Fault diagnosis of a squirrel cage induction motor fed by an inverter using lissajous curve of an auxiliary winding voltage

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ABSTRACT

The development of power electronic components has allowed the increase of the induction machine performance. Indeed, monitoring squirrel cage induction motors driven through rectifiers and inverters has been a major concern. This paper presents a new method to diagnose the combination inverter-machine faults. This technic considers an auxiliary winding which is a small coil inserted between two stator phases. It is based on Lissajous curve of this auxiliary winding voltage Park components. For this purpose, modeling the electromechanical conversion chain is necessary. The focus will particularly be on modeling both the squirrel cage induction machine and the inverter in a non-defected case which is a reference. Moreover, the explicit expressions developed for the inserted winding voltage and its Park components will be presented. The simulation results show the effectiveness of the proposed method.

Keywords:
Auxiliary winding voltage
Diagnosis
Inverter
Lissajous curve
Squirrel cage motor

1. INTRODUCTION

Through considerable technological progress in the power electronics field over recent years, the power electronic converters are extensively used in different applications making varying speed drive of induction machines possible by adjusting the frequency of the applied voltages. This amount use refers to the ability of these converters to improve the static and dynamic characteristics efficiency and limit the requirements of machines, due to high capability of the inverter to ensure flexible voltage and frequency variation, which is the case of electromechanical conversion chain.

The electromechanical conversion chain is a structure that is widely used and occupies a privileged place in the industrial sector. It consists of a squirrel cage induction machine fed by a power electronic inverter connected to a rectifier that converts the alternative voltage to the continuous one, fed by a transformer related to a power grid of a medium distribution voltage as shown in Figure 1. The connection between the rectifier and the inverter called DC link and it is generally equipped with a filter.

The squirrel cage induction machine is the principal drive in our chain, it is known for its simplicity, robustness and its low maintenance cost. Associating this machine with the power devices adds extremely interesting performance to be used in variable speed drives. In this case, the machine is not fed directly from the power grid but supplied from a switched voltage waveform created by an inverter. This voltage will change because of many reasons [1] such as one or multiple of its power switches fail that can lead to critical damage throughout the chain especially the motor.
Despite all the squirrel cage induction motor advantages, no industrial system is immune from failure. Therefore, a monitoring system and online diagnosis become a must for anticipating the risk of a defect with incipient fault detection for instance. According to signals nature, different techniques have been used for rotor faults such as broken rotor bars, broken end rings and eccentricity [2, 3]. For instance, motor current signature analysis (MCSA) is one of the instruments used for monitoring the induction machine, it focuses on the spectrum analysis of the stator current with evaluating the amplitude of the appearing current harmonics over a constant torque [4, 5]. On the other hand, wavelet transform (WT) is required for nonconstant torque or nonstationary signals, this method can be divided into two types discrete (DWT) [6] and continuous wavelet transform (CWT) [7]. The fast fourier transform spectral signature analysis (FFT) [8, 9] is the most popular technique for detecting broken rotor bars fault. This method is limited only on stationary and linear signals. Moreover, it presents problems to analyse noisy signals [10, 11]. There are also vibration signals and current signals approach which present a problem during the acquisition of mechanical signal or current signature related to failure [12].

This paper presents a new diagnosis methodology based on the so-called auxiliary winding voltage signal approach. In fact, the aim of this technique is monitoring the voltage of an auxiliary small coil “sneak” inserted between two of the stator phases. This analytical procedure is expected to yield accurate predictions regarding monitoring squirrel cage induction machine failures through the Lissajous curve of the auxiliary winding voltage [13]. For that purpose, modeling of the combination inverter-squirrel cage induction machine as a meshed circuit is presented.

2. INVERTER - SQUIRREL CAGE INDUCTION MACHINE MODELING

Explaining the squirrel cage motor the three-phase DC/AC inverters turn out to be one of the most circuit configuration used for induction machine speed control due to their high capability to ensure flexible voltage and frequency variation [14].

