A simple faulted phase-based fault distance estimation algorithm for a loop distribution system

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Article Info

ABSTRACT

This paper presents a single ended faulted phase-based traveling wave fault localization algorithm for loop distribution grids which is that the sensor can get many reflected signals from the fault point to face the complexity of localization. This localization algorithm uses a band pass filter to remove noise from the corrupted signal. The arriving times of the faulted phase-based filtered signals can be obtained by using phase-modal and discrete wavelet transformations. The estimated fault distance can be calculated using the traveling wave method. The proposed algorithm presents detail level analysis using three detail levels coefficients. The proposed algorithm is tested with MATLAB simulation single line to ground fault in a 10 kV grounded loop distribution system. The simulation result shows that the faulted phase time delay can give better accuracy than using conventional time delays. The proposed algorithm can give fault distance estimation accuracy up to 99.7% with 30 dB contaminated signal-to-noise ratio (SNR) for the nearest lines from the measured terminal.

Keywords:
Band pass filter
Discrete wavelets transform
Fault location
Loop distribution system
Noise
Traveling wave

1. INTRODUCTION

A fault in a power system interrupts a modern way of living. An ability to locate a fault in a power system loop distribution network is very important to improve reliability for customer satisfaction and utilities. The outage location is needed to know accurately to remove the outage line quickly from the remaining parts of the system. Therefore, different conventional fault distance estimation methods such as impedance-based method, frequency domain method, and traveling wave (TW) method are used to solve this problem.

Some researchers utilized impedance-based algorithms with the help of system fault signals [1], [2]. Next, the knowledge-based method has been used to detect the fault location using neural networks, decision trees and support vector machine techniques [3]-[7]. Some previous researcher used voltage sag matching algorithm in [8], comparing faulty phase voltage with measure value approach was used in [9] and weighted least square approach in [10] respectively. All the above algorithms require training data sets with pre-defined different fault situations.

Traveling wave-based algorithms can give the best accuracy with the help of discrete wavelet transforms (DWT) filters. Most of fault localization algorithms use the measured fault signals from single end of the system by identifying the first sudden changing point in the waveform [11]-[13]. This method was analyzing in time domain that cannot get accurate arriving time for high impedance faults. A simple fault localization algorithm based on characteristics of network topology and recloser-generating traveling wave
A simple faulted phase-based fault distance estimation algorithm for a loop distribution system (Shwe Myint)
The variable \( t_0 \) is the arriving time of the zero mode, which can be obtained using the residual current. The value can be calculated from (5).

\[
d = \frac{v_0 v_1 (t_2 - t_1)}{(v_1 - v_0)}
\]  

(5)

The zero-mode wave velocity can be estimated based on the system characteristic impedance,

\[
d = \frac{v_0 v_1 (t_2 - t_1)}{(v_1 - v_0)}
\]  

(6)

where \( L_0 \) is the zero-sequence inductance and \( C_0 \) is zero sequence capacitance of the power line. The arriving time of the aerial mode using different transformation can be calculated using the same in (7).

\[
d = \frac{v_0 v_1 (t_2 - t_1)}{(v_1 - v_0)}
\]  

(7)

The wave velocity of the aerial mode is given by (8),

\[
d = \frac{v_0 v_1 (t_2 - t_1)}{(v_1 - v_0)}
\]  

(8)

where \( L_1 \) and \( C_1 \) are positive sequence inductance and capacitance of the power line respectively. The arriving time of the aerial mode can be different depending on the transformation used to process the time domain signal. Using these different arriving times of aerial components can result different accuracies; therefore, the modal difference component and faulted phase-based arriving time are used and compared with that of the conventional aerial mode components.

### 2.2. Phase to modal transform

The phase components are transformed to modal components using Karenbauer’s transform to avoid mutual effects. The transformation matrix is shown in (9). The \( \alpha \), \( \beta \) and \( \gamma \) modal represent the difference between two current phases. On the other hand, the zero-modal (0) is similar to the zero component in the sequence network.

\[
d = \frac{v_0 v_1 (t_2 - t_1)}{(v_1 - v_0)}
\]  

(9)

In this article, the most accurate arriving time of aerial mode is chosen from the aerial components related with Park’s, Clark’s and Karenbauer’s transform, and aerial different component.

