

## A study on non-linear behavior of memristor emulator using multisim

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### Article Info

#### Article history:

Received Dec 20, 2018

Revised Jul 30, 2019

Accepted Aug 10, 2019

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#### Keywords:

Memristors  
Emulator  
TiO<sub>2</sub>memristor  
Resistor  
Capacitor

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### ABSTRACT

A Memristor (memory resistor) is a two terminal non-linear passive element used to relate magnetic flux with respect to electric charge. A Memristor opposes the flow of electric current across a device like a resistor but also remember the last charge that was flowing through it. Memristor is a fourth passive circuit element after inductor 'L' resistor 'R', and capacitor 'C'. The voltage and current relationship in a memristor is a multivariable function therefore analyzing the circuit is a difficult task. This paper depicts the designing of a memristor model emulator using multisim and studied about its linear and non-linear characteristics.

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## 1. INTRODUCTION

Memory for the resistor concept was first proposed by widrow in 1960 and named as memistor. Later in 1968, Fano et al listed an unknown passive element apart from resistor, capacitor and inductor [1]. In 1971, Prof. Leon Chua a mathematician realized the first practical and mathematical memristor. Among the four main fundamental variables current 'I' voltage 'V' charge 'q' and flux ' $\Phi$ ' chua predicted that there is a missing relationship between flux and charge characterized by  $g(\Phi, q) = 0$  which has been named as a memristor [2], [3]. The missing relationship between flux and charge is shown in Figure 1. In 2008 Stanley Willams group built a nano scale chip made with TiO<sub>2</sub> which is a nonvolatile memory resistor. A memristor emulator circuit using multisim has been proposed in this paper and studied its characteristics [1]. It is expected with a lot of potential applications on memristor [4]. Memristor can also be used as a nonvolatile memory device since it has high density and fast as DRAM [5]. Few cases has been depicted on negative shade of memristors as well [6]. It is also been used in the field of artificial neural network in the field of communication systems [7]. Itoh, M et al, presented the application of memristor as an oscillator [8] and also been used in the application of masking the signal in communication [9]. These are also used as ring oscillator physically unclonable function to improve the efficiency [10-12]. Similar devices for energy storage are emulated as well [13]. Relevant study also reviewed and implemented in application to IOT [14-16]. Other types of encryption and super capacitor devices are presented with simulation results [17], [18].

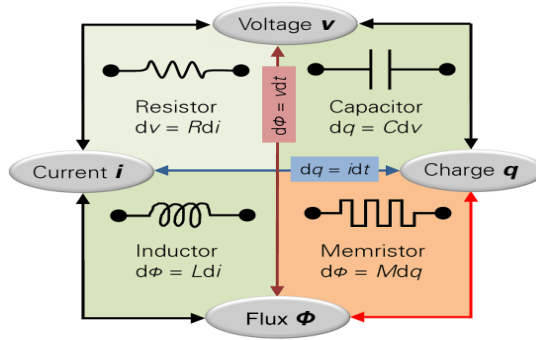


Figure 1. Missing Element Memristor

**1.1. Principle**

The V-I relationship in a memristor is defined as:

$$v(t) = i(t)R = \frac{d\phi}{dq} i(t) \tag{1}$$

From Equation (1)  $\phi(t)$  denotes the flux and  $q(t)$  denotes the charge with respect to the time. The resistance of the device is the gradient at the operating point in  $\phi$ - $q$  curve. If  $\phi$ - $q$  relationship is a nonlinear then the value of resistance varies with the operating point [19]. In the absence of external voltage the operating point will not change and the resistance remains constant. So, the signal is remembered as the value of memory resistance (Memristance 'M') [3].

$$R = M = \frac{d\phi}{dq} \tag{2}$$

The first memristor was designed by HP Company using TiO<sub>2</sub>. The HP Company team members built a nano device and shared one common point is that it reveals pinched hysteresis loop [20]. A thin oxygen poor titanium dioxide and titanium dioxide layer are inserted between two electrodes of platinum [4].

