows:

- a) The aim is to reduce the unit’s fuel costs, considering no reliability.
- b) Decreasing the fuel cost of units by applying 20% reliability.
- c) Decreasing the fuel cost of plants by applying 40% reliability.
- d) Decreasing the fuel cost of plants by applying 50% reliability.
- e) Decreasing the fuel cost of plants by applying 60% reliability.
- f) Increasing the reliability considering no fuel cost.

The obtained results are illustrated in Table 2. In case 1, the fuel cost is 29491.4284 (\$/h), which is the minimum among the other cases. The EENS by EMA method is 46.6274 MWh and is 46.6279 MWh through PSO-SIF method [24], that is the worst case in comparison with the other cases. Comparing the results of the second experimentation by EMA method that is shown in Table 2 depicts the system EENS value decreases by 0.2675 MWh and reaches to 46.3599MWh in comparing the previous case and increase the reliability percentage up to 20%.

In obtained results by EMA method, it is obvious as the reliability in the system increases, the EENS value decreases proportionally and as the fuel cost decreases, its value increases proportionally. This is accomplished in a way that as the reliability increases by 40% and the units' fuel cost decrease of 40% in the third case, the EENS value decreases in comparison with the first case by 6.9995 MWh and this value is 6.9984 MWh for PSO-SIF method.

In Figure 2 and Figure 3, the convergence characteristics of the CELDR problem objective function in per-unit form through the EMA and PSO-SIF methods are presented (case studies 1, 2 and 3). At last, in case 6, the CELDR was accomplished to decrease the optimized system’s EENS considering no fuel costs. The system EENS by EMA method is 33.8997 MWh, which is the minimum among the other cases, the fuel costs by EMA method is 35725.5827\$/h and is 35725.7280 for PSO-SIF method, that is the worst case in comparison with the other case studies.

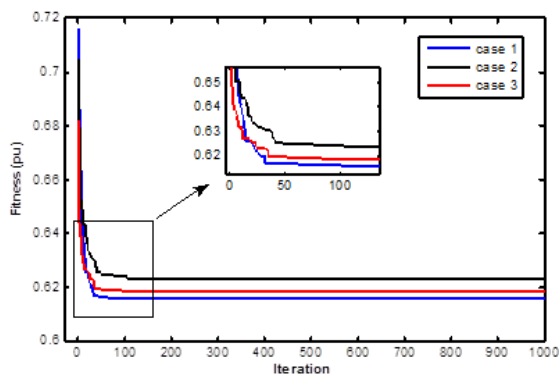


Figure 2. Convergence characteristics of the EMA for test system

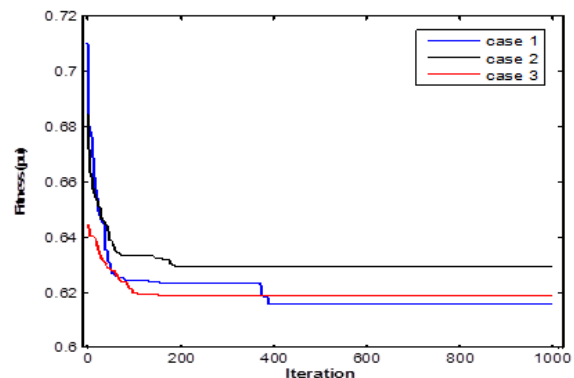


Figure 3. Convergence characteristics of the PSO-SIF for test system

### 5.1.2. Solving CELDR problem considering different outage rate of power units

In this section, six experimentations are conducted to investigate the influence of units' outage rate on the power amount delivered to the system. The aim is to decrease the unit fuel cost considering 50% system reliability influence on the objective function. The *FOR* values for B-G experimentations are shown in Table 2 and are detailed as follows:

- The *FOR* values of *A* mode are presented in [24], and applied in all the six cases.
- Increased *FOR* of unit 1 by 25% in comparison with *A*.
- Decreased *FOR* of unit 2 by 57% in comparison with *A*.
- Decreased *FOR* of unit 3 by 40% in comparison with *A*.
- Increased *FOR* of unit 4 by 50% in comparison with *A*.
- Increased *FOR* of unit 5 by 66% in comparison with *A*.
- Decreased *FOR* of unit 6 by 50% in comparison with *A*.