### 2.3. Wavelet transforms

The DWT splits into two components. They are approximation coefficients (cA) (low frequency) and detail coefficients (cD) (high frequency). Given an input signal \( x(k) \), its DWT can be calculated as (10),

\[
d = \frac{v_0 v_1 (t_2 - t_1)}{(v_1 - v_0)}
\]  

(10)

where \( a_0 \) is the scale factor, \( b_0 \) is the translation factor. The variable \( k \) represents an input sample number. Variables \( m \) and \( n \) represent mother wavelet and decomposed level, respectively.

In this paper, detail coefficients of db6 mother wavelet for level1, 2 and 3 are extracted and utilized to reconstruct the signals. The arriving times are detected from the component that is combining the three reconstructed signals using combinations of three detail levels, D1, D2 and D3 to obtain accurate arriving time of the reflected fault signal. The accuracy comparison of db4 and db6 was described in [20]. To estimate fault distance using traveling wave method, in this paper, faulted phase-based time delay is utilized. It is necessary to get correct faulted phase from the fault information accuracy and faulted line from previous work [20]. Figure 1 shows the three levels detail coefficients decomposition diagram.
A simple faulted phase-based fault distance estimation algorithm for a loop distribution system (Shwe Myint)

3. PROPOSED ALGORITHM

In this process, the recorded fault signals will firstly pass through the noise filter to remove noise from the input signal and then the filtered signals will be transformed to modal components to avoid mutual effects. In traveling wave fault location methods, the arriving times of fault signals are very important parameters to estimate fault distance, they can be extracted in time domain, sequence domain and wavelet domain as well. Therefore, the arriving times are extracted by using detail coefficients of DWT in this paper. After that, the correct faulted phase is detected by using fault information accuracy content in the three-phase current signals. Finally, the estimated fault distance can be estimated by using time delays of detail coefficients of modal current components. The process is generally illustrated in Figure 2. The arriving times of absolute maxima of detail coefficient of zero and aerial mode current traveling wave signals can be estimated by using db6 mother wavelet because db6 mother wavelet can give more accurate arriving time than db4 mother wavelet that is used by most of previous fault location researchers for that purpose.

4. SIMULATION RESULTS AND DISCUSSIONS

This paper uses a loop overhead distribution (modified IEEE 14-bus) test system that consists of three power supplies of 33 kV/10 kV, 50Hz as shown in Figure 3. The faults are simulated in one kilometer step on all branches of the test system. This paper uses the distributed line parameter model in the simulation. Before locating fault, the system firstly identifies the faulted line with the help of the fault detectors at all buses. Therefore, the fault detectors are installed at all buses of the test system. In this paper, the faulted section identification algorithm [25] is applied to get accurate faulted feeder. After obtaining faulty feeder, the system continues to estimate fault distance using only the recording signals from bus 1 (B1) for all lines.

Figure 1. DWT decomposition

Figure 2. Fault estimation process
of the test system. Various fault distances with fault resistance 0.001 $\Omega$ to 50 $\Omega$ considering noise effects with 30 to 70 signal-to-noise ratio (SNR) dB are simulated and analyzed as well. Total 1650 cases for 55 points with 100 iterations for every case are studied. System parameters are generator source resistance 13.96 $\Omega$ and source inductance of 0.35H.

4.1. Accuracy calculation

In the loop distribution system, there are many possible predefined fault distance values because there are many paths from the fault location to the measure terminal. For example, when a fault occurs at the middle of line (L7) which is 4 km long, there are five possible ways to get different five arriving signals from the fault point (F) to the measure terminal (B1). They are shown in the Figure 4.