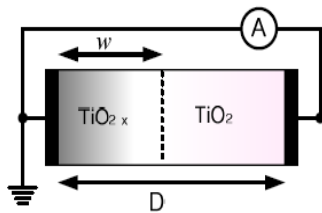


Figure 2. Physical Memristor



Figure 3. Memristor Symbol

Where the TiO<sub>2x</sub> is an undoped layer and TiO<sub>2</sub> is a doped layer shown in Figure 2. When a voltage or a current is applied between the two terminals of a memristor the value of resistance will change. Here D and w denotes the thickness area and doped area. R<sub>ON</sub> and R<sub>OFF</sub> implies high and low level doped concentration areas [1].

$$v(t) = \left\{ Ron \frac{w(t)}{D} \middle| Roff \left( 1 - \frac{w(t)}{D} \right) \right\} i(t) \tag{3}$$

The Equation three shows the relationship between voltage and current with respect to the thickness and doped area. The Symbol for a Memristor is shown in Figure 3.

Memristor can be considered as a fourth passive element with high flexibility, no leakage current and more compatible with CMOS [21]. A Memristor is a combination of memory and a resistance which is a continuous variable resistor whose resistance value will depends upon the history of current passed in it [22].

When a memristor is excited with positive voltage, the conductivity increases with decrease in resistance on the other hand when a negative potential is applied the resistance increases. If the voltage or potential is turned off, the memristor will remain its last value of resistance [23]. If Memristor is used as a memory element the high resistance state will be logic 1 and low resistance will be logic 0 [24].

**1.2. Schematic representation of Memristor Emulator**

The Figure 4 shows the block diagram of Memristor Emulator. The inverting amplifier circuit is one whose output is 180° out of phase with the input due to negative feedback. The output of inverting amplifier is fed to a voltage to current converter with grounded load. The V-I converter converts the voltage into a current which should drive the RC parallel circuit. The values of Resistor 10KΩ and Capacitor 1μF are to be assumed for the analysis of memristor emulator circuit.

From Equation (4) AD633JN is a four-quadrant analog multiplier whose result is a product of two outputs from R and C respectively. Where X and Y are differential inputs with a high impedance summing input (Z) and one output (W) the low impedance output voltage is a full scale 10 V provided by a Zener diode [19]. Hence output can be represented by:

$$W = \frac{(X1-X2)(Y1-Y2)}{10V} + Z \tag{4}$$

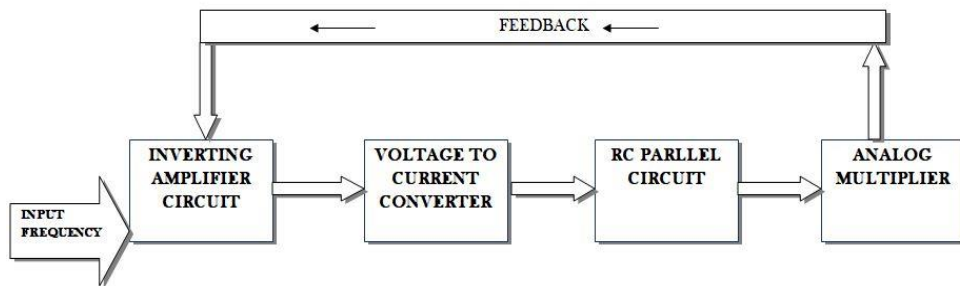


Figure 4. Block Diagram of Memristor Emulator

**1.3. Basic Memristor Emulator Circuit**

Basic Memristor Emulator Model in Figure 5, voltage at the input :

$$V_{in} = (R_s \times I_{in}) + V_x \tag{5}$$

From Equation (5), where  $I_{in}$  is the input current,  $R_s$  is the resistance at the input of inverting terminal  $V_x$  is the voltage applied to the non-inverting terminal of the op Amp. Here the voltage  $V_x$  is proportional to input current then consider:

$$V_x = m \times I_{in} \tag{6}$$

Then;

$$V_{in} = (R_s \times I_{in}) + (m \times I_{in}) \tag{7}$$

Rewriting the equation  $V_{in} = (R_s + m) I_{in}$  (8)

Where  $m$  is the proportional coefficient and the input resistance is  $(R_s + m)$  the value of  $m$  can be controlled by the time integral of input current  $I_{in}$ . So, the above fig. acts like a memristor. To emulate  $V_x$  the components resistor, capacitor and multiplier are used [19].