Table 2. Results of CELDR in a system with a six - generation applying different reliability percentages

O/P	Case 1		Case 2		Case 3		Case 4		Case 5		Case 6	
	$\gamma=1.0, \mu=0.0$		$\gamma=0.8, \mu=0.2$		$\gamma=0.6, \mu=0.4$		$\gamma=0.5, \mu=0.5$		$\gamma=0.4, \mu=0.6$		$\gamma=0.0, \mu=1.0$	
	PSO_S IF [24]	EMA	PSOSI F [24]	EMA	PSO_SI F [24]	EMA	PSO_SI F [24]	EMA	PSO_S IF [24]	EMA	PSO_S IF [24]	EMA
P1	94.799 8	94.799 8	94.807 4	94.80 22	94.804 4	94.79 98	94.799 8	94.800 1	94.80 00	94.799 7	20.000 0	20.000 0
P2	100.00 00	100.00 00	26.986 0	99.99 85	99.988 3	99.99 98	20.002 7	100.00 00	99.98 65	99.999 8	20.000 0	20.000 0
P3	568.79 89	568.79 90	419.20 13	568.7 990	344.39 94	344.3 994	269.59 96	194.79 98	120.0 013	119.99 99	120.00 00	120.00 0
P4	259.59 96	259.59 96	508.93 65	286.4 000	510.64 24	510.8 003	515.99 81	510.79 98	510.8 098	510.80 08	519.99 96	519.99 99
P5	136.80 15	136.80 16	110.06 86	110.0 001	110.16 52	110.0 005	259.59 96	259.59 97	334.3 979	334.99 47	480.00 04	479.98 99
P6	40.000 0	40.000 0	40.000 0	40.00 00	40.000 0	40.00 00	40.000 0	40.000 4	40.00 00	40.000 0	40.000 0	40.000 0
F <sub>FC</sub>	29491. 428	29491. 4284	31191. 78	29534 .0355	31616. 91	31616 .8955	32862. 8637	33294. 2263	34217 .1802	34216. 8246	35725. 728	35725. 5827
EE	46.627 9	46.627 4	40.777 6	46.35 99	39.629 5	39.62 79	37.680 0	36.636 0	35.13 99	35.139 9	33.900 0	33.899 7
NS	1200 0.6157	1200 0.6157	1200 0.6274	12000 0.623	1200 0.6183	1200 0.618	1200 0.6072	1200 0.6069	1200 0.581	1200 0.5814	1200 0.4754	1200 0.4754
TP	01	01	17	315	71	362	80	93	481	50	55	51

The results obtained from A-G experimentations by the EMA method by comparing PSO-SIF method are shown in Table 3. In the experiment *B*, the *FOR* of unit 1 is increased by 25% in comparison with the state *A*. As a result, the reliability of the unit 1 is decreased. As shown in Table 3, as the *FOR* of unit 1 in the state *B* increased in comparison with state *A* of the same unit, the amount of delivering power in constant load of 1200 MW decreases from 94.8001MW to 20.0002MW.

As seen from Table 3, in solving this case study with the PSO-SIF method in the constant load of 1200 MW the power generation of unit 1 decreases from 94.7998MW to 57.3999MW. In solving this case, the aim is to find the minimum value of *F* that obtained results by EMA and PSO-SIF methods are 0.611181pu and 0.621957 pu, respectively. The results show the superiority of EMA. This results show the existence of linear relation between *FOR* and consequently the unit 1 reliability and the power amount delivered to the system. Therefore the total EENS of the system increases from 36.6360 MWh in *A* case study to 37.5840 MWh in *B* case. This depicts the influence of a power unit on total system EENS. And in the last. In solving case study *G*, the outage rate of unit 6 is decreased by 50% in comparison with that of the case *A*. The decreasing of outage rate results in a considerable increase in unit 6 reliability and generated power amount. As it is shown in Table 3, the generated power of unit 6 increases from 40.0004 MW in the case *A* to 199.9998 MW in case *G*. Here, the amount of EENS is decreased in comparing with case *A* as expected (36.6360 to 32.7586).