Three-leg inverter consists of six IGBT’s with anti-parallel diodes for bidirectional power flow. The insulated gate bipolar transistor is a semiconductor device that can combine high efficiency and fast switching. The two switches $S_j, \bar{S}_j$ in the same leg cannot be turned ON at the same time. They are complementary. Their state is defined as:

$$S_j = \begin{cases} +1 & \text{if } j = a, b, c \\ -1 & \text{otherwise} \end{cases}$$

As we are dealing with balanced three phase voltages, we have $V_{an} + V_{bn} + V_{cn}=0$, thus we found $V_{n0}$ as:

$$V_{n0} = \frac{V_{a0} + V_{b0} + V_{c0}}{3}$$

From (2) the line-to-neutral voltages are presented in matrix form as:

$$\begin{bmatrix} V_{an} \\ V_{bn} \\ V_{cn} \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 2 & -1 & -1 \\ -1 & 2 & -1 \\ -1 & -1 & 2 \end{bmatrix} \begin{bmatrix} V_{a0} \\ V_{b0} \\ V_{c0} \end{bmatrix}$$

Where the three leg voltage ($V_{a0}, V_{b0}, V_{c0}$) is measured relatively to the negative terminal of the DC voltage (E), and the phase voltage ($V_{an}, V_{bn}, V_{cn}$) measured relative to the neutral N. The AC output line voltages ($V_{ab}, V_{bc}, V_{ca}$) can only switch between these voltages values $E, 0, and -E$. A three-leg inverter has eight possible switching-states (000~111) including six non-zero voltage vectors and two zero voltage vectors(000,111) which are listed in Table 1 [15].
Table 1. The switching states in a three-phase inverter

<table>
<thead>
<tr>
<th>$S_a$</th>
<th>$S_b$</th>
<th>$S_c$</th>
<th>$V_{sa}$</th>
<th>$V_{sb}$</th>
<th>$V_{sc}$</th>
<th>$V_{rs}$</th>
<th>$V_{se}$</th>
<th>$V_{in}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>$E$</td>
<td>$E$</td>
<td>$E$</td>
</tr>
<tr>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>$\frac{E}{2}$</td>
<td>$-\frac{E}{2}$</td>
<td>$\frac{E}{2}$</td>
<td>$-\frac{E}{2}$</td>
<td>$\frac{E}{2}$</td>
</tr>
<tr>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0</td>
<td>$\frac{E}{2}$</td>
<td>$-\frac{E}{2}$</td>
<td>$\frac{E}{2}$</td>
<td>$-\frac{E}{2}$</td>
<td>$\frac{E}{2}$</td>
</tr>
<tr>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>$\frac{E}{2}$</td>
<td>$-\frac{E}{2}$</td>
<td>$\frac{E}{2}$</td>
<td>$-\frac{E}{2}$</td>
<td>$\frac{E}{2}$</td>
</tr>
<tr>
<td>1</td>
<td>0</td>
<td>1</td>
<td>$E$</td>
<td>0</td>
<td>$\frac{E}{2}$</td>
<td>$\frac{E}{2}$</td>
<td>$\frac{E}{2}$</td>
<td>$\frac{E}{2}$</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td>0</td>
<td>$E$</td>
<td>0</td>
<td>$\frac{E}{2}$</td>
<td>$\frac{E}{2}$</td>
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<td>$\frac{E}{2}$</td>
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<tr>
<td>1</td>
<td>1</td>
<td>1</td>
<td>$E$</td>
<td>$E$</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

A squirrel cage induction motor model is built considering that the stator is a three phase winding and the rotor cage can be regarded as a whole of meshes representing the $N_r$ rotor bars similarly separated and short-circuited together by two identical end rings as shown in Figure 2.

Figure 2. Multi-winding model of a cage asynchronous motor

$I_{rk}$ with $k = 1 \ldots N_r$ are the $N_r$ rotor loops current and $i_e$ is one of the end rings current.
These loops are connected between them electrically and coupled magnetically. The current in each
circuit is considered as an independent variable. The induction motor model takes into account the machine
geometric construction and the following assumptions [16, 17]:

a) Sinusoidally distributed stator windings.
b) Infinity iron permeability.
c) Neglecting saturation.
d) Uniform air gap.
e) Neglecting inter-bar currents.
f) Evenly distributed rotor bars.
g) Neglecting flux coupling between different winding without air gap crossing.