We can write  $V_x$  as:

$$V_x = \frac{q}{c} \times R_3 \times I_{in} \tag{9}$$

Substitute  $Vx$  in  $Vin$

$$\text{Therefore } Vin = \left\{ Rs + \frac{q}{c} \times R3 \right\} \times Iin \tag{10}$$

From the equation (10) we can say the input resistance increases proportionally to the time integral of current at input with offset  $Rs$ .  $Rs$  is a fixed part and  $\frac{q}{c} \times R3$  is a variable part. We can call this as incremental memristor emulator circuit [19].

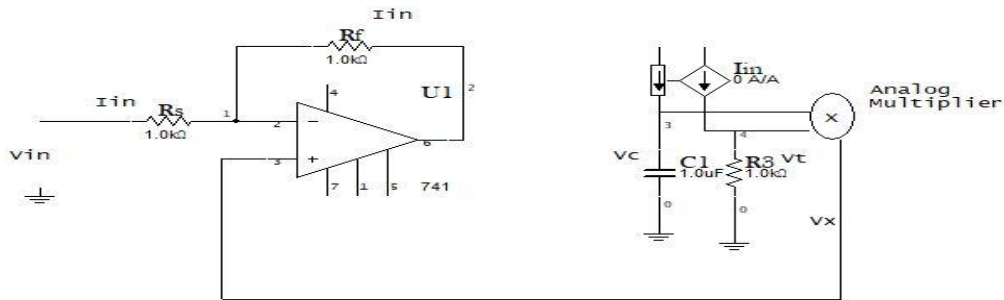


Figure 5. Basic Memristor Emulator Model

## 2. METHODOLOGY

### 2.1. Realization of Memristor using MULTISIM

The Figure 6 shows a memristor emulator in multisim assuming the values of resistances for op Amp are  $1K\Omega$  and for RC circuit  $R=10K\Omega$  and  $C=1\mu F$ . For linear characteristics the memristor is a linear resistor the voltage to current relation is a straight line since both are directly proportional to each other [19]. Memristor with fixed value  $M$  is a linear resistor. If  $M$  is variable it can act as a memory function, so a non linear component is necessary as a converted component. A Diode 1N1199C can convert the fixed value  $M$  to variable  $M$  [25]. A complete representation of a simple memristor emulator is shown in the Figure (6). In practice the value of  $Rs$  is considered a small value around  $1K\Omega$ . When an input is applied to a memristor emulator it is converted in terms as a input current  $Iin$  with resistor  $Rs$  and op Amp U1 via virtual ground concept. A Grounded load voltage to current converter provides an output current. The output current from V-I converter is driven to a parallel RC circuit where a charge in the capacitor takes place  $Vc = \frac{q}{c}$  with  $Vt = R3 \times Iin$ . The quadrant analog multiplier multiplies the voltage  $Vc$  and  $Vt$  with output product  $Vx = \frac{q}{c} \times R3 \times Iin$ . During the charge emulator stores its value as a function of memory resistor [19].