Table 3. CELDR problem results considering different FOR of power units

O/ P	A		B		C		D		E		F		G	
	PSO_ SIF [24]	EMA	PSO_ SIF [24]	EMA	PSO_ SIF [24]	EMA	PSO_ SIF [24]	EMA	PSO_ SIF [24]	EMA	PSO_ SIF [24]	EMA	PSOS IF [24]	EMA
P1	94.79 98	94.80 01	57.39 99	20.00 02	20.00 00	94.79 98	94.79 98	20.00 00	94.79 93	94.79 98	94.79 98	94.80 22	20.00 01	94.79 98
P2	20.00 27	100.0 000	20.00 21	100.0 000	100.0 0	100.0 000	20.00 04	20.00 01	100.0 000	100.0 000	100.0 000	100.0 000	99.99 92	100.0 000
P3	269.5 996	194.7 998	269.5 996	269.5 996	269.5 996	120.0 000	575.8 662	600.0 000	269.5 996	269.5 996	344.3 994	344.3 998	269.5 996	120.0 000
P4	515.9 981	510.7 998	366.3 990	510.7 997	409.1 993	510.7 999	359.3 328	409.9 998	409.2 0000	508.9 349	510.7 999	510.7 976	508.9 324	508.9 324
P5	259.5 996	259.5 997	446.5 992	259.6 003	361.2 009	334.3 994	110.0 007	110.0 000	259.5 993	186.6 655	110.0 000	110.0 000	133.2 403	176.2 679
P6	40.00 00	40.00 04	40.00 00	40.00 00	40.00 00	40.00 08	40.00 00	40.00 00	66.80 30	40.00 00	40.00 07	40.00 02	168.2 282	199.9 998
F <sub>FC</sub>	32862 .8637	33294 .2263	33531 .4483	33264 .7786	33435 .4890	34216 .8206	29716 .8443	30531 .8085	32565 .4949	32425 .5583	31616 .8925	31616 .8825	33706 .4957	34682 .2466
EE	37.68	36.63	39.37	37.58	36.90	33.64	28.09	26.60	43.50	43.23	41.82	41.82	35.32	32.75
NS	00	60	60	40	00	33.64	60	00	80	99	799	799	038	86
TP	1200	1200	1200	1200	1200	1200	1200	1200	1200	1200	1200	1200	1200	1200
F	0.607 280	0.606 993	0.621 957	0.611 181	0.613 348	0.603 962	0.573 768	0.571 701	0.624 306	0.623 886	0.590 923	0.590 922	0.614 260	0.611 347

5.1.3. Solving CELDR problem considering emission cost

Tests are conducted on a system with six generation units considering fuel cost, emission cost and reliability level in 2 sections with and without considering power loss transmission. In the first section, the CEELDR problem is solved by the EMA method without considering power losses of the system and obtained results in comparing the results of the PSO-SIF method is presented in Table 4. As seen from Table 4, the aim of solving the CEELDR problem in this section is the minimization of fuel cost, emission cost, EENS, all of the system cost and minimization of all three functions. As seen from Table 4, the EMA method could find the minimum objective function ( $F$ ) in per-unit form better than PSO-SIF method.