According to these loops, possible actual fault distances from the measuring point are 8, 16, 10, 12 and 22 km that are possible actual fault distances for that case. Hence the range of possible fault distance (PFD) in this case is between 8 and 22 km. If the estimated fault distance (EFD) resides within the possible fault distance, the estimated fault distance is feasible. Otherwise, the algorithm assumes that the estimated distance is erroneous and should be discarded. This scenario can occur under noisy environment. Distance helps eliminate erroneous estimation. If the estimated fault distance is within the valid range, the algorithm can continue. Then we can access the performance of the algorithm by calculating the fault distance estimation accuracy (FDEAC) which can be defined by (11).

$$d = \frac{v_0 v_1 (t_2 - t_1)}{(v_1 - v_0)}$$  (11)
According to the example shown in Figure 4, the actual fault distance can have multiple values depending on the path the traveling wave take. Therefore, the algorithm must choose the possible fault distance from the list to calculate the accuracy value. In this paper, the value closest to the average estimated fault distance is chosen. If there are two possible AFD values, the smallest one is chosen.

For example, in the case of signals mixed with noise 60 SNR dB, and the estimated fault distance is 7.9908 km. Therefore, the actual fault distance would be 8km because it is the closest one to the estimated value in this case. The FDEAC is 99.89% by (11).

4.2. Arriving time based on faulted phase

This paper uses the arrival time of the mode related to the faulted phase to achieve better accuracy. For example, the arrival times of the travelling wave when phase ‘c’ to ground (CG) fault occurs in the middle of L7. Four modes of travelling wave are extracted from the simulation and shown in Table 1.

From this example, the arrival time of $\beta$ and $\gamma$ modal components are the same because they are related to phase ‘c’, the faulted phase. If wrong information is used, the estimation could be erroneous. Therefore, the proposed algorithm used the arriving time of faulted phase related modal component to get higher accuracy.

Table 1. Arriving times of detail coefficients of zero and aerial mode components when a single line to ground (CG) fault occurs at L7

<table>
<thead>
<tr>
<th>Components</th>
<th>Arriving time (ms)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$a$ modal</td>
<td>40.05</td>
</tr>
<tr>
<td>$\beta$ modal</td>
<td>40.03</td>
</tr>
<tr>
<td>$\gamma$ modal</td>
<td>40.03</td>
</tr>
<tr>
<td>Zero modal</td>
<td>40.15</td>
</tr>
</tbody>
</table>

4.3. Detail level analysis without noise

In order to obtain the time delay, the wavelet transform is used to localize the arrival time among different modes. This paper uses the db6 mother wavelet and three level of decomposition to extract the arrival time information. To verify the best accuracy, different combinations of detail coefficients are used to compare the fault estimation error. The cases are the arriving times taken from: i) the combination of reconstructed signals by using detail coefficients level1 (D1), level2 (D2) and level3 (D3) shown here as (D1+D2+D3); ii) the combination of reconstructed signals by using detail coefficients, D1 and D2, shown here as (D1+D2); iii) the reconstructed signals by using detail coefficients, D1; iv) the reconstructed signals by using detail coefficients, D2; and v) the reconstructed signals by using detail coefficients, D3, respectively. In this study, the proposed algorithm is tested with single line to ground (SLG) fault for all lines of test system. The result is shown in Table 2. Table 2 shows the performance of FDEAC for all lines of the test system without noise in the simulation. This accuracy using the time delay with combination of the fault information from the detail level 1, 2 and 3 (D1+D2+D3) give the best accuracy in five comparative cases, which is expected because they cover widest frequency range of all combinations.

Table 2. Average % of FDEAC for all lines with different detail levels without noise effects