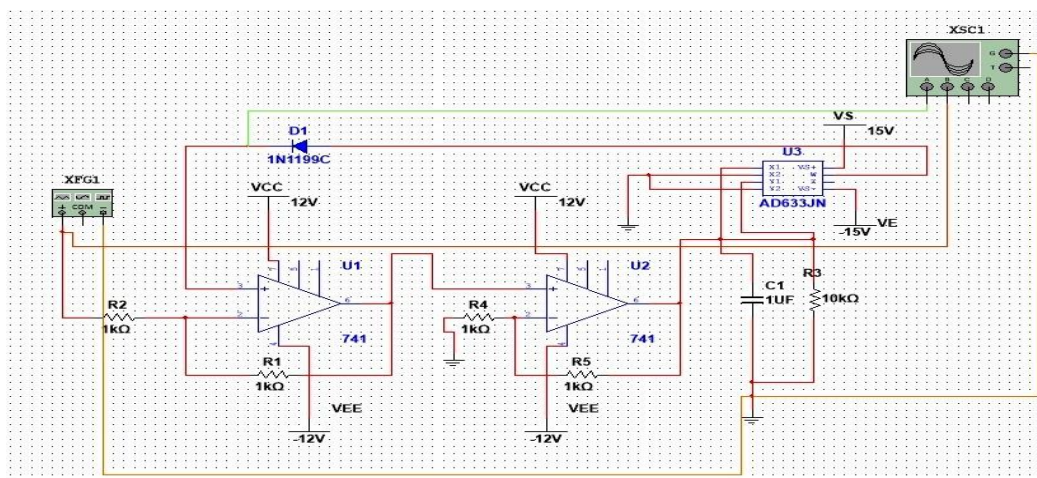


Figure 6. Realization of Memristor using MULTISIM

### 3. RESULT ANALYSIS

#### 3.1. Memristor Emulator Simulation Graphs

The Figure 7 shows a Simulation Graph result for frequency  $F=1$  Hz, in which red color indicates the input sine wave form with input 10Vpp amplitude. For frequency  $F=1$ Hz which is almost a DC component and shows a linear relationship between input and output (blue color) with respect to time.

The Figure 8 shows a Simulation Graph result for frequency  $F=100$  Hz, the output wave is a low level clamped signal which shows a slightly non-linear relationship with input ac component.

The Figure 9 shows a Simulation Graph result for frequency  $F=500$  Hz, the output wave shows a non-linear relationship with an input. The corresponding input and output waveforms with respect to time for both A/B (input/output) and B/A (output/input) are shown in Figure 10 and 11 respectively.