Table 4. CEELDR problem results considering fuel and emission cost and EENS

UNIT NO.	Minimization $F_c$		Minimization $E$		Minimization $EENS$		Minimization $F_c, E$		Minimization $F_c, E, EENS$	
	PSO-SIF [24]	EMA	PSO-SIF [24]	EMA	PSO-SIF [24]	EMA	PSO-SIF [24]	EMA	PSO-SIF [24]	EMA
Unit 1	94.7998	94.7998	20.0000	20.0000	20.0000	20.0000	20.0006	20.0000	20.0000	57.4028
Unit 2	100.0000	100.0000	20.0000	20.0000	20.0000	20.0000	20.0000	20.0000	20.0000	20.0006
Unit 3	568.7989	568.7990	120.0000	120.0000	120.0000	120.0000	344.3995	568.7989	269.5996	269.6004
Unit 4	259.5996	259.5996	520.0000	520.0000	519.9996	520.0000	515.9995	409.1988	508.9324	515.9964
Unit 5	136.8015	136.8016	479.9995	479.9999	480.0004	479.9999	259.6001	142.0022	341.4675	296.9996
Unit 6	40.0000	40.0000	40.0005	40.0000	40.0000	40.0000	40.0002	40.0000	40.0005	40.0000
Fuel cost	29491.42 89	29491.42 84	35725.74 06	35725.73 34	35725.72 73	35725.73 35	32853.56 82	30484.44 57	33733.81 92	33292.08 97
Emissi on	20227.65 38	20227.65 381	15064.27 39	15064.26 88	15064.29 88	15064.26 91	16456.55 68	18018.25 15	15971.73 65	16375.39 56
Total cost	49719.08 28	49719.08 22	50790.01 45	50790.00 23	50790.02 61	50790.00 27	49310.12 50	48502.69 72	49705.55 57	49667.48 54
EENS Total power	46.6279	46.62798	33.9001	33.9000	33.9000	33.9000	38.4280	43.9839	37.0026	37.3060
F	0.653968	0.615701 9	0.622537	0.622536	0.475457	0.475455	0.768560	0.678622	0.682154	0.650223

The results of solving the CEELDR problem with power loss of the system through the EMA and PSO-SIF is presented in Table 5. Data for B coefficient of power transmission losses are reported in [25]. As seen from Table 5, in solving the CEELDR problem with considering the only fuel cost or emission cost or EENS, the EMA method could find the minimum value of objective function better than PSO-SIF method that shows the high ability of the proposed EMA method.

In solving the CEELDR problem with considering all functions the obtained minimum fuel cost (29729.6280 \$/h), emission cost (15223.0114\$/h), system's EENS (35.00708 MWh), both fuel and emission

cost (48824.3726 \$/h) and minimum value of all functions (both fuel and emission cost is 49730.1020 and EENS is 38.9893 MWh) by EMA method is lower than PSO-SIF method.

The CEELDR problem with power loss of the system and considering all of the functions in the objective function is solved also by PSO-TVAC [2] & PSO [25] method and the obtained results are presented in Table 6. In this comparison, per-unit coding is used to combine proposed multi-objective problem and offer a single objective function. For PSO,  $C_1$  and  $C_2$  were considered equal to 2.0. The weighting inertia coefficients for both PSO and PSO-TVAC were considered a varying number in the range [0.3, 0.9] and the initial population size and iteration number were 100 and 5000, respectively. The adjustable parameters for PSO-TVAC were chosen as:  $C_{1i} = C_{2f} = 2.5$  and  $C_{1i} = C_{2i} = 0.5$ . The adjustable parameters for PSO-SIF were chosen as:  $\delta_1 = 0.04$  and  $\delta_2 = 0.03$ . As it is obvious from Table 6, the minimum total cost obtained using EMA is 49730.1020 (\$/h) and the related EENS of which is 38.9893 (MWh) that are lower than both total cost and system's EENS obtained through PSO and PSO-TVAC approaches which shows the superiority of the EMA over the mentioned techniques.