<table>
<thead>
<tr>
<th>Faulted Lines</th>
<th>$D_1+D_2+D_3$</th>
<th>$D_1+D_2$</th>
<th>$D_1$</th>
<th>$D_2$</th>
<th>$D_3$</th>
</tr>
</thead>
<tbody>
<tr>
<td>L1</td>
<td>99.68</td>
<td>99.68</td>
<td>99.90</td>
<td>0.00</td>
<td>98.19</td>
</tr>
<tr>
<td>L2</td>
<td>99.75</td>
<td>99.97</td>
<td>99.68</td>
<td>99.68</td>
<td>98.90</td>
</tr>
<tr>
<td>L3</td>
<td>99.91</td>
<td>93.53</td>
<td>93.62</td>
<td>93.81</td>
<td>94.66</td>
</tr>
<tr>
<td>L4</td>
<td>99.82</td>
<td>99.82</td>
<td>85.91</td>
<td>99.82</td>
<td>99.68</td>
</tr>
<tr>
<td>L5</td>
<td>99.68</td>
<td>99.81</td>
<td>99.98</td>
<td>99.64</td>
<td>66.27</td>
</tr>
<tr>
<td>L6</td>
<td>99.89</td>
<td>99.58</td>
<td>99.79</td>
<td>99.79</td>
<td>85.52</td>
</tr>
<tr>
<td>L7</td>
<td>99.89</td>
<td>99.58</td>
<td>99.79</td>
<td>99.79</td>
<td>85.52</td>
</tr>
<tr>
<td>L8</td>
<td>99.89</td>
<td>94.44</td>
<td>94.27</td>
<td>99.99</td>
<td>99.82</td>
</tr>
<tr>
<td>L9</td>
<td>99.91</td>
<td>99.83</td>
<td>99.91</td>
<td>63.17</td>
<td>99.19</td>
</tr>
<tr>
<td>L10</td>
<td>99.85</td>
<td>99.98</td>
<td>99.93</td>
<td>99.98</td>
<td>99.65</td>
</tr>
<tr>
<td>L11</td>
<td>99.85</td>
<td>94.11</td>
<td>99.94</td>
<td>94.76</td>
<td>85.63</td>
</tr>
<tr>
<td>L12</td>
<td>99.92</td>
<td>95.63</td>
<td>95.63</td>
<td>98.48</td>
<td>99.92</td>
</tr>
<tr>
<td>L13</td>
<td>95.85</td>
<td>93.90</td>
<td>96.86</td>
<td>93.90</td>
<td>51.82</td>
</tr>
<tr>
<td>L14</td>
<td>99.85</td>
<td>88.52</td>
<td>99.94</td>
<td>88.52</td>
<td>80.95</td>
</tr>
<tr>
<td>L15</td>
<td>99.88</td>
<td>96.10</td>
<td>99.98</td>
<td>99.78</td>
<td>99.83</td>
</tr>
<tr>
<td>L16</td>
<td>99.92</td>
<td>97.50</td>
<td>99.99</td>
<td>97.50</td>
<td>89.40</td>
</tr>
</tbody>
</table>

Average 99.59 97.02 97.52 95.14 97.05
4.4. Detail level analysis with noise

In order to verify the accuracy of the set of detail coefficients used to extract the arrival time, the Gaussian white noise is added to simulate a practical situation where the input signal may be noisy. The simulation was done with SNR from 30 to 70 dB. The result is shown in Figure 5.

According to Figure 5, although the estimation accuracies by D_1 are the best in overall, the values are not significant in single case for five parameters with different detail levels. However, the parameter with combination of detail level 1, level 2, and level 3 can give better accuracy in high noise levels, such as 40dB and 50dB and the fault distance estimation accuracy by using this parameter for most of faulted lines are above 99%. Therefore, the arriving times for proposed fault distance estimation algorithm can be detected from the component that is a combination of reconstructed signals by using detail coefficients level 1, level 2 and level 3 (D_1+D_2+D_3) of db6 mother wavelet.

Figure 5. Performance of average FDEAC for all lines with different detail levels under different noise levels

4.5. Accuracy performance of proposed algorithm

Simulation results with additive noise of different signal-to-noise ratio are shown in Table 3. The results compare the average accuracy of fault distance estimation for the travelling wave using different delay time, including dq, d0 and modal transformation. Examples include all single line to ground faults.

According to the result in Table 3 in the case of phase ‘a’ to ground (AG) fault, higher accuracy can be obtained from the time delay of the faulted phase, meaning that the algorithm will use the time delay from \( \Delta t_\alpha \) or \( \Delta t_\beta \). The estimation result using the non-faulted phase, specifically \( \Delta t_\gamma \), gives low accuracy percentage. In addition, the estimation accuracy using time delay from the faulted phase is comparable to the time delay from traditional dq and d0 transformation.