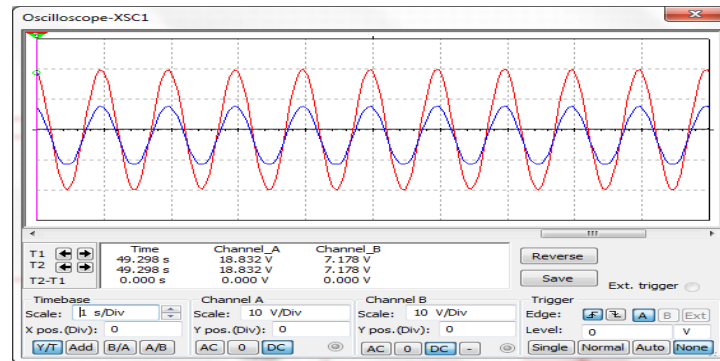


Figure 7. Memristor Emulator Simulation Graph for the frequency  $F=1$ Hz

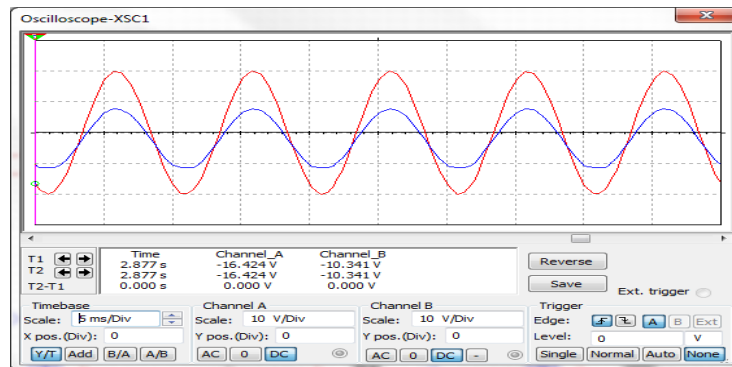


Figure 8. Memristor Emulator Simulation Graph for the frequency  $F=100$ Hz

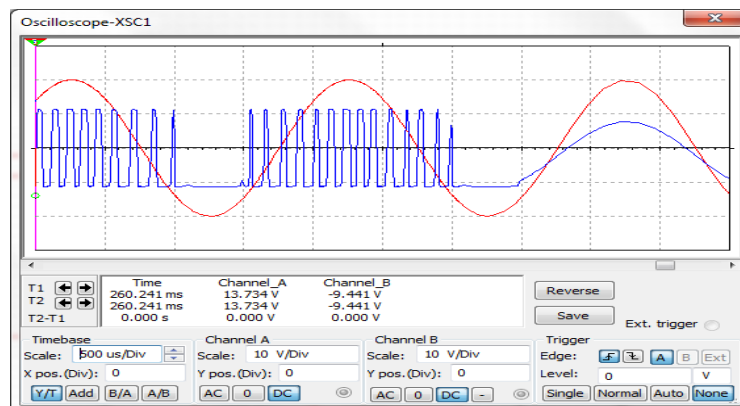


Figure 9. Memristor Emulator Simulation Graph for the frequency  $F=500$ Hz

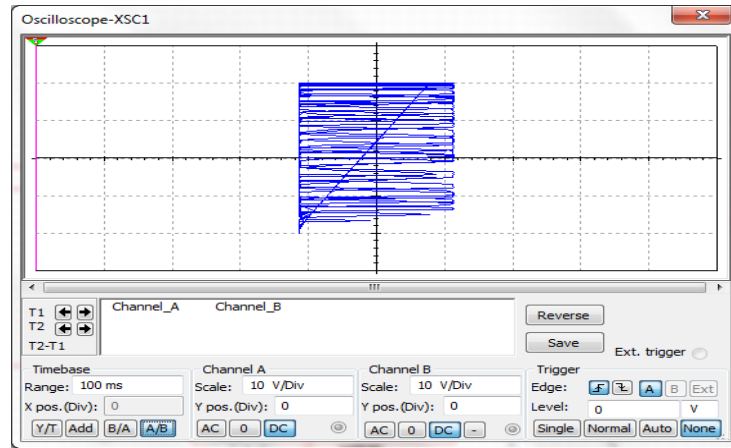


Figure 10. A/B (Output/Input)

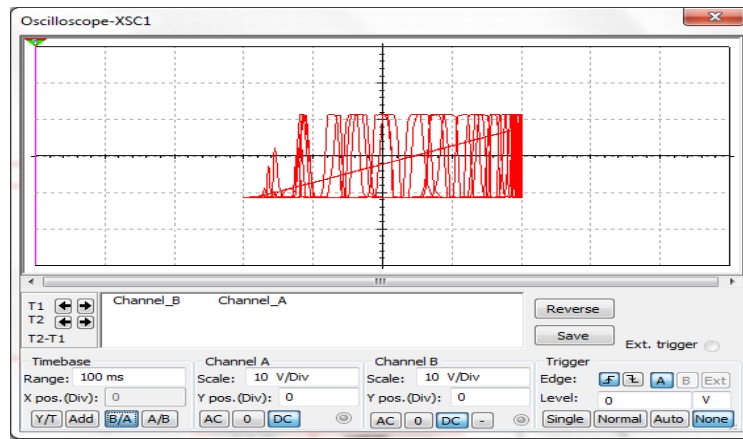


Figure 11. B/A (Output/Input)

The Figure 12 shows a Simulation Graph result for frequency  $F=1$  KHz, the output wave shows a non-linear relationship with an input. The corresponding input and output waveforms with respect to time for both A/B (input/output) and B/A (output/input) are shown in Figure 13 and 14 respectively.