Table 5. CEELDR problem results with power loss considering fuel and emission cost and EENS

UNIT	Minimization $F_c$		Minimization $E$		Minimization $EENS$		Minimization $F_c, E$		Minimize $F_c, E, EENS$	
	EMA	PSO-SIF	EMA	PSO-SIF	EMA	PSO-SIF	EMA	PSO-SIF	EMA	PSO-SIF
Unit 1	98.2816	104.3632	20.0000	20.0000	20.0000	20.3254	20.0000	20.0000	20.0000	102.9689
Unit 2	100.0000	100.0000	20.0000	20.0000	34.4883	100.0000	20.0000	20.0000	20.0000	20.0000
Unit 3	568.8165	600.0000	134.4839	134.4847	120.0000	120.0000	568.7988	562.9216	344.3999	348.7237
Unit 4	259.5997	260.3522	520.0000	520.0000	520.0000	520.0000	455.9223	461.7216	508.9665	520.0000
Unit 5	147.3999	110.0000	500.0000	500.0000	500.0000	426.0485	110.0000	110.0000	283.0018	180.6293
Unit 6	40.0000	40.0000	40.0000	40.0000	40.0000	40.0000	40.0000	40.0000	40.0000	40.0000
Fuel cost	29729.62	29854.74	36618.51	36618.53	36617.91	35889.35	30772.65	30922.138	33240.93	32407.35
on	80	32	59	50	83	13	08	7	95	71
Emission	20294.03	20595.29	15223.01	15223.18	15384.78	16500.28	18051.72	18008.943	16489.16	17420.07
TC	12	07	14	95	80	69	18	1	25	51
EENS	50023.65	50450.03	51841.52	51841.55	52002.70	52389.63	48824.37	48931.081	49730.10	49827.43
PL	92	39	73	29	63	82	26	8	20	23
PT	47.0860	47.7815	35.2241	35.2242	35.00708	35.09447	43.9583	43.7805	38.9893	39.6738
F	14.0977	17.4154	34.4838	34.4846	34.4882	26.3739	14.7211	14.6432	16.3682	12.3221
Error	1214.097	1214.715	1234.483	1234.484	1234.488	1226.373	1217.721	1214.6432	1216.368	1212.322
	7	4	8	6	2	9	1	1	2	1
	0.620675	0.623361	0.629096	0.629342	0.49098	0.492215	0.681797	0.685038	0.652960	0.655175
	0	0	0	8.1998*10 <sup>-4</sup>	0	0	0	5*10 <sup>-6</sup>	0	5*10 <sup>-6</sup>

Table 6. Comparison of the results of each method for CEELDR problem with power loss considering fuel and emission cost and EENS

Unit	Minimization $F_c, E, EENS$			
	PSO-TVAC[2]	PSO-SIF[24]	PSO [25]	EMA
Unit 1	94.5590	102.9689	110.0000	20.0000
Unit 2	98.4950	20.0000	97.3447	20.0000
Unit 3	417.6985	348.7237	195.6196	344.3999
Unit 4	267.9044	520.0000	276.7271	508.9665
Unit 5	295.5654	180.6293	403.9220	283.0018
Unit 6	41.7404	40.0000	139.5134	40.0000
Fuel cost (\$/h)	31503.6376	32407.3571	34622.3139	33240.9395
Emission (\$/h)	19177.1914	17420.0751	19048.1476	16489.1625
Total cost (\$/h)	50680.8290	49827.4323	53670.4646	49730.1020
EENS (Mwh)	44.009273	39.6738	40.82079	38.9893
Power loss (MW)	15.962638	12.3221	23.1271	16.3682
Total power	1215.9626	1212.3221	1223.1271	1216.3682
F (pu)	0.676843	0.655175	0.697930	0.652960

### 6. CONCLUSION

This paper proposed the EMA to solve the CELDR&CEELDR problems. This algorithm is applied on above problems with system power loss, valve-point effect and operational constraints. The obtained results of solving CELDR & CEELDR problems by EMA method in section 5.1.1 depict the fact that the system tends to utilize power units, which have lower values of FOR or units have higher reliability considering power supplied to system. In obtained results by EMA method, it is obvious as the reliability

increases, the EENS value decreases proportionally, and as the fuel cost decreases, its value increases proportionally. The obtained results of solving multi-objective CELDR and CEELDR problems by EMA method shows the high ability of proposed EMA method in compared other algorithms.

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