In the case of phase ‘b’ to ground (BG) fault, a very good average accuracy can be found using the faulted phase time delay (\( \Delta t_\alpha \) or \( \Delta t_\beta \)) specifically above 99%. There is exception at 30 dB SNR cases. The accuracy gets lower because of higher noise interference. Furthermore, if the conventional time delay, \( \Delta t_d \), is used, the estimation error is less accurate for the BG fault.

Table 3. Average fault distance estimation accuracy percentage of proposed fault localization algorithm for fault occurred at L1

<table>
<thead>
<tr>
<th>Fault type</th>
<th>SNR (dB)</th>
<th>( \Delta t_\alpha )</th>
<th>( \Delta t_\beta )</th>
<th>( \Delta t_\gamma )</th>
<th>( \Delta t_d )</th>
</tr>
</thead>
<tbody>
<tr>
<td>AG</td>
<td>30</td>
<td>99.88</td>
<td>99.96</td>
<td>99.49</td>
<td>99.98</td>
</tr>
<tr>
<td>AG</td>
<td>40</td>
<td>99.56</td>
<td>99.51</td>
<td>99.54</td>
<td>99.51</td>
</tr>
<tr>
<td>AG</td>
<td>50</td>
<td>99.28</td>
<td>99.28</td>
<td>99.28</td>
<td>99.28</td>
</tr>
<tr>
<td>AG</td>
<td>60</td>
<td>99.96</td>
<td>99.26</td>
<td>99.26</td>
<td>99.26</td>
</tr>
<tr>
<td>AG</td>
<td>70</td>
<td>99.26</td>
<td>99.26</td>
<td>99.26</td>
<td>99.26</td>
</tr>
<tr>
<td>BG</td>
<td>30</td>
<td>31.10</td>
<td>26.63</td>
<td>31.80</td>
<td>13.85</td>
</tr>
<tr>
<td>BG</td>
<td>40</td>
<td>98.05</td>
<td>47.93</td>
<td>94.05</td>
<td>13.85</td>
</tr>
<tr>
<td>BG</td>
<td>50</td>
<td>99.84</td>
<td>73.91</td>
<td>99.88</td>
<td>18.96</td>
</tr>
<tr>
<td>BG</td>
<td>60</td>
<td>99.63</td>
<td>91.27</td>
<td>99.66</td>
<td>89.67</td>
</tr>
<tr>
<td>BG</td>
<td>70</td>
<td>99.28</td>
<td>98.40</td>
<td>99.28</td>
<td>82.00</td>
</tr>
<tr>
<td>CG</td>
<td>30</td>
<td>97.87</td>
<td>99.56</td>
<td>40.04</td>
<td>99.64</td>
</tr>
<tr>
<td>CG</td>
<td>40</td>
<td>98.79</td>
<td>99.79</td>
<td>22.37</td>
<td>99.79</td>
</tr>
<tr>
<td>CG</td>
<td>50</td>
<td>99.10</td>
<td>99.26</td>
<td>61.25</td>
<td>99.26</td>
</tr>
<tr>
<td>CG</td>
<td>70</td>
<td>99.26</td>
<td>99.26</td>
<td>49.10</td>
<td>99.26</td>
</tr>
</tbody>
</table>
Finally, in the case of phase ‘c’ to ground (CG) fault, the fault distance estimation result using the information from the faulted phase ($\Delta t_\beta$ or $\Delta t_\gamma$) gives above 99% accuracy. In addition, the proposed algorithm using the faulted phase time delay can get better accuracy than the conventional time delay under low signal-to-noise ratio (30dB and 40dB). These results are similar to the (AG) fault cases.

According to the result shown in Table 3, the proposed algorithm has demonstrated that the time delay of that related to the faulted phase of the transform current waveform using Karenbauer’s transformation give the best accuracy. Furthermore, in case of the single phase to ground fault, two time-delay parameters should be the very close, for example, $\Delta t_\alpha$ and $\Delta t_\beta$ for phase ‘a’ to ground fault. Therefore, the algorithm can use this information to verify the result as well.