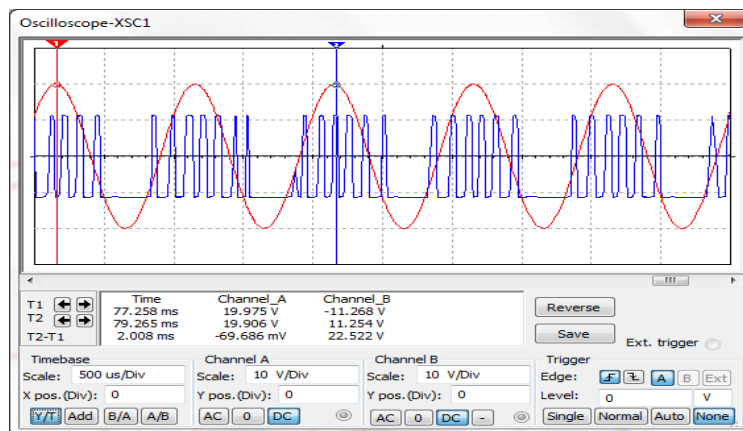


Figure 12. Memristor Emulator Simulation Graph for the frequency  $F=1$  KHz

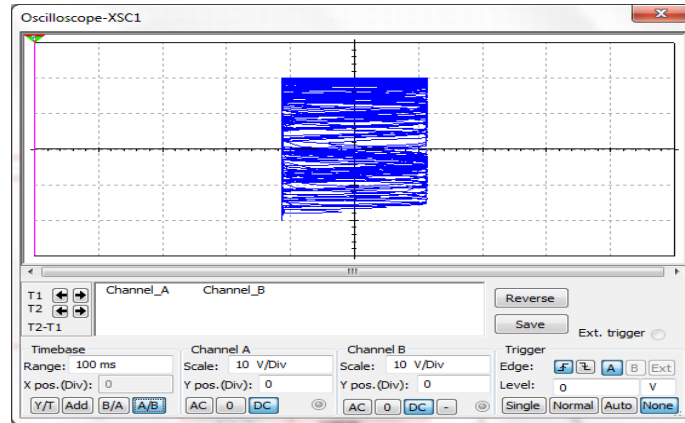


Figure 13. A/B (Output/Input)

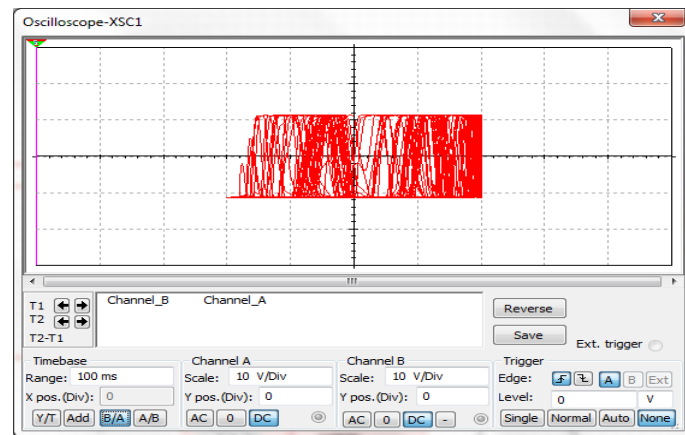


Figure 14. B/A (Output/Input)

From the above experiment for the different frequencies from 1Hz to 1 KHz sinusoidal input the output waveform becomes nonlinear.

**4. CONCLUSION**

The nonlinear passive element called Memristor is used and an emulator has been designed. The linear and nonlinear characteristics of the device are studied and also simulation work has been carried out using multisim. Indeed no physical memristor device was not available in market, Multisim is used and emulator circuit has been designed and device characteristics are analyzed. A simulation result depicts the effectiveness of the memristor. This study explicitly shows that memristor is effective in all aspects of linear and nonlinear characteristics.

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