The motor matrix mathematical model can be written as:

$$[V_s] = [R_s] [I_{3s}] + \frac{d[\phi_{3s}]}{dt}$$  \quad (4)

With,

$$[\phi_{3s}] = [L_s] [I_{3s}] + [M_{sr}] [I_r]$$  \quad (5)

$$\begin{bmatrix} [V_r] \\ [V_e] \end{bmatrix} = \begin{bmatrix} [R_e] & \frac{R_e}{N_r} \\ \frac{R_e}{N_r} & R_e \end{bmatrix} \begin{bmatrix} [I_r] \\ i_e \end{bmatrix} + \frac{d}{dt} \begin{bmatrix} [\phi_r] \\ \phi_e \end{bmatrix}$$ \quad (6)

$$\begin{bmatrix} [\phi_r] \\ \phi_e \end{bmatrix} = \begin{bmatrix} [M_{rs}] [I_{3s}] \\ 0 \end{bmatrix} + \begin{bmatrix} [L_r] & \frac{i_e}{N_r} \\ \frac{i_e}{N_r} & L_e \end{bmatrix} \begin{bmatrix} [I_r] \\ i_e \end{bmatrix}$$ \quad (7)
Where, \([V]\) is the voltage vector, \([i]\) is the currents vector, \([R_s]_{3x3}\) and \([R_r]_{N_r \times N_r}\) are the stator and rotor resistances matrices respectively. Whereas \([L_s]_{3x3}\) is the stator winding inductance matrix, \([L_r]_{N_r \times N_r}\) is the rotor inductance matrix, \([M_{sr}]_{3xN_r}\) is the mutual inductance matrix between stator and rotor, \([\phi_s]\) and \([\phi_r]\) are the stator and rotor fluxes vectors respectively.

Furthermore,

\[
[R_s] = \begin{bmatrix} R_s & 0 & 0 \\ 0 & R_s & 0 \\ 0 & 0 & R_s \end{bmatrix}
\]  

(8)

\[
[R_r] = \begin{bmatrix} R_{b0} + R_{b(N_r-1)} + 2 \frac{R_e}{N_r} & 0 & \cdots & 0 \\ -R_{b1} & R_{b1} & \cdots & 0 \\ 0 & \cdots & \ddots & \cdots \\ -R_{b(N_r-1)} & 0 & \cdots & 0 \\ \end{bmatrix}
\]  

(9)

According to winding function approach, the inductance between two windings ‘‘i’’ and ‘‘j’’ in any electric machine can be calculated by the following [18] and [19]:

\[
L_{ij}(\varphi) = \mu_0 L \int_0^{2\pi} \frac{n_i(\varphi, \theta) N_j(\varphi, \theta)}{e(\varphi, \theta)} d\theta
\]  

(10)

\(n_i(\varphi, \theta)\) is the winding distribution of coil ‘‘i’’, \(N_j(\varphi, \theta)\) is the winding function of coil ‘‘j’’. It represents the magneto motive force distribution along the air gap, \(\varphi\) is the rotor angular position, \(\theta\) is the particular angular position along the stator inner surface, \(e\) is the air gap length, \(r\) is the average radius of the air gap and \(L\) is the motor effective stack length [20].

We add the leakage inductances to the self-inductances. Therefore, the inductances matrices can be obtained from (10) as follows [21, 22]:

\[
[L_s] = \begin{bmatrix} L_{sp} + L_{sf} & M_{sa} & M_{sa} s \\ M_{sb} & L_{sp} + L_{sf} & M_{sb} s \\ M_{sc} & M_{sc} s & L_{sp} + L_{sf} \end{bmatrix}
\]  

(11)

\[
[L_r] = \begin{bmatrix} L_{rp} + 2L_b + 2 \frac{L_e}{N_r} & M_{rr} - L_b & \cdots & \cdots & M_{rr} - L_b \\ M_{rr} - L_b & L_{rp} + 2L_b + 2 \frac{L_e}{N_r} & M_{rr} - L_b & \cdots & \cdots \\ \vdots & \vdots & \ddots & \ddots & \vdots \\ M_{rr} - L_b & \cdots & M_{rr} - L_b & L_{rp} + 2L_b + 2 \frac{L_e}{N_r} & M_{rr} - L_b \\ M_{rr} - L_b & \cdots & \cdots & M_{rr} - L_b & L_{rp} + 2L_b + 2 \frac{L_e}{N_r} \end{bmatrix}
\]  

(12)

And,

\[
[M_{sr}] = \begin{bmatrix} -L_{sr} \cos(\theta + ka) & \cdots \\ \cdots & \cdots \\ -L_{sr} \cos(\theta + ka - 2\pi/3) & \cdots \\ \cdots & \cdots \\ -L_{sr} \cos(\theta + ka - 4\pi/3) & \cdots \end{bmatrix}
\]  

avec \([M_{rs}] = [M_{sr}]^T\)