To demonstrate an overall performance, the averaged fault distance accuracy percentage of all lines are shown in Figure 6. The results show that the performance of average fault distance estimation accuracy for all lines with additive noise at 70 dB SNR. The simulations were done for high fault current at 0.001 Ohm fault resistance shown in Figure 6(a) and moderate fault resistance at 50 Ohms shown in Figure 6(b). Each subfigure shows average fault distance estimation accuracy using three-time delays: d0 time delay, dq time delay and faulted phase (FP) time delay to compare the overall accuracy.

According to the result in Figure 6, the proposed FP subscription time delay ($\Delta t_\alpha$, $\Delta t_\beta$, and $\Delta t_\gamma$) gives better averaged accuracy than the conventional time delays ($\Delta t_d$ and $\Delta t_{dq}$) for fault distance estimation in case of faults in most lines. The averaged estimation accuracy for fault on line 13 is worse than the algorithm that use the $\Delta t_{dq}$ time delay. However, this recording was done at Bus 1, which is far away. Different point of observation can be done to double check or narrow down the fault location. The result on line 4 at 50 Ohms fault resistance is also worse than the 0.001 Ohm fault resistance case. This may be due to shorter distance and lower fault signal causing the wavelet to give the inaccurate time delay. However, overall performance is good for fault on all lines in this network topology. Hence, the time delay of the faulted phase should be used to calculate the fault distance.

![Figure 6. Average fault distance estimation accuracy for all lines with SNR=70 dB for](attachment:figure6.png)
The performance of overall average estimation accuracy for all specified SNR values is illustrated in Figure 7(a) for 0.001 Ohm minimum fault resistance and Figure 7(b) for 50 Ohm maximum assumed fault resistance respectively. In Figure 7, The results compare the fault distance estimation accuracy all lines with the same SNR. Three lines represents the value estimated with d0 time delay, dq time delay and FP time delay to demonstrate the advantage of the proposed algorithm.

![Figure 7. Overall average estimation accuracy in all lines with SNR= 30 to 70dB for (a) R_f = 0.001\(\Omega\) and (b) R_f = 50 \(\Omega\)](image)

According to the result in Figure 7, the averaged estimation accuracy of the proposed faulted phase time delay demonstrates that it gives better accuracy than conventional time delay from aerial component (\(\Delta t_d\)) and aerial different component (\(\Delta t_{dq}\)) for all the noise case. This is due to the fact that the faulted phase contains more information about the fault than the healthy line, which used in the conventional dq transformation. Hence, the proposed algorithm has demonstrated that it can accurately locate the fault in a loop transmission under the simulation even with additive noise.

5. CONCLUSION

This paper proposes a simple fault localization technique in loop distribution systems. The proposed technique passed through band pass filter, Karenbauer’s transform, and wavelet transform criteria to estimate for fault distance by using only three phase current signals at the source bus (B1) of the test loop distribution network. The proposed algorithm uses the arriving time of faulted phase-based modal component that can give higher accuracy than that of conventional methods with the consideration of noise effects, such
as white noise. According to detail level analysis section, using the arriving times of the component combined the three reconstructed signals using three detail level coefficients (D1, D2 and D3) can give best accuracy. The proposed algorithm shows that the faulted phase time delay can give better accuracy than using conventional time delay and aerial different time delay.

The algorithm performance is successfully tested with data obtained by simulations with 1650 different cases of sampled data at various situations, faulted feeders, faulted resistance, 30 to 70 dB SNR values and fault locations. The proposed methodology is evaluated through MATLAB/Simulation single line to ground fault in a 10 kV grounded loop distribution system. The proposed algorithm can give fault location accuracy up to 99.7% with 30 dB contaminated SNR for the nearest lines from the measured terminal. Using proposed algorithm, the overall fault information accuracy can get up to 83% and overall fault distance estimation accuracy up to 93%. This proposed technique can be used to implement in real data with actual fault records.

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REFERENCES


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