(13)

Using park transformation in the case of a fixed rotor reference frame, we transform the three-phase stator windings \(a\), \(b\) and \(c\) in three orthogonal \(d\), \(q\) and \(o\) windings. The overall mathematical model machine equations in the axis system \(d\), \(q\) can be written as follows:

\[
\frac{d[i]}{dt} = -[L]^{-1} \left([R] + \frac{d[L]}{dt}\right)[i] - [L]^{-1}[V]
\]  

(14)
Where $[I] = \begin{bmatrix} i_d(q) \\ i_r \end{bmatrix}$ and $[V] = \begin{bmatrix} V_d(q) \\ V_r \end{bmatrix}$ with $V_e = 0$.

The globale resistance and inductance matrixes can be written as:

$$
[R] = \begin{bmatrix} R_s & 0 & 0 \\ 0 & R_x & \frac{R_e}{N_r} \bigl[1_{N_r \times 1} \bigr] \\ 0 & \frac{R_e}{N_r} \bigl[1_{N_r \times 1} \bigr] & R_e \end{bmatrix}
$$

(15)

$$
[L] = \begin{bmatrix} L_s & M_{sr} \\ M_{sr} & L_x \bigl[1_{N_r \times 1} \bigr] \\ 0 & \frac{L_e}{N_r} \bigl[1_{N_r \times 1} \bigr] \end{bmatrix}
$$

(16)

According to the fundamental equation of dynamics, the evolution of the mechanical speed is expressed as below:

$$
\begin{bmatrix} \frac{d\omega}{dt} \\ \omega \end{bmatrix} = C_{em} - C_r - f_v \omega
$$

(17)

$$
C_{em} = \frac{\sqrt{3}}{2} p L_{sr} \left( I_{qs} \sum_{k=0}^{N_r-1} l_{rk} \cos(Ka) - I_{ds} \sum_{k=0}^{N_r-1} l_{rk} \sin(Ka) \right)
$$

(18)

With:

$$
L_{sr} = \frac{4 \mu_0 N_s R_l}{en p^2} \sin(a/2), \quad a = \frac{2\pi}{N_e} p \text{ and } K = 0, \ldots, N_r
$$

Where $C_{em}$ is the electromagnetic torque, $C_r$ is the load torque, $\omega$ is the mechanical speed and $f_v$ is the friction coefficient. The geometric parameters $R$, $L$, and $e$ are defined respectively as the air gap mean radius, the stack length, and the ring thickness.

### 3. SQUIRREL CAGE INDUCTION MACHINE FED BY AN INVERTER SIMULATIONS

The mathematical model of a squirrel-cage induction motor fed by an inverter is developed and simulated by MATLAB. The simulation results are given below for a three-phase non-defected 450W motor. The machine parameters values are given in Table 2.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>quantity</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$V$</td>
<td>Power supply voltage</td>
<td>220/380 V</td>
</tr>
<tr>
<td>$f$</td>
<td>Frequency</td>
<td>50 Hz</td>
</tr>
<tr>
<td>$p$</td>
<td>Number of pole pairs</td>
<td>1</td>
</tr>
<tr>
<td>$N_s$</td>
<td>Number of rotor bars</td>
<td>27</td>
</tr>
<tr>
<td>$N_r$</td>
<td>Number of</td>
<td>193</td>
</tr>
<tr>
<td>$E$</td>
<td>Ring thickness</td>
<td>0.38 mm</td>
</tr>
<tr>
<td>$R$</td>
<td>Air gap mean radius</td>
<td>37.5</td>
</tr>
<tr>
<td>$L$</td>
<td>Stack length</td>
<td>60 mm</td>
</tr>
<tr>
<td>$R_s$</td>
<td>Resistant stator winding</td>
<td>4.1Ω</td>
</tr>
<tr>
<td>$R_b$</td>
<td>Resistance of a rotor bar</td>
<td>74 μΩ</td>
</tr>
<tr>
<td>$R_e$</td>
<td>Resistance of the rotor end ring</td>
<td>74 μΩ</td>
</tr>
<tr>
<td>$L_b$</td>
<td>Leakage inductance of rotor bars</td>
<td>0.33 μH</td>
</tr>
<tr>
<td>$L_e$</td>
<td>Leakage inductance of rotor end rings</td>
<td>0.33 μH</td>
</tr>
<tr>
<td>$J$</td>
<td>Moment of inertia</td>
<td>$4.5 \times 10^{-3} \text{Nm}^2$</td>
</tr>
</tbody>
</table>

Table 2. Squirrel cage induction motor parameters
Figure 3 and Figure 4 show the induction motor speed and torque respectively under normal condition. The maximum speed value achieved in this condition is about 310 rad/sec that still maintained within 0.5sec. The starting torque is about 7.5Nm and is variable from 0 to 0.3 sec as shown in Figure 4. During the steady-state, oscillations appear at the speed and the electromagnetic torque curves.

![Figure 3. The induction motor speed](image1)
![Figure 4. Electromagnetic torque](image2)

**4. AUXILIARY WINDING VOLTAGE PARK COMPONENTS**

The method consists of inserting an auxiliary winding which is a small coil “sneak” that forms an angle $\theta_0$ with the A stator phase as shown in Figure 5. This coil has no conductive contact with the other phases but it is mutually coupled with all the other circuits on both the stator and rotor sides. This technic was applied previously for a wound rotor induction motor [15-24, 25].

![Figure 5. Auxiliary winding emplacement inside the squirrel cage induction motor](image3)

The position of this added coil is chosen that all electrical magnitudes can be measured such as voltage and flux. The Lissajous curve of the auxiliary winding voltage Park components is the major criterion of the proposed method, monitoring this factor enabling efficient detection of failures. For that purpose, the auxiliary winding voltage expression is the main key of this technic.

**4.1. Diagnostic system mathematical model**

**4.1.1. Auxiliary winding voltage**

After applying the fourth order Runge-Kutta method to resolve numerically the differential matrix in (14), we obtain the current vector used to determine the auxiliary winding flux [15-25]

$$\varphi_{aux} = a \, I_{sa} + b \, I_{sb} + c \, I_{sc} + \sum_{i=1}^{N_r} d_i I_{ri}$$  \hspace{1cm} (19)

The coefficients $a$, $b$, $c$ and $d_i$ depend on the angle $\theta_0$ such as:
\[ a = M_{saux} \cos(\theta_0) \]
\[ b = M_{saux} \cos\left(\frac{2\pi}{3} - \theta_0\right) \]
\[ c = M_{saux} \cos\left(\frac{4\pi}{3} - \theta_0\right) \]
\[ d_j = M_{raux} \cos\left(\theta + \frac{j\pi}{3}\right), j = 0, 2, 4, \ldots \]

\( M_{saux}, M_{raux} \) are the stator and rotor auxiliary winding mutual inductances respectively.

The flux in (19) lead to the auxiliary winding voltage expression:
\[ V_{aux} = \frac{d\varphi_{aux}}{dt} \quad (20) \]

In order to use the Lissajous curve for our model, the determination of the auxiliary winding voltage Park components is essential. For that purpose, it is necessary to apply the Park transformation to the auxiliary winding voltage system in order to obtain the two components \( V_{auxd}, V_{auxq} \), we should consider two other fictive coils forming with the inserting coil a three phase system. Then,
\[ V_{auxa} = \frac{d\varphi_{auxa}}{dt}, V_{auxb} = \frac{d\varphi_{auxb}}{dt}, V_{auxc} = \frac{d\varphi_{auxc}}{dt} \quad (21) \]

With,
\[
\begin{bmatrix}
\varphi_{auxa} \\
\varphi_{auxb} \\
\varphi_{auxc}
\end{bmatrix} = \begin{bmatrix}
I_s \\
I_{sb} \\
I_{sc} \\
I_{r1} \\
\vdots \\
I_{rN_r}
\end{bmatrix}
\begin{bmatrix}
A
\end{bmatrix}_{3 \times Nr}
\quad (22)
\]

\([A]_{3 \times Nr}\) is the coefficients matrix when \( \theta_0 = 0 \). We choose the angle value equals to zero because using different values of it doesn't have any influence on simulations results. Thus \( \varphi_{auxa} \) is representing as:
\[ \varphi_{auxa} = \varphi_{sa} + \varphi_{sb} + \varphi_{sc} + \sum_{i=1}^{Nr} \varphi_{ri} \quad (23) \]
\[ \varphi_{auxa} = M_{saux} I_s - \frac{M_{saux}}{2} I_{sb} - \frac{M_{saux}}{2} I_{sc} + \sum_{i=1}^{Nr} M_{raux} \cos\left(\theta + \frac{j\pi}{3}\right) I_{r1,j}, j = 0, 2, 4, \ldots \quad (24) \]

The flux Park components is defined as:
\[ \varphi_{auxad} = \frac{\sqrt{3}}{2}\left(\varphi_{auxa} \cos(\theta_0) + \varphi_{auxb} \cos\left(\frac{2\pi}{3} - \theta_0\right) + \varphi_{auxc} \cos\left(\frac{4\pi}{3} - \theta_0\right)\right) \quad (25) \]
\[ \varphi_{auxaq} = -\frac{\sqrt{3}}{2}\left(\varphi_{auxa} \sin(\theta_0) + \varphi_{auxb} \sin\left(\frac{2\pi}{3} - \theta_0\right) + \varphi_{auxc} \sin\left(\frac{4\pi}{3} - \theta_0\right)\right) \quad (26) \]

The expressions of the auxiliary winding voltage Park components are obtained from the derivatives of its flux Park components such as:
\[ V_{auxad} = \frac{d\varphi_{auxad}}{dt} \; \text{and} \; V_{auxaq} = \frac{d\varphi_{auxaq}}{dt} \quad (27) \]

Where,
\( \varphi_{auxad} \) is the direct component of the auxiliary winding flux.
\( \varphi_{auxaq} \) is the indirect component of the auxiliary winding flux.
\( V_{auxad} \) is the direct component of the auxiliary winding voltage.
\( V_{auxaq} \) is the indirect component of the auxiliary winding voltage.
5. AUXILIARY WINDING VOLTAGE SIMULATION RESULTS

The simulations were performed for a non-loaded machine fed by an inverter and for a 0.5Nm and 1.5Nm loaded machine, this step is necessary to build an efficient knowledge about the machine state. The Lissajous curve of the auxiliary winding voltage Park components is considered as an index of the squirrel-cage induction motor quality which informs us about the working conditions of the machine.

The curves obtained in the case of a healthy motor fed by an inverter are considered as a reference to which the results obtained in the next study presenting the broken bar motor cases will be compared. Figure 6(a) shows the Lissajous curve of the auxiliary winding voltage Park components. It has a flower shape with six petals representing the number of the inverter switches. This shape clearly shows the difference between the squirrel cage motor fed by an inverter and the one fed by a sinusoidal voltage source where the Lissajous curve is a circle as shown in Figure 6(b).

![Figure 6](image)

*Figure 6. Lissajous curve of auxiliary winding voltage Park components in case of a no-loaded motor, (a) motor fed by an inverter, (b) motor fed by a sinusoidal voltage*

Two sec after its starting, the motor is loaded with Cr=0.5Nm and then with Cr=1.5Nm. The figures below show the Lissajous curve of auxiliary winding voltage Park component in the case of different loads. When the load increase, the flower becomes wider and its six petals widened also. The maximum value changes from about 200 V to 300 V as shown in Figure 7. The flower orientation also changes according to the level of the load. The change of the Lissajous curve shape approves clearly the validity of this technic in the case of a healthy squirrel cage motor. The change of the Lissajous curve shape approves clearly the validity of this technic in the case of a healthy squirrel cage motor.

![Figure 7](image)

*Figure 7. Lissajous curve of auxiliary winding voltage Park components, (a) In case of Cr=0.5Nm, (b) In case of Cr=1.5Nm*
6. CONCLUSION

In this paper, a new technic to diagnose the squirrel cage induction motor fed by an inverter is presented. It is based on Lissajous curve of an auxiliary winding voltage Park components. The method was verified by simulation for a healthy combination motor-inverter. It gives satisfactory results when the machine is loaded at different levels. The shape of the Lissajous curve is a flower with six petals that widens proportionally with the motor load. The efficiency of this approach mainly depends on monitoring the Lissajous curve behaviour of an auxiliary winding voltage Park components. The implementation of this diagnosis approach in the cases of the motor broken bars and its broken end rings faults detection will be presented in a future work.

REFERENCES


Fault diagnosis of a squirrel cage induction motor fed by an inverter using... (Yakov Khadouj Jelbaoua)


**BIOGRAPHIES OF AUTHORS